

INTER-CONNECTION BETWEEN REFRACTIVITY GRADIENT VARIATIONS AND INTERTROPICAL DISCONTINUITY OVER NIGERIA

Abstract

Radio signal transmission is significantly impacted by the troposphere's complexity. As a result, refractivity gradients has been a crucial parameter for path clearance estimation and propagation effects including ducting, super-refraction, and sub-refraction. Through empirical formulations, this study focuses on the correlations that exist between Intertropical Discontinuity (ITD) and Refractivity Gradient. One important factor influencing West African weather patterns is the ITD. Utilising hourly temperature and relative humidity data for the years 2017 and 2018 at two levels (surface and 1000 hpa) gathered from the archives of the European Centre for Medium-Range Forecasts (ECMWF) for twenty meteorological stations in Nigeria, the refractivity gradient values were computed. Using ANOVA method, five regression models (Linear, Cubic, Quadratic, Power and Log) were developed between refractivity gradient and ITD. The linear model ($L = B_0 + B_1RG$) have been found to be mostly significant with coefficient of determination ranging between 97% and 99%) across all the regions.

Keywords: Radio signal transmission, meteorological stations, refractivity gradient, radiation

Introduction

The temperature and humidity variations in Nigeria cause the intertropical discontinuity, which considerably aids in the formation of the refractivity gradient. Using radiosonde recordings, (Dairo et al. 2018) conducted study on the refractivity gradient along the Intertropical discontinuity. The large temperature and moisture content variations among the various trade wind systems lead the area to suffer a refractivity gradient, which is mostly governed by the intertropical discontinuity zone.

Horizontal layers with highly variable refractivity greatly show the large-scale variations in the refractive index of the atmosphere. Multipath effects are produced when there are significant variations in the refractive index due to large-scale variations in the atmospheric radio refraction index (Emmanuel et al. 2020). The condition is especially true if the same signal reaches its objective and then battles with another signal along the way, reaching a lapse in the troposphere

that attends it. The large-scale difference in refractive index provides an explanation; radiation passing through the atmosphere gently bends as it moves across the earth Arowolo and Oluleye (2022). Thus, the altitude dependence of the refractivity determines the radio wave's reach. Consequently, the path's curve will be influenced by the atmosphere's refractivity (Tanko et al., 2019).

Radar systems that are active in the tropics are likewise impacted by the intertropical discontinuity's effect on the refractivity gradient. (López et al., 2018) conducted research to investigate the influence that the ITD has on the performance of weather radar. They discovered that the fluctuations in the refractivity gradient that occur over the ITD might cause errors to be introduced into radar data, which in turn affects how accurately rainfall estimation and storm tracking are performed.

Methodology

Site Description

The study was carried out on 19 locations in Nigeria, namely: Sokoto, Kastina, Kano, Maiduguri, Ibadan, Ado-Ekiti, Ogbomosho, Ilorin, Osogbo, Lagos, Yenagoa, Benin, Port Harcourt, Warri, Minna, Jos, Abeokuta, Bida and Abuja; whose geographical coordinate are presented. The terrain is divided into four distinct regions: the Coastal, Derived Savannah, Guinea and Sub-Saharan Region. Regarding the many kinds of tropical climates, the position of the Intertropical Discontinuity is the factor that has the most significant influence on the climate. The ITD is a low-pressure region that denotes the place where the trade winds converge. The position of the ITD shifts during the course of the year, and although it stays relatively close to the equator, the ITD over land tends to move to latitudes that are farther north or south than the ITD over sea. This is because of the wider range in temperature throughout the area (Pospichal et al., 2010). Depending on the distribution of land and water, the position of the ITD can shift by as much as 40 to 45 degrees of latitude to the north or south of the equator. In spite of these differences, the ITD correlates rather strongly with the height of the sun and indicates the time of day when the sun is at its highest position in the sky.

Table .1 Geographic Coordinate of the Study Locations

STUDY LOCATION	LATITUDE (°N)	LONGITUDE (°E)	VEGETATION
Sokoto	13.07	5.23	Short Grass Savannah
Katsina	12.98	7.62	Short Grass Savannah
Kano	12	8.59	Short Grass Savannah
Maiduguri	11.83	13.15	Short Grass Savannah
Ibadan	7.38	3.95	Rain Forest
Ado-Ekiti	7.61	5.24	Rainforest
Ogbomosho	8.12	4.24	Woodland and Tall grass Savannah
Ilorin	8.47	4.54	Woodland and Tall grass Savannah
Osogbo	7.78	4.54	Woodland and Tall grass Savannah
Lagos	6.52	3.37	Fresh Water Swamp
Yenagoa	4.92	6.67	Fresh Water Swamp

Benin	6.33	5.6	Rainforest
Port Harcourt	4.82	7.05	Fresh Water Swamp
Warri	5.55	5.79	Rainforest
Minna	9.58	6.54	Rainforest
Jos	9.9	8.86	Woodland and Tall grass Savannah
Abeokuta	7.15	3.36	Rainforest
Bida	9.08	6.01	Woodland and Tall grass Savannah
Abuja	9.07	7.48	Woodland and Tall grass Savannah

Data

Refractivity and Refractivity Gradient

The radio refractivity, denoted as (N) is mathematically represented as;

$$N = 77.6 \frac{P}{T} + 3.73 \times 10^5 \frac{e}{T^2} \quad (\text{N-units}) \quad (1.1)$$

Equation (1.1) above is divided into two parts

$$N = N_{DRY} + N_{WET} \quad (1.2)$$

where,

$$N_{DRY} = 77.6 \frac{P}{T}$$

$$N_{WET} = 3.73 \times 10^5 \frac{e}{T^2}$$

where,

- P= atmospheric pressure (hpa),
- e = water vapour pressure (hpa),
- T= absolute temperature (K)

The differential equation that describes the relationship between the water vapour pressure, e (hPa), the saturation vapour pressure, es (hPa), and the relative humidity, H (%), may be derived from equation (1.2) as follows:

$$e = \frac{H}{100} es \quad (1.3)$$

where,

$$es = a \exp \left[\frac{bt}{t+c} \right] \quad (1.4)$$

The values of the coefficients in equation (1.4) are obtained as $a = 6.1121$, $b = 17.502$, $c = 240.97$. The atmospheric temperature, denoted as T, is measured in Kelvin (K), whereas the dry atmospheric pressure, represented by P in (hPa). Additionally, the temperature, denoted as t in (°C).

Hence, the Refractivity Gradient in N-units per km may be represented as:

$$G = \frac{dN}{dh} = \frac{N_{1km} - N_s}{\Delta h} \quad (1.5)$$

Where N_{1km} is the refractivity at 1 km height is, N_s is the refractivity at the surface, Δh is change in height.

The connection between the Latitudinal (L) location of the Intertropical discontinuity (ITD), which is the independent variable, and the Refractivity Gradient (RG), which is the dependent variable, was investigated using five regression models in this work.

3.4 REGRESSION LINE. EQUATIONS ADOPTED

a. LINEAR: $L = B_0 + B_1RG$ (1.6)

where B_0 is the intercept and B_1 is the slope

b. QUADRATIC: $L = RG^2 + RG + B_0$ (1.7)

c. CUBIC: $L = -RG^3 - RG^2 - RG - B_0$ (1.8)

d. LOG: $\ln RG = -B_0 + B_1 \ln L$ (1.9)

e. POWER: $RG = -B_0 + B_1 \ln L$ (2.0)

RESULTS

In order to establish the relationship between Refractivity gradient and Intertropical Discontinuity, a linear and multiple regression model were conducted, with ITD parameters such as; mean daily values of Latitudes, longitudes and dewpoint temperatures were modelled against mean daily values of Refractivity Gradient, however, it was discovered that only the latitudinal positions of the Intertropical Discontinuity were suitable for these models while other parameters like dewpoint temperatures, longitudinal positions were insignificant for

both linear and multiple regressions adopted in this work as calculated in the tables shown below across the various regions in Nigeria;

L (latitudinal position of ITD) is the independent variable or predictor in these models while Refractivity Gradient is the dependent variable. The models performed better in the Derived and Guinea savannah regions with about 98% coefficient of determination followed by Sub-sahelian and Coastal regions with 97% coefficient of determination. All of the predictors explain a large amount of the variance between the variables. $R^2 = 0.984-0.973$ across all stations; it shows that the variability of L is explained by 97-98% of the variance of RG, the coefficient of multiple correlation (R) = 0.986 explains the strong correlation between the predicted data and the observed data. Overall, it was discovered that cubic regression model has the highest correlation amongst other models

Table 2. Models for Coastal Region

MODELS	N	B ₀	SEB ₀	B ₁	SEB ₁	B ₂	SEB ₂	B ₃	SEB ₃	R	R ²	F	P-value
LINEAR	365	34.796	6.889	0.252	554e-6	-		-	-	0.972	0.973	12,882	0.0000
QUADRATIC	365	49.310	43.097	0.591	0.012	0.002	2e-7	-	-	0.992	0.984	11,608	1.72e-181
CUBIC	365	-20.915	-76.925	-1.897	-0.245	-0.027	3.78e-5	-109e-4	6.182e-10	0.996	0.992	15,857	3.24e-8
LOG	365	-5.824	-0.069	0.549	2.6e-4	-	-	-	-	0.986	0.972	12,837	0.0000
POWER	365	-206.193	-170.315	47.611	15.664	-	-	-	-	0.991	0.983	20,856	0.0000

Table 3 Models for Derived Region

MODELS	N	B ₀	SEB ₀	B ₁	SEB ₁	B ₂	SEB ₂	B ₃	SEB ₃	R	R ²	F	P-value
LINEAR	365	46.430	11.286	0.6027	259e-5	-		-	-	0.992	0.982	19,582	0.0000
QUADRATIC	365	64.760	130.038	1.269	0.093	0.006	3.9e-6	-	-	0.994	0.985	12,080	3.13e-18
CUBIC	365	-175.029	-2457	-11.833	-9.040	-0.231	0.003	-0.0014	1.12e-7	0.997	0.992	14,699	7.13e-33
LOG	365	-4.9135	-0.039	0.3599	115e-5	-	-	-	-	0.915	0.972	12,686	0.0000
POWER	365	-105.739	-37.537	19.995	2.839	-	-	-	-	0.994	0.982	19,935	0.0000

Table 4 Models for Guinea Savannah

REGRESSION MODELS	N	B ₀	SEB ₀	B ₁	SEB ₁	B ₂	SEB ₂	B ₃	SEB ₃	R	R ²	F	P-value
LINEAR	365	15.130	0.4796	0.1099	813e-7	-	-	-	-	0.992	0.984	22,009	0.0000
QUADRATIC	365	14.909	0.443	0.1218	125e-6	268e-6	505e-11			0.994	0.989	17,188	1.09e-30
CUBIC	365	15.177	0.4356	0.1289	116e-6	-18e-5	-579.6e-12	-7.10E-6	-3.24e-12	0.997	0.994	19,190	5.1e-8
LOG	365	-22.558	-11.103	8.497	1.665	-	-	-	-	0.915	0.838	1,872	0.0000
POWER	365	-296.249	-463.630	110.129	68.776	-	-	-	-	0.994	0.989	31,100	0.0000

Table 5 Models for Sahel Region

MODELS	N	B ₀	SEB ₀	B ₁	SEB ₁	B ₂	SEB ₂	B ₃	SEB ₃	R	R ²	F	P-value
LINEAR	365	11.944	0.334	0.0491	1.62e-5	-	-	-	-	0.991	0.983	20,865	0.0000
QUADRATIC	365	11.642	0.403	0.048	1.49e-5	4.758E-5	188.6e-12	-	-	0.994	0.988	14,619	0
CUBIC	365	11.490	0.299	0.055	27e-6	8.601E-5	306.8e-12	-7.19e-7	-284.87e-16	0.998	0.994	18,695	2.96e-65
LOG	365	-29.397	-11.406	12.003	1.858	-	-	-	-	0.971	0.943	6,013	0.0000
POWER	365	-596.790	-2381.79	245.932	391.523	-	-	-	-	0.993	0.985	23,853	0.0000

VALIDATION OF MODEL (ACTUAL VS PREDICTED VALUES OF REFRACTIVITY GRADIENTS)

COASTAL REGION

The values of the actual refractivity gradients against predicted refractivity gradients are plotted below fig 1 below. Also, the differences in the values obtained becomes smaller as we move down the year from January to December. In this region, $R^2 = 0.9862$ signifies its ability to find the probability of future events occurring within the given predicted results outcomes. If more samples are added to the model, the coefficient will show the likelihood or the probability of a new point or the new dataset falling on the line.

The correlation coefficient in this region is 0.9862, the correlation is positive. It shows there is a strong linear relationship between Actual RG and Predicted RG. As Actual RG increases, Predicted RG also appears to increase. While R^2 suggests that 97% of changes Actual RG to changes in Predicted RG, 3% are unexplained which justifies that this model can be used to forecast future values of Refractivity gradients provided that the latitudinal position of ITD is known for stations in the coastal region.

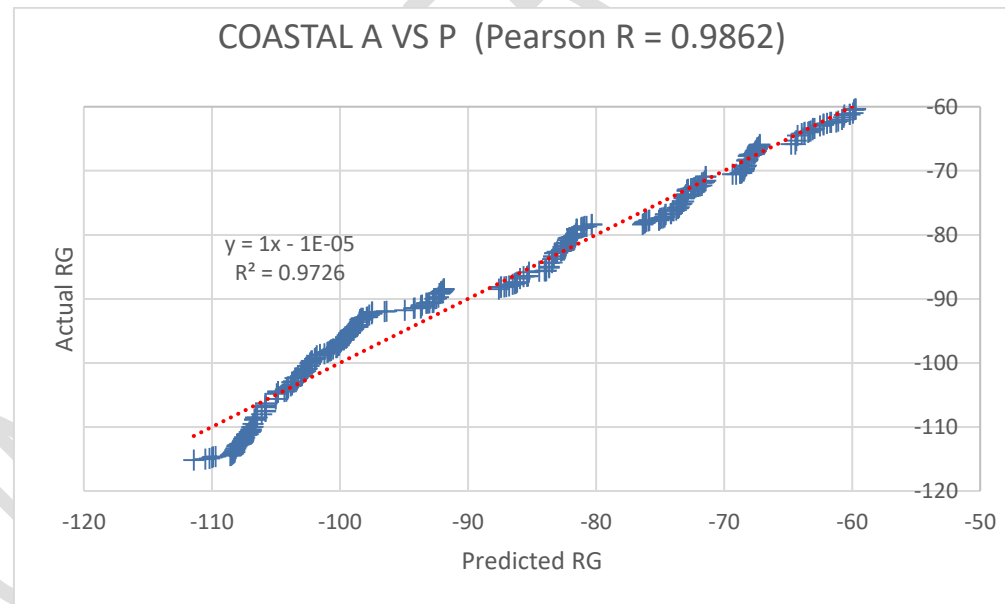


figure 1 ACTUAL VS PREDICTED VALUES OF REFRACTIVITY GRADIENTS (COASTAL

REGION)

DERIVED REGION

The values of the actual refractivity gradients against predicted refractivity gradients are plotted below as shown in fig 2 below. Also, the differences in the values obtained becomes smaller as we move down the year from January to December in this region. $R^2 = 0.9918$ signifies its ability to find the probability of future events occurring within the given predicted results outcomes. If more samples are added to the model, the coefficient will show the likelihood or the probability of a new point or the new dataset falling on the line.

The correlation coefficient in this region is 0.9902, the correlation is positive. It shows there is a strong linear relationship between Actual RG and Predicted RG. As Actual RG increases, Predicted RG also increases. While R^2 suggests that 98% of changes Actual RG to changes in Predicted RG, 2% are unexplained which justifies that this model can be used to forecast future values of Refractivity gradients provided that the latitudinal position of ITD is known for stations in the derived region. This also implies the model is more accurate in the derived region by 1% over the coastal region.

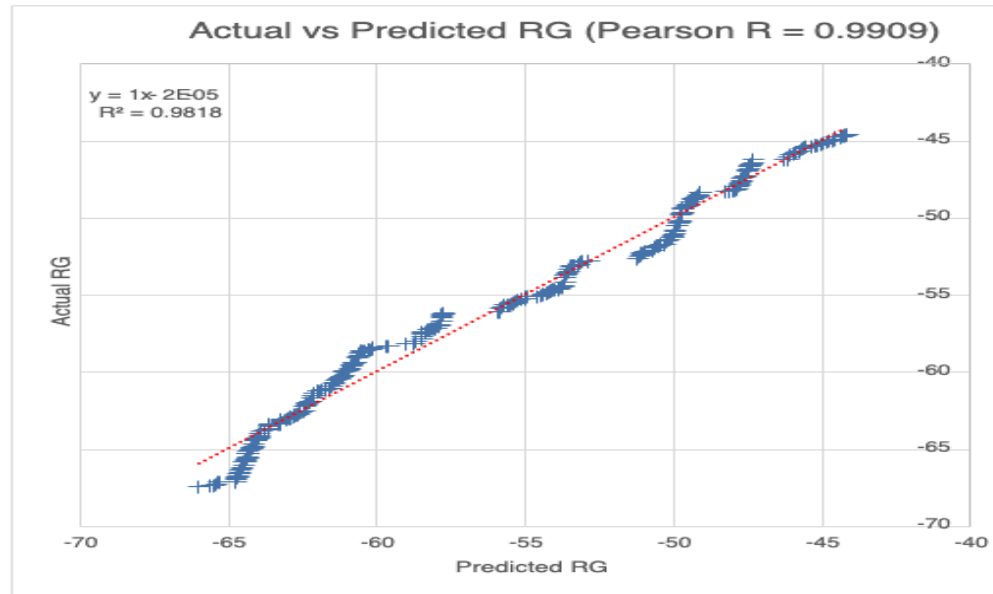


figure 2 ACTUAL VS PREDICTED VALUES OF REFRACTIVITY GRADIENTS

(DERIVED REGION)

Guinea Region

The values of the actual refractivity gradients against predicted refractivity gradients are plotted below and shown. In fig 3 below. The differences in the values obtained becomes smaller as we move down the year from January to December in this region. $R^2 = 0.9804$ signifies its ability to find the probability of future events occurring within the given predicted results outcomes. If more samples are added to the model, the coefficient will show the likelihood or the probability of a new point or the new dataset falling on the line.

The correlation coefficient in this region is 0.9919, the correlation is positive. It shows there is a stronger linear relationship between Actual RG and Predicted RG. As Actual RG increases, Predicted RG also increases. While R^2 suggests that 98% of changes Actual RG to changes in Predicted RG, 2% are unexplained which justifies that this model can be used to forecast future values of Refractivity gradients provided that the latitudinal position of ITD is known for stations in the Guinea Savanna region. This also implies the model is more accurate in the Guinea region over the coastal and derived region.

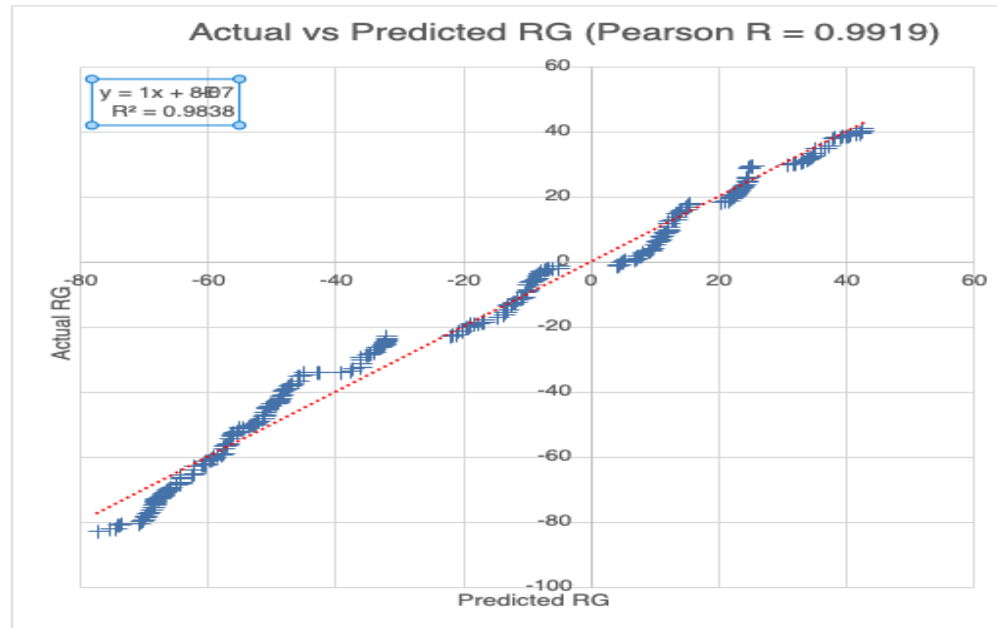


figure 3 ACTUAL VS PREDICTED VALUES OF REFRACTIVITY GRADIENTS (Guinea Region)

Sub-Saharan Region

The values of the actual refractivity gradients against predicted refractivity gradients are plotted below as shown in fig 4 below. The differences in the values obtained becomes smaller as we move down the year from January to December in this region. $R^2 = 0.9828$ signifies its ability to find the probability of future events occurring within the given predicted results outcomes. If more samples are added to the model, the coefficient will show the likelihood or the probability of a new point or the new dataset falling on the line.

The correlation coefficient in this region is 0.9919, the correlation is positive. It shows there is a stronger linear relationship between Actual RG and Predicted RG. As Actual RG increases, Predicted RG also increases. While R^2 suggests that 98% of changes Actual RG to changes in Predicted RG, 2% are unexplained which justifies that this model can be used to forecast future values of Refractivity gradients provided that the latitudinal position of ITD is known for stations in the Guinea Savanna region. This also implies the model is more accurate in the Sahel region over the coastal and derived region.

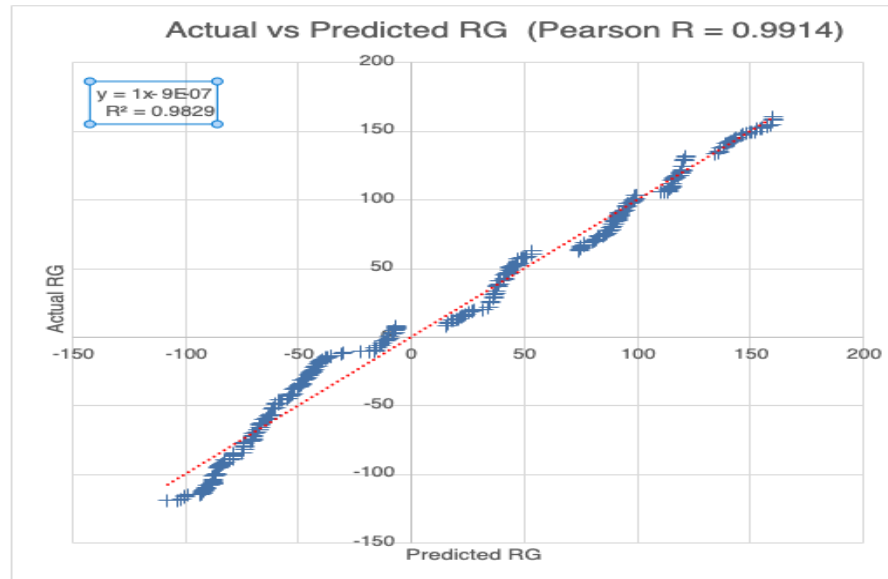


figure 4 ACTUAL VS PREDICTED VALUES OF REFRACTIVITY GRADIENTS (Sub-Saharan Region)

CONCLUSION AND RECOMMENDATION

5.1 Conclusion

This work has demonstrated the relationship between refractivity gradients and intertropical discontinuity. Relative to other stations, the coastal stations have lower refractivity values due to their proximity to the ocean. Variations in refractivity gradients are found to be large during dry seasons and very low during wet seasons across all stations. Rainfall distribution at all stations has been found to be influenced by the migration of the intertropical discontinuity (ITD) across all sites. The refractivity gradient value decreases throughout the stations as the ITD's latitudinal position rises.

Across the four geographical regions of Nigeria, the regression model constructed for this study demonstrated a positive correlation between the values of the refractivity gradient and the latitudinal position of the Intertropical discontinuity. With almost 98% accuracy, the regression models fared better in the Guinea and Sub-Saharan regions. Overall, cubic regression model performs best across all regions of study. In addition to

helping radio engineers prepare for anomalous propagations in communication fields, this would also aid in the estimation of refractivity gradients for sites with climates comparable to the regions this work is studying.

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