

Density Functional Theory(DFT) Study of Alkali-Metal-Based Half-Heusler Compound NaCrSb

Abstract

In this study we investigated half-Heusler alloy (NaCrSb) using density functional theory as implemented in Quantum espresso software version qe-6.8 for simulation on ubuntu operating system version 22.04LTS. The Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation (GGA) was used for the exchange-correlation potential. The projector augmented-wave (PAW) method was employed to describe the core electrons. The material NaCrSb is structurally stable from studied at beta (β)-phase. The half-Heusler alloy has measured band gap of 1.93eV was obtained for NaCrSb, with a range of values. This indicates that NaCrSb is an indirect bandgap semiconductor material. The compound NaCrSb exhibits behavior during spin up and down that is characteristic of both metals and semiconductors, which foretells the half-metallic Heusler alloy. The B/G ratio of 2.53 indicates that the NaCrSb material is ductile. The material's resistance to impact is addressed holistically by the Vicker's hardness. Na-1s and Na-3s; Cr-1s, Cr-2p, Cr-3s; and Sb-1s, Sb-2s, Sb-3p has high orbital contribution for the Na, Cr, and Sb-atoms. At fermi energy both the spin up and spin down is at zero point in plot of partial density of state (PDOS) against energy. It became vivid from this that NaCrSb is a half-metallic Heusler alloy. Positive frequencies were detected in the phonon dispersion curves along the $\Gamma - \Gamma - K - \Gamma - L - W - \Gamma$ high symmetry directions. This suggests that NaCrSb is dynamically stable. The search for new materials with special qualities is what propels progress in materials research and technology.

Key words: Half-Heusler; Half-metallic; electronic band structure; mechanical properties; density of state; phonon, alloy

1. 0. Introductions

The origin of the name "half Heusler" stems from their structural similarity to Heusler alloys which have similar crystal structure but are composed of equal proportions of two metallic elements. The thermoelectric applications of half Heusler alloy are particularly noteworthy, as they can efficiently convert waste heat into electricity or vice versa. This property is crucial for energy harvesting and power generation technologies. Additionally, half Heusler alloys have shown promise in magnetic refrigeration, spintronics and catalysis. According to a study Smith and Johnson (2023). Half-Heusler alloy exhibit promising thermoelectric properties. (Ettah et al., 2023). Half Heusler thermoelectric materials for applications in power generation and refrigeration. Half-Heusler alloy are a class of intermetallic compounds with the chemical formula XYZ , where X is typically a transition metal. Y is a metal (e.g. Co, Fe), and Z is a metalloid (e.g. Ti, Zr), (Coey *et al.*, 2010). Importance of density functional theory (DFT) density functional theory is a powerful computational method used to study the electric structure, energetic and properties of materials at the atomic scale. It provides a theoretical framework for predicting the behaviour of materials based on the principles of quantum mechanics, without the need for empirical parameters. DFT calculations have been widely employed to investigate the properties of Half-Heusler Alloys, offering insights into their structural stability, electronic properties,

mechanical behaviour, thermodynamic stability and phonon properties. DFT calculations are used to determine the equilibrium crystal structure of Half-Heusler alloys including lattice parameters, atomic positions and structural stability. Studies have investigated the effects of composition, doping and strain on the structural properties of Half-Heusler alloys (Zhang *et al.*, 2016).

DFT enables the calculations of electronic band structures, density of states (DOS) and charge densities of Half-Heusler alloys. These properties are crucial for understanding the materials electrical conductivity, band gap and electronic transport behaviour, first principles calculations have been used to predict the electronic properties of Half-Heusler alloys and identify potential candidates for thermoelectric application (Wang *et al.*, 2018). DFT can determine various mechanical properties of Half-Heusler alloys, such as elastic constants, bulk modulus, shear modulus and young's modulus. These properties are essential for understanding the materials stability, deformation behaviour and response to external forces (Li *et al.*, 2016).

DFT calculations can predict the thermodynamic stability, formation enthalpy and phase diagrams of Half-Heusler alloys under different temperature and pressure conditions. These thermodynamic properties provides insights into the materials' stability range and phase transitions, guiding experimental synthesis effects (Zhang *et al.*, 2019).

DFT-based phonon properties calculations can be determine dispersion relations, phonon densities of states and thermal properties (e.g. specific heat capacity thermal conductivity) of Half-Heusler alloys phonon properties are crucial for understanding the materials' thermal transport behaviour and phonon-mediated thermal conductivity (Togo and Tanaka, 2015).

In addition to their electronic and magnetic properties, Half-Heusler alloys also demonstrate excellent mechanical stability and computability making them suitable various structural applications their robustness and resistance to corrosion further enhance their appeal for engineering application in harsh environments. Overall, the rich and tunable properties of Half-Heusler alloys continue to fuel research interest and exploration in materials science and engineering, with ongoing advancements in synthesis, characterization techniques and computational modeling, these alloys hold great promise for addressing challenges in energy conversion, electronics and beyond, paving the way for innovative technologies with enhanced performance and efficiency. The project is aimed at studying that structural, electronic, mechanical, density of state, and phonon properties of Half-Heusler alloy NaCrSb using density functional theory. The objectives of the research includes.

2.0. Literature Review

Our DFT calculation reveal the crystal structure, electronic band structure, phonon dispersion curves and thermodynamic stability of CoTiSb. Additionally, we analyze its mechanical properties, including elastic constants and shear modulu our findings provide valuable insights into the material's suitability for applications such as thermodynamics, spritronics, and catalysis. Overall, CoTiSb is a fascinating material with a wide range of potential applications. Its properties can be further optimized and tailored through careful material design, synthesis and characterization, paving the way for its use in advanced technologies (Felser *et al.*, 2007).

Half-Heusler alloys, exemplified by the alloy NiMnSb, have garnered significant interest in the scientific community for their potential applications across various technological domains due to their distinct amalgamation of properties. This investigation utilizes density functional theory (DFT) calculations to delve into the intricacies of structural, electronics, mechanical, thermodynamic and phonon attributes of NiMnSb. Employing DFT methodologies, we elucidate the crystalline framework, electronic bandmanifestation, phonon dispersion behaviours and thermodynamic robustness of the alloy. Additionally, mechanical traits such as elastic moduli and shear modulus are scrutinized, offering insights into the alloy's mechanical integrity. The outcomes of this study furnish valuable perspectives on the aptness of NiMnSb for diverse applications, encompassing fields such as thermodynamics, spintronics and catalysis (Kandpal *et al.*, 2006).

3.0. Methodology

In this study, we are delving into the structural, electronic, mechanical, thermodynamic and phonon properties of half heusler alloy (NaCrSb) using a computational technique of Density Functional Theory (DFT). This method is widely used in materials science to study how atoms arrange themselves in material and how they interact with each other. Quantum espresso software version qe-6.8 for simulation on ubuntu operating system version 22.04LTS. The Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation (GGA) was used for the exchange-correlation potential. The projector augmented-wave (PAW) method was employed to describe the core electrons.

4.0. Results and Discusion

4.1 Structural Properties

In order to find the ground state geometry, geometry optimization for the purpose of determining structural attributes entails volume optimization, cell shape determination, and atomic position optimization. Making DFT

calculations for every possible values of $a=b$ and c and figuring out which one yields the lowest total energy is one method of figuring out a cell's shape. Using an DFT optimization process within QE is an alternate (and faster) method that looks for the set of lattice parameters, unit cell angles, and internal positions that result in a zero stress tensor (which automatically equates to a minimal total energy). The regular full-Heusler and half-Heusler compounds crystallize in the centrosym-metric and noncentrosymmetric cubic C1b structure, respectively, with the $F\bar{4}3m$ (no. 216) space group in the centrosym-metric cubic L21 structure with the $Fm\bar{3}m$ (no. 225) space group, respectively. (Graf, 2011). The phase is $\beta(4b\ 4a\ 4c)$ phase. Fig. 1 is extracted using Xcrysden tools from the obtimizeds input files. The crystal structure of the β -phase phase of NaCrSb compound in Figure 1 shows structural positions of atoms in their respective phases.

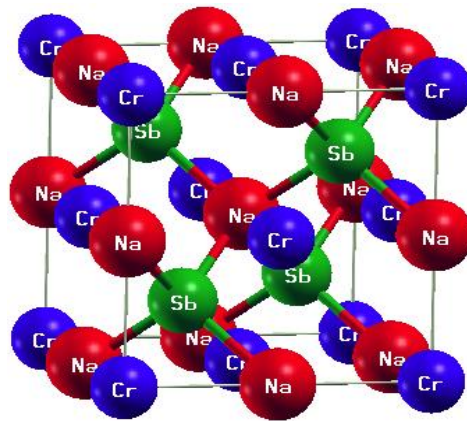


Figure 1: The crystal structure of (a) α -phase (b) β -phase (c) γ -phase of NaCrSb compound

Table. 1: Structural Parameters for NaCrSb for β -phase phases considered

Compounds	Configurations	E(Ry)	a(Å)	B(Gpa)	B'
NaCrSb	β - Phase(4b 4a 4c)	455.75	12.81	37.2	4.58

We performed Series of self-consistent calculations to optimised the structure of NaCrSb. The informational collections produced from the self-consistent energy computations were fitted to the third and fourth-order Birch-Murnaghan condition of state (Murnaghan, 1944) and the optimized Lattice Constant(a_0), Bulk Modulus(B), pressure derivative(B') and minimum energy (E_{min}) were obtained. The bulk modulus estimates how safe a material is to impressibility and its pressure derivative estimates its reaction to slight expansion in pressure.

4.2. Electronic Band Structure

As shown in Figure 2, the optimized latticed constants in high symmetry directions of the first Brillouin zone $L - \Gamma - X - W - k - \Gamma$ have been used to compute the electronic band gap structural properties of the KCrAs alloy.

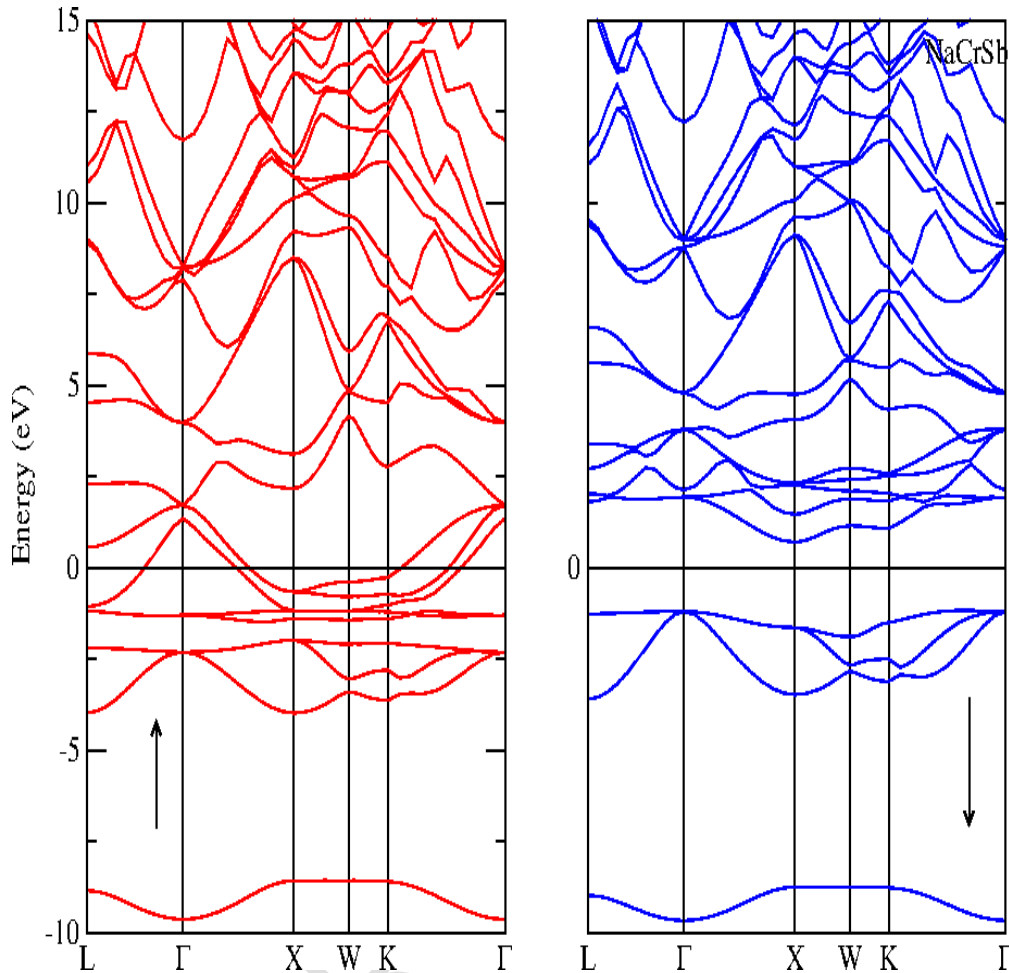


Figure 2: Calculated electronic band structure of NaCrSb

For NaCrSb, a low bandgap semiconductor half-Heusler alloy at spin down, the measured band gap was 1.93eV, with a range of values. The structure NaCrSb, with its valence band maximum (VBM) situated at the Γ -point of the Brillouin zone and its conduction band minimum (CBM) at the X-point, has been identified in Figure 2. This suggests that NaCrSb is a material with an indirect bandgap semiconductor. The two spin bands in this material, NaCrSb, showed entirely different behaviors. At the Fermi level (E_F) line, one of the typically the majority-spin band, also called the spin-up band in red displays characteristic metallic behavior. Meanwhile, the minority band which is blue in hue and spin-down shows semiconductor behavior with a gap at the E_F line. The material NaCrSb demonstrates both semiconductor and metal behavior at different spin up and down

orientations. Therefore, half-metallic heusler alloy is predicted by NaCrSb. These results correspond with those of Hoang et al. (2021).

4.3. Mechanical Properties

Mechanical Stability Criteria (Born Criteria for cubic crystals)

$$C_{11} > 0, C_{44} > 0, C_{11} - C_{12} > 0, C_{11} + 2C_{12} > 0 \quad (4.1)$$

(Félix, 2014); where C_{11} , C_{12} , C_{44} are elastic constant

Anisotropy factor (A)

$$A = \frac{2C_{44}}{C_{11} - C_{12}} \quad (4.2)$$

The term anisotropy refers to the fact that the properties of a magnetic material are dependent on the directions in which they are measured. Anisotropy makes an important contribution to hysteresis in magnetic materials and is therefore of considerable practical importance. The anisotropy has a number of possible origins.

Cauchy's pressure (C^p)

Cauchy pressure determined as the difference between two elastic constants. This parameter gives an idea of the type of chemical bond between atoms and, also determines the plasticity of metals and alloys.

$$(4.3)$$

Vick's Hardness (H_v): Vickers hardness, a measure of the hardness of a material, calculated from the size of an impression produced under load by a pyramid-shaped diamond indenter

$$H_v = 0.92 \left(\frac{B}{G}\right)^{1.3137} * G^{0.708} \quad (4.4)$$

Equations Source: (Osafire and Umukoro, 2020).

Table 2: Calculated Elastic Constants (C_{11} , C_{12} and C_{44}) Bulk modulus(B), shear modulus (G), B/G Ratio, Cauthy's pressure (C^p), young modulus (E), Poisson ratio(u), Zener Anisotropy factor(A) and Vick's Hardness (H_v) of Half-Heusler Alloy NaCrSb

Compou nds	C_{11} (Gpa)	C_{12} (Gpa)	C_{44} (Gpa)	B (Gpa)	G (Gpa)	B/G (Gpa)	C^p (Gpa)	E (Gpa)	u	A	H_v
NaCrSb	60.41	31.18	17.27	40.92	16.2	2.53	13.91	42.95	0.32	1.18	22.37

The Elastic Constants (C_{11} , C_{12} , and C_{44}), Bulk modulus (B), shear modulus (G), B/G ratio, Cauthy's pressure (C_p), young modulus (E), Poisson ratio (u), Zener Anisotropy factor (A), and Vick's Hardness (H_v) of the Half-Heusler Alloy NaCrSb were calculated using equations (4.1) through (4.4) based on the results shown in Table 2. The potential bonding of the atoms in the compound is suggested by the Poisson ratio and the Cauchy pressure. In their research, Frantsevich et al. (1982) reported that the Poisson ratio's crucial value was 0.26. We obtained 0.32 as the Poisson ratio for NaCrSb. A sizeable negative \square supports directional covalent bonding, while a positive value suggests non directional metallic bonding. Results of C_p for the compound

NaCrSb is positive and substantial, supporting a non directional metallic bonding among the atoms. In isotropic materials, the properties of the material are independent of the direction, while the material properties are direction-dependent in anisotropic materials. When a material is measured from different directions, any deviation from unity automatically renders the material anisotropic. The values of the anisotropy/isotropy test for the material is 0.29. The result shows NaCrSb is anisotropic. Pugh (2009) determined that the reference value between brittleness and ductility in a material is 1.75 at the critical value from the ratio of bulk modulus to shear modulus (B/G) of a material. The material is brittle or ductile when the B/G value is below or above the reference value. In fabrication processes, a material's brittleness or ductility may have an impact on the manner of failure. With a B/G ratio value of 2.53, Table 2's results demonstrate the ductile nature of the NaCrSb material. The material's resistance to indentation is addressed holistically by the Vicker's hardness. It describes how a material's ductility can influence the mechanism of failure throughout the fabrication process. The ductility of the NaCrSb material is supported by Table 2's data.

4.4. Density of State

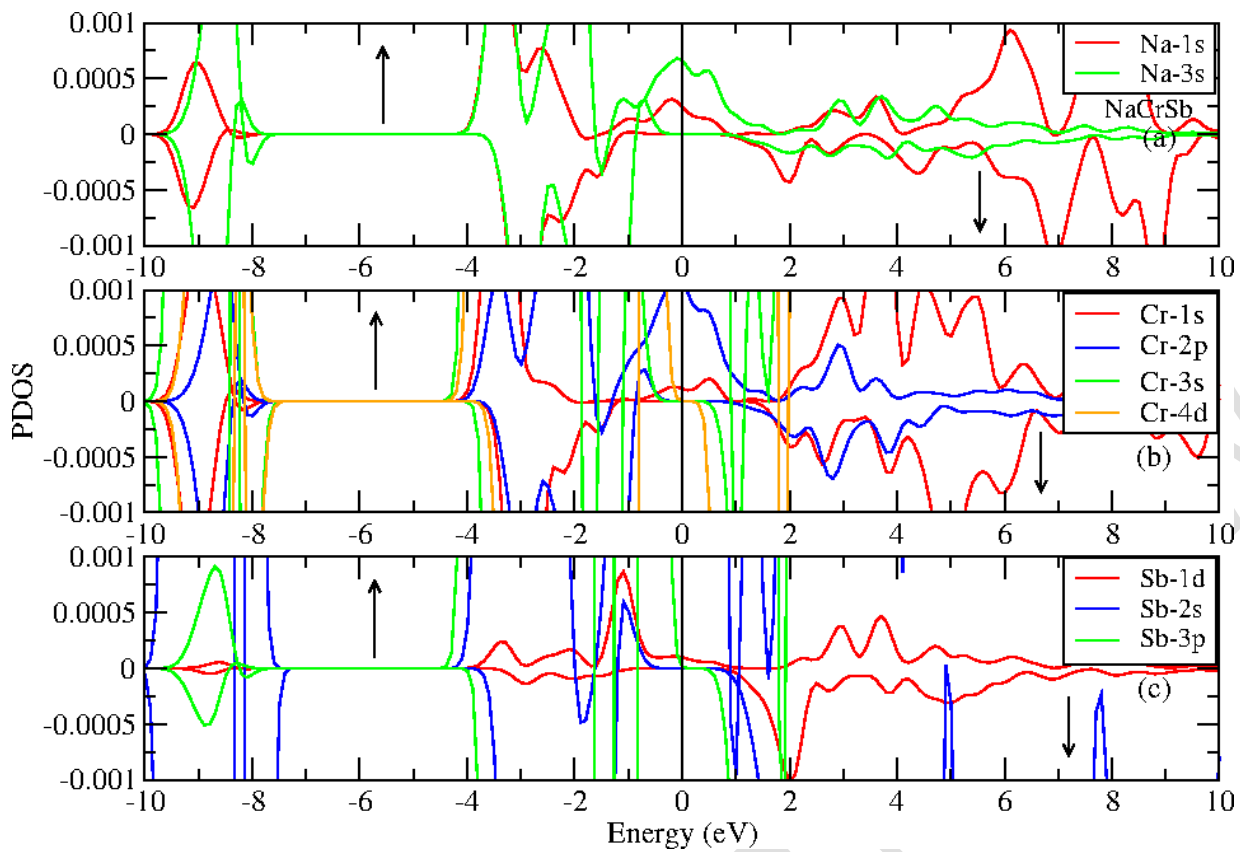


Fig. 3. Plot of PDOS against energy for NaCrSb. Atom projected DOS calculated for the

(a). Na -1s, Na- 3s, (b). Cr-1s, Cr-2p, Cr-3s and Cr- 4d and (c). Sb-1s, Sb- 2s, and Sb - 3p.

Fig. 3(a) shows that Na-1s and Na-3s has the high orbital contribution for the Na-atoms. While in Fig. 3(b) and (c) Cr-1s, Cr-2p, Cr-3s and Sb-1s, Sb- 2s, and Sb - 3p has high orbital present for Cr-atoms as well. At fermi energy both the spin up and spin down is at zero point in plot of partial density of state(PDOS) against energy. It became clear from this that NaCrGe is a half-metallic Heusler alloy.

4.5. Phonon properties

The phonon spectra were calculated to determine the vibrational characteristics of the NaCrSb molecular structure. Thermo_pw is a code that computes the physical properties of materials using Quantum ESPRESSO

routines as the underlying engine.

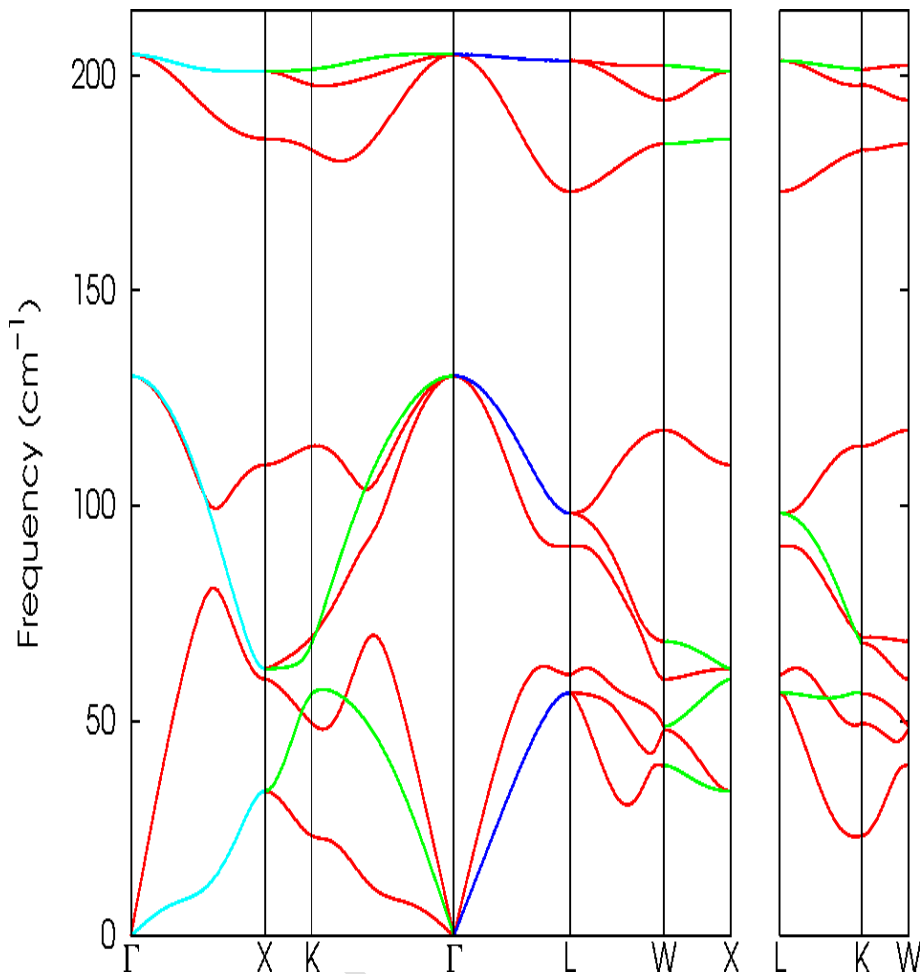


Figure. 4. Calculated phonon frequency versus wave vector coordinate for NaCrSb

Fig. 4 shows the phonon dispersion curves along the Γ - X - K - Γ - L - W - X high symmetry directions. The compound NaCrSb revealed positive frequencies, which indicates NaCrSb is dynamically stable.

5.0. Conclusion

The research provides valuable insights into the structural, electronic, mechanical, density of state and phonon properties of half-Heusler alloy (NaCrSb) using density functional theory. The lowest ground state energy was found in the β -phase, suggesting that the material NaCrSb is structurally stable at this phase. The materials are semiconductor half-Heusler alloys with small bandgaps, and the measured band gap of 1.93eV was obtained for NaCrSb, with a range of values. This indicates that NaCrSb is an indirect bandgap semiconductor material. The substance NaCrSb exhibits behavior during spin up and down that is characteristic of both metals and semiconductors, which foretells the half-metallic Heusler alloy. The B/G ratio of 2.53 indicates that the NaCrSb material is ductile. The material's resistance to impact is addressed holistically by the Vicker's hardness. It

discusses how a material's ductility can influence the mechanism of fracture throughout the fabrication process. Positive frequencies were detected in the phonon dispersion curves along the $\Gamma - \Gamma - K - \Gamma - L - W - \Gamma$ high symmetry directions. This suggests that NaCrSb is dynamically stable. The search for new materials with special qualities is what propels progress in materials research and technology. We suggests that NaCrSb is a promising sort of material with practical applications in spintronics.

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