

Original Research Article

Application of Multilayer Perceptron with Residual Learning for Medium-term Forecasting of U.S. Fossil Energy Consumption

Abstract

Accurate midterm forecasts of fossil fuel consumption are essential for effective energy planning, economic management, and resource allocation. While machine learning models have demonstrated their efficacy in handling large-scale nonlinear datasets, many, including Multilayer Perceptrons (MLPs), suffer from performance degradation with increased depth. Fortunately, recent studies have revealed that Residual Networks (ResNets) can mitigate or even overcome this challenge. In this paper, we propose a Weighted Residual Network based on MLP to enhance predictive performance. We employ the Adam algorithm for model training and utilize the Gridsearch algorithm for hyperparameter tuning. In the application section, we develop predictive models using three case studies: natural gas, petroleum, and total fossil fuel consumption. We validate the effectiveness of our proposed model and compare it with ten other machine learning models. Our findings demonstrate that our proposed model consistently outperforms others in all three cases, underscoring its superior performance in midterm forecasting of fossil fuel consumption.

Keywords: Weighted Residual Network, Multilayer Perceptron, Adaptive Moment Estimation, Grid Search, fossil energy consumption

1 Introduction

Accurate mid-term forecasts of fossil energy consumption are crucial for energy planning, economic management, and resource allocation. Numerous studies have shown the effectiveness of machine learning models in handling large-scale nonlinear datasets, such as k CNN-LSTM [1], SSA-PLSTM [2], CNN-GRU [3].

Multilayer Perceptron (MLP) is a fundamental neural network architecture in machine learning models. Frank Rosenblatt introduced the concept of a layered perceptron network in his seminal work "Perceptron" [4] [5] [6]. His perceptrons comprised an input layer, a hidden layer with static weights, and an output layer with trainable connections. However, this model was initially perceived as an extreme learning machine rather than

a deep learning network [7]. Despite this classification, Rosenblatt’s work laid the foundation for subsequent advancements in neural network architectures. In 1965, Alexey Grigorevich Ivakhnenko and Valentin Lapa published the pioneering Group Method of Data Handling, representing the first instance of a deep-learning feedforward network. Notably, this method did not incorporate stochastic gradient descent [8] [9]. Two years later, Shun’ichi Amari introduced a deep-learning network capable of classifying non-linearly separable pattern classes, employing stochastic gradient descent for the first time in such networks [10]. Amari’s team also constructed a five-layered feedforward network, underscoring the viability of deep learning architectures. The modern backpropagation method, a pivotal aspect of MLP training, was introduced by Seppo Linnainmaa in 1970 [11]. This application of chain-rule-based supervised learning revolutionized neural network training by facilitating error propagation for parameter updates. Subsequent enhancements to the backpropagation algorithm, such as its formalization by Paul Werbos in 1982 [12], and experimental investigations by David E. Rumelhart et al. in 1985 [13], further underscored its significance in the realm of deep learning. To date, MLP has undergone significant development and finds widespread application in energy consumption prediction [17] [18] [19].

The depth of the MLP model is constrained by the vanishing gradient problem, posing challenges in training deeper networks. In addressing this issue, Sepp Hochreiter introduced skip connections, also known as residual connections, within the long short-term memory (LSTM) recurrent neural network architecture in 1991 [14]. These connections allow gradients to flow more effectively through the network, mitigating the vanishing gradient problem. Subsequently, in 2015, the concept of Highway Networks emerged as a further refinement. Inspired by the forget gates utilized in LSTM networks, Highway Networks integrate similar mechanisms into feedforward neural networks [15]. By enabling information to propagate more freely through the network, Highway Networks alleviate the challenges associated with vanishing gradients. Building upon the principles of Highway Networks, ResNet (Residual Network) simplifies the architecture by eliminating forget gates and directly employing simple skip connections [16]. This approach enables signals to bypass certain layers without the need for gating mechanisms, facilitating the training of exceedingly deep neural networks. The effectiveness of this structure has been empirically demonstrated across various domains. In recent years, numerous machine learning models based on the ResNet architecture have been extensively introduced, including ResNet-LSTM [20], ResNet-ARIMA [21], and ResNet-LightGBM [22]. However, there remains a paucity of ResNet-based models tailored specifically for studying energy consumption time series forecasting, particularly within the domain of U.S. fossil energy consumption, with virtually no examples to date.

In this study, we propose a novel approach termed Weighted ResNet with MLP, with the objective of enhancing feature extraction from time series data and improving forecast accuracy.

The subsequent sections of the paper will delineate the data collection process in Section 2, expound upon the theory and solution methodology of WResNet-MLP in

Section 3, explore its application across three cases involving natural gas, petroleum, and total fossil fuel consumption in Section 4, and conclude with a summary in Section 5.

2 Data Collection

Utilizing consumption data of natural gas, petroleum, and total fossil fuels in the United States as the contextual foundation for constructing and analyzing time series forecasting models holds paramount importance. Firstly, energy consumption stands as a pivotal metric within a nation's economic and societal framework, with accurate forecasting serving as a cornerstone for governmental departments in formulating energy policies. Secondly, constructing and analyzing time series forecasting models facilitates the elucidation of inherent trends and cyclical variations within energy consumption, thereby fostering a deeper comprehension of the interplay between energy utilization and economic development. Furthermore, the application of forecasting models aids in assessing factors such as energy supply-demand equilibrium, resource efficiency, and environmental conservation, thus furnishing a scientific basis for sustainable energy development and environmental protection initiatives. Lastly, by applying advanced time series forecasting methodologies to actual energy consumption datasets, there exists the potential to propel the advancement and application of time series forecasting techniques, thereby fostering progress in related academic research endeavors. Consequently, employing the consumption metrics of natural gas, petroleum, and total fossil fuels in the United States as a backdrop for time series forecasting model construction and analysis bears profound significance in the realms of energy management, environmental conservation, and sustainable development.

The data collection originates from the U.S. Energy Information Administration (EIA), encompassing monthly records spanning from January 1973 to December 2023. These data are visually depicted in Figure 1.

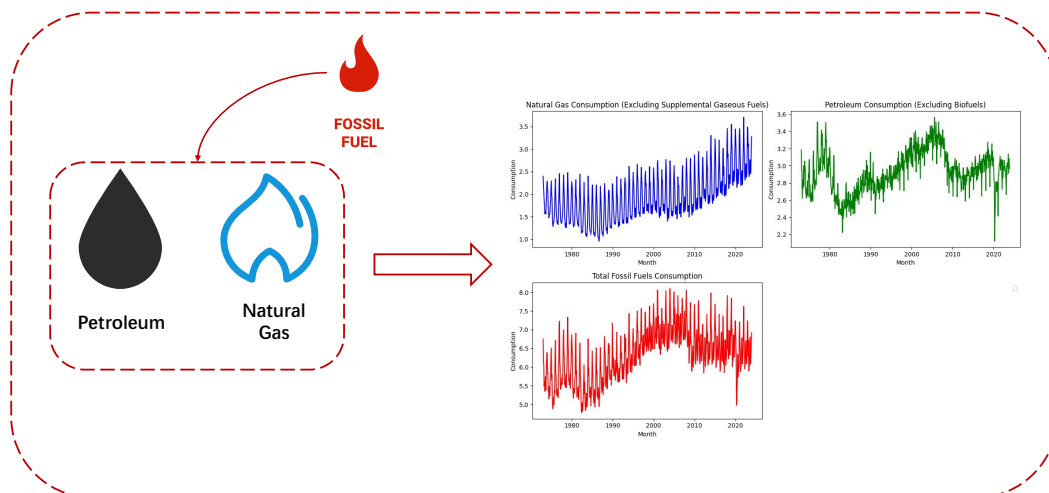


Fig. 1. Natural Gas, Petroleum, Total Fossil Fuels Consumption

3 Research Methodology

3.1 The proposed model and its mathematical principles

At the heart of ResNet lies the skip connection, a structural feature that facilitates the transfer of information from earlier layers directly to subsequent layers. This mechanism enables the network to effectively capture key characteristics within the data, enhancing its ability to learn and generalize.

The Weighted ResNet with MLP (WResNet-MLP) model proposed in this study comprises a ResNet input layer and an output layer. Positioned between these layers are multiple blocks consisting of MLP units, the quantity of which is determined by the chosen depth, denoted as d , of the ResNet architecture. The schematic representation of the WResNet-MLP structure, with an input denoted as \mathbf{Z} , is depicted in Figure 2.

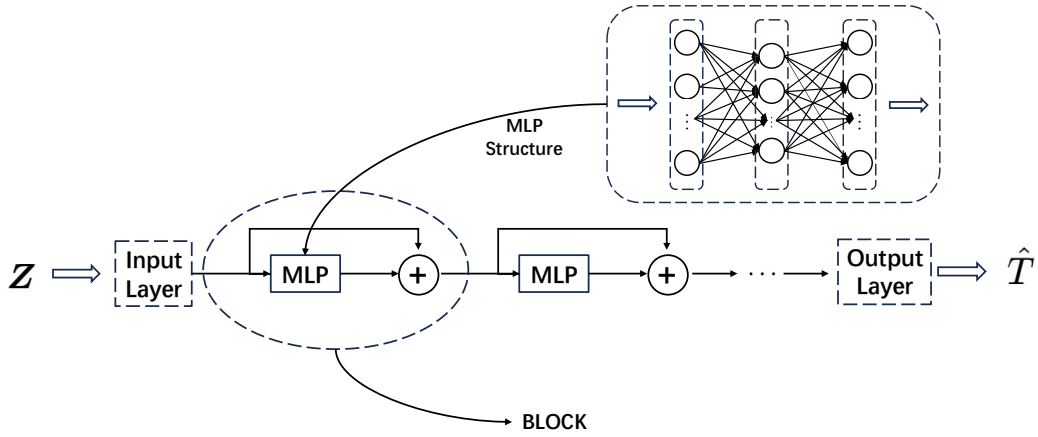


Fig. 2. The structure of WResNet-MLP with the input \mathbf{Z}

Let (\mathbf{Z}, \mathbf{T}) denote the input of the model, comprising n instances (\mathbf{Z}_i, T_i) for $(i = 1, 2, \dots, n)$. The output value \mathbf{s}_0 of the input layer is computed as follows:

$$\mathbf{s}_0 = \mathbf{W}^{(1)}\mathbf{Z} + \beta^{(1)}, \quad (1)$$

Subsequently, the output of the first block is determined as:

$$\begin{cases} \mathbf{s}_1 = \mathbf{W}^{(3)}\delta(\mathbf{W}^{(2)}\mathbf{s}_0 + \beta^{(2)}) + \beta^{(3)}, \\ \mathbf{s}_2 = \mathbf{s}_0 + \mathbf{W}_1^{(4)}\mathbf{s}_1, \end{cases} \quad (2)$$

where \mathbf{s}_1 represents the output of the MLP, and \mathbf{s}_2 denotes the output of the first block. The symbol $\delta(\cdot)$ represents the activation function, with various options available. In this paper, we adopt the sigmoid function as $\delta(\cdot)$ due to its favorable mathematical characteristics, defined as:

$$\sigma(\cdot) = \frac{1}{1 + e^{-\cdot}} \quad (3)$$

Likewise, the output of the second block is obtained as follows:

$$\begin{cases} \mathbf{s}_3 = \mathbf{W}^{(3)}\delta(\mathbf{W}^{(2)}\mathbf{s}_2 + \beta^{(2)}) + \beta^{(3)}, \\ \mathbf{s}_4 = \mathbf{s}_2 + \mathbf{W}_2^{(4)}\mathbf{s}_3, \end{cases} \quad (4)$$

Following the d layers of blocks, the output is represented as:

$$\mathbf{s}_{2d} = \mathbf{s}_{2d-2} + W_d^{(4)} \mathbf{s}_{2d-1}, \quad (5)$$

Consequently, the output of the WResNet-MLP model is expressed as:

$$\hat{T} = \mathbf{W}^{(5)} \mathbf{h}_{2d} + \boldsymbol{\beta}^{(5)}. \quad (6)$$

In the preceding equation, $\mathbf{W}^{(k)}$ (for $k = 1, 2, 3, 4, 5$) and $\boldsymbol{\beta}^{(k)}$ (for $k = 1, 2, 3, 5$) denote the parameters of the WResNet-MLP model.

3.2 Optimizing Model Training

Neural networks, including the WResNet-MLP model in this study, typically lack analytical solutions. Hence, optimization algorithms like Gradient Descent [23], Stochastic Gradient Descent [24], and Adam [25] are utilized. Here, we employ the Adam algorithm for its efficiency, robustness, and adaptability.

Firstly, we define the training error e_i at each point (Z_i, T_i) as follows:

$$e_i = T_i - \mathbf{W}^{(5)} \mathbf{h}_{2d} + \boldsymbol{\beta}^{(5)}, \quad (7)$$

This yields the sum of training errors:

$$E(\mathbf{W}, \boldsymbol{\beta}) = \frac{1}{n} \sum_{i=1}^n e_i^2 = e^T e, \quad (8)$$

where \mathbf{W} comprises $W^{(k)}$ and $\boldsymbol{\beta}$ comprises $\boldsymbol{\beta}^{(k)}$. These parameters \mathbf{W} and $\boldsymbol{\beta}$ are to be solved using the Adam algorithm.

Next, to complete the Adam optimization process, we must compute the gradient of $E(\mathbf{W}, \boldsymbol{\beta})$:

$$\nabla E = \left[\frac{\partial E}{\partial \mathbf{W}}, \frac{\partial E}{\partial \boldsymbol{\beta}} \right], \quad (9)$$

where ∇E represents the gradient.

Unlike traditional gradient descent methods, Adam introduces the notion of modified bias-corrected first moment estimate \hat{m}_i and bias-corrected second moment estimate \hat{v}_i to accelerate convergence. Before computing these, we require the values of the first-order moment estimate m_i and second-order moment estimate v_i , which are expressed as follows:

$$m_i = \mu_1 \cdot m_{i-1} + (1 - \mu_1) \cdot \nabla E, \quad (10)$$

$$v_i = \mu_2 \cdot v_{i-1} + (1 - \mu_2) \cdot \nabla E^2, \quad (11)$$

where μ_1 and μ_2 denote decay rates controlling the speed of decay for the first and second moments of the gradients, respectively.

Then, the \hat{m}_i and \hat{v}_i could be obtained:

$$\hat{m}_i = \frac{m_i}{1 - \mu_1^i}, \quad (12)$$

$$\hat{v}_i = \frac{v_i}{1 - \mu_2^i}, \quad (13)$$

Finally, the iterative formula is derived as:

$$\begin{bmatrix} \mathbf{W}^{i+1} \\ \boldsymbol{\beta}^{i+1} \end{bmatrix} = \begin{bmatrix} \mathbf{W}^i \\ \boldsymbol{\beta}^i \end{bmatrix} - r \cdot \frac{\hat{m}_i}{\sqrt{\hat{v}_i + \epsilon}}. \quad (14)$$

Here, r represents the learning rate of Adam, and ϵ is a small constant.

Algorithm 1: Adam Training for WResNet-MLP

Input: $E(\mathbf{W}, \boldsymbol{\beta})$ (Eq.(8)), Learning rate r , max_iterations
Initialize: $[\mathbf{W}, \boldsymbol{\beta}] \leftarrow random()$;
 $\mu_1 \leftarrow 0.9$; $\mu_2 \leftarrow 0.999$;
 $m_0 \leftarrow 0$; $v_0 \leftarrow 0$;
 $iteration \leftarrow 0$;
1 while $iteration < max_iterations$ **do**
2 $iteration = iteration + 1$;
3 $\nabla E \leftarrow Eq.(9)$;
4 $\hat{m}_i, \hat{v}_i \leftarrow Eq.(12)(13)$;
5 $\begin{bmatrix} \mathbf{W}^{i+1} \\ \boldsymbol{\beta}^{i+1} \end{bmatrix} \leftarrow Eq.(14)$;
6 end
7 return $[\mathbf{W}, \boldsymbol{\beta}]$

Following Adam training, parameters such as depth (d), learning rate (r), and the number of neurons in the MLP still require tuning. This is accomplished using the Grid Search algorithm.

4 Applications

In this section, we employ the proposed model to develop prediction models for three distinct datasets: natural gas consumption, oil consumption, and overall fossil fuel consumption. Each of the three datasets comprises 612 data points. The initial 80% of the data is allocated for training purposes, while the remaining 20% is reserved for testing. To enhance stability during model training, we preprocess the data using min-max scaling.

Furthermore, this study utilizes the Mean Absolute Percentage Error (MAPE) as a key metric to assess the model’s performance. The representation of the MAPE is shown in Eq.(15). Additionally, we conduct comparative analyses with 10 machine learning models to validate the efficacy of our proposed approach, and their specific information is shown in Tab.1.

$$MAPE = \frac{1}{s} \sum_{k \in U} \frac{|\hat{T}(k) - T(k)|}{|T(k)|} \quad (15)$$

where s is the length of U , and U is the training dataset or testing dataset.

Table 1: The specific information of comparison machine learning models

Full Name	Abbreviation	Reference	Year
Gated Recurrent Unit	gru	[26]	2017
Random Forest Regression	rf	[27]	2001
Extreme Gradient Boosting	xgb	[28]	2015
Long Short-Term Memory	lstm	[29]	2000
Support Vector Regression	svr	[30]	1996
Convolution Neural Network	cnn	[31]	2015
Multilayer Perceptron	mlp	[32]	2009
CNN-LSTM	cnnlstm	[33]	2019
Convolutional LSTM	convlstm	[34]	2017
General Regression Neural Network	grnn	[35]	2004

4.1 Case 1:Natural Gas Consumption

Natural gas is pivotal in shaping the United States' energy landscape, influencing its energy supply, economic growth, and environmental stewardship. Accurately forecasting future natural gas consumption trends is instrumental in optimizing energy resource utilization and fostering sustainable national economic development.

The MAPE evaluation for training and testing across all models in Case-1 is presented in Table 2, while the prediction curves for both training and testing are depicted in Figures 3 and 4, respectively.

Upon examination of Table 2, it becomes evident that the proposed WResNet-MLP model exhibits the most favorable test MAPE value. While the rf model displays the best train MAPE value, its test MAPE value is among the least satisfactory. Although the cnn model's MAPE closely resembles that of the proposed model, its train MAPE is inferior to that of WResNet-MLP.

Furthermore, upon reviewing Figures 3 and 4, it is apparent that the prediction curve of the proposed model closely aligns with the true curve in both training and testing phases. Conversely, the testing forecasting curves of models such as gru, rf, xgb, and grnn exhibit an overall upward shift when compared to the original curve.

Table 2: MAPE Evaluation for Training and Testing Across All Models: Case-1

Model	WResNet-MLP	gru	rf	xgb	lstm	svr	cnn	mlp	cnnlstm	convlstm	grnn
Train	10.572	7.412	2.960	4.051	5.600	8.699	10.699	8.375	5.017	6.862	5.023
Test	8.447	12.914	17.704	20.203	14.717	14.033	8.609	16.063	14.316	16.273	18.105

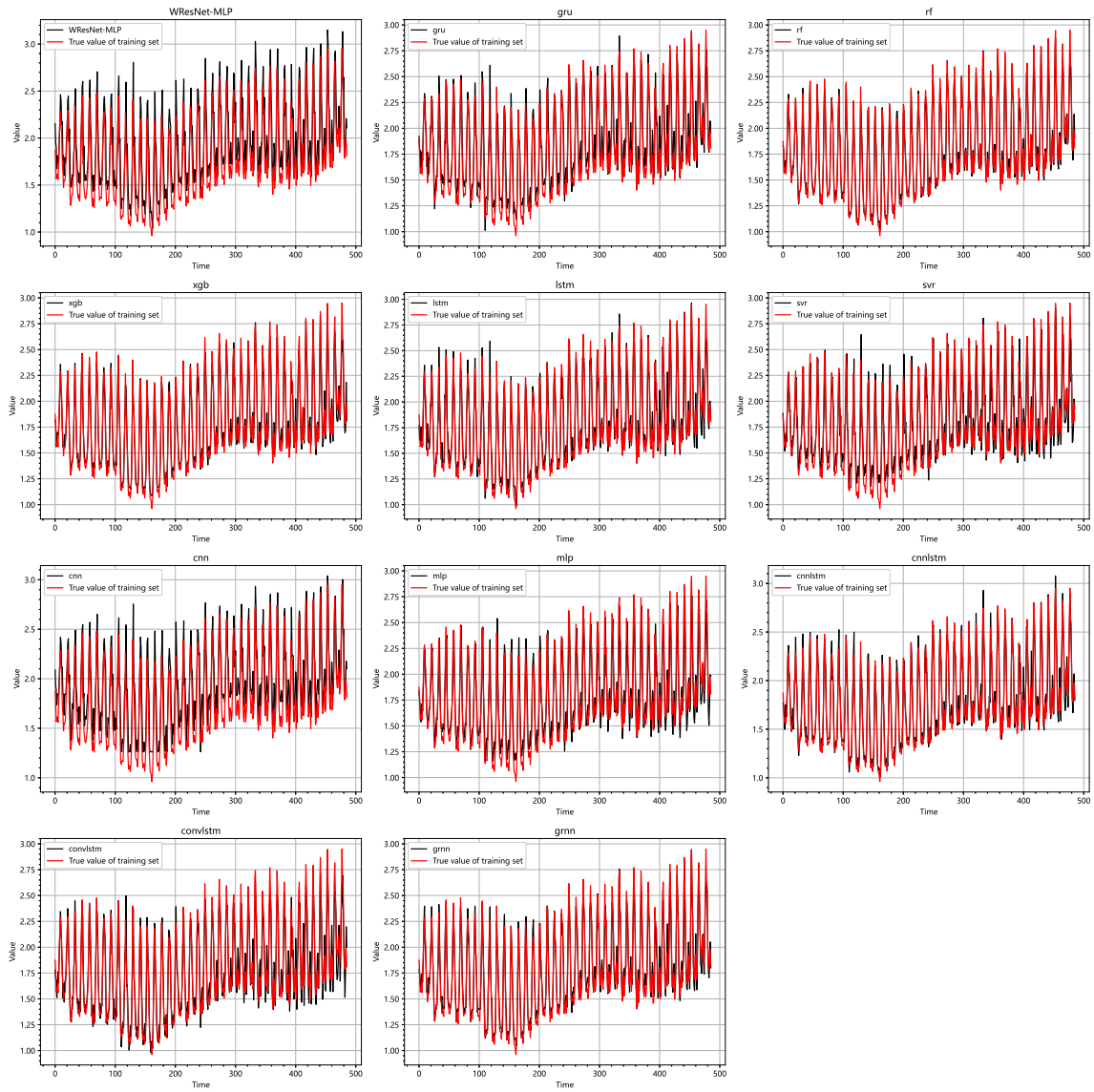


Fig. 3. Forecasted Natural Gas Consumption Values: Training Set

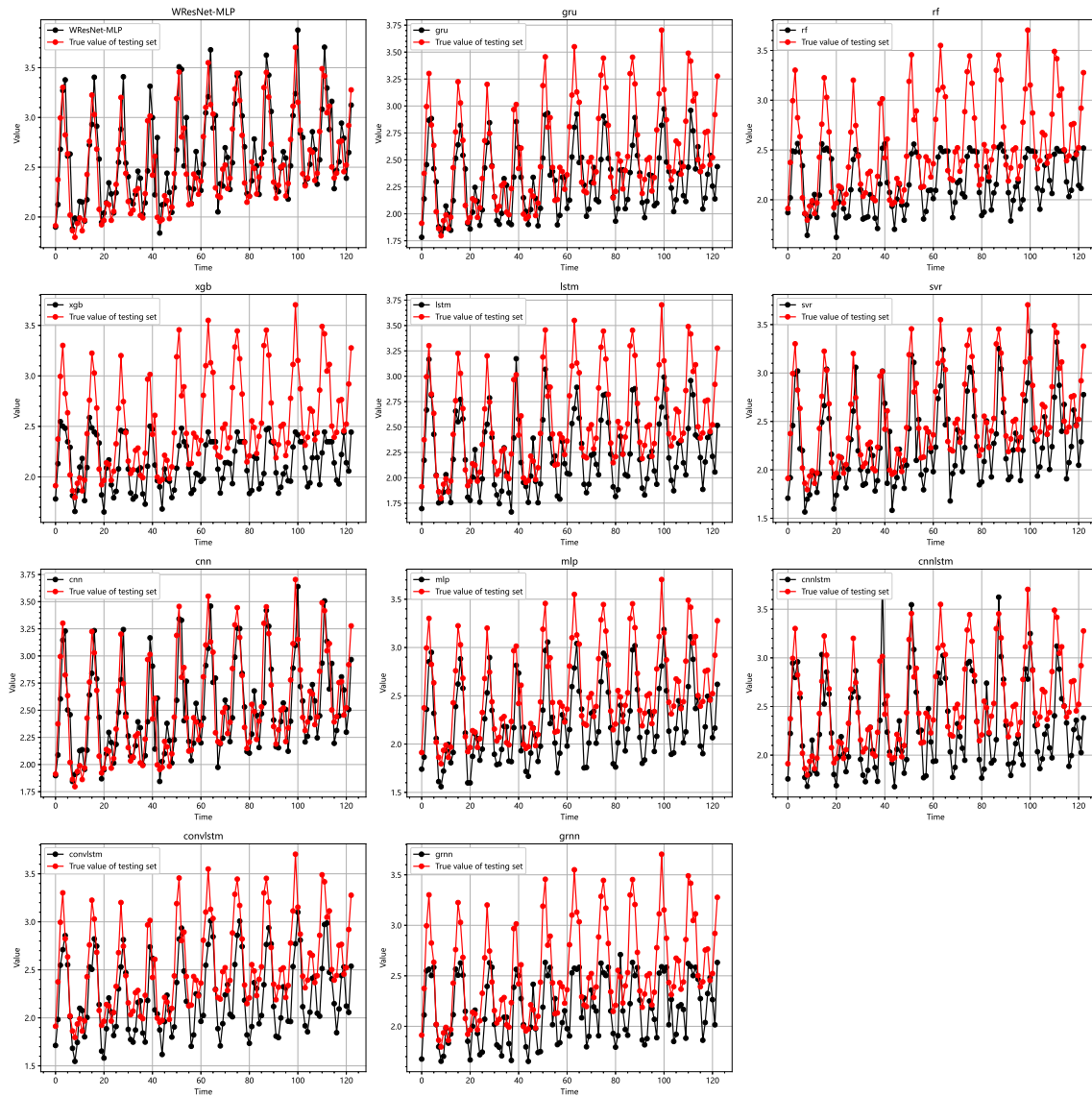


Fig. 4. Forecasted Natural Gas Consumption Values: Testing Set

4.2 Case 2:Petroleum Consumption

Petroleum is a pivotal energy resource in modern industrial society, extensively utilized in transportation, energy production, chemical engineering, and other sectors. Therefore, accurately forecasting future trends in petroleum consumption holds significant implications for national energy security, economic development, and environmental conservation.

Table 3 displays the MAPE evaluation results for training and testing across all models in Case-1. Additionally, Figures 5 and 6 illustrate the prediction curves for both training and testing phases, respectively.

Upon examining Table 3, it's evident that the proposed WResNet-MLP model demonstrates the most promising test MAPE value. While the rf model boasts the best train MAPE value, its test MAPE value falls short in comparison. Upon reviewing Figures 5 and 6, it becomes apparent that in scenarios with significant fluctuations

between adjacent data points, the proposed model exhibits robust performance. Additionally, models such as gru, lstm, cnn, and convlstm also perform admirably under similar conditions.

Table 3: MAPE Evaluation for Training and Testing Across All Models: Case-2

Model	WResNet-MLP	gru	rf	xgb	lstm	svr	cnn	mlp	cnnlstm	convlstm	grnn
Train	3.638	3.624	2.481	3.091	3.615	3.623	3.499	3.610	3.141	3.559	3.069
Test	3.460	3.740	3.761	3.677	3.652	3.539	3.699	3.507	3.796	3.764	3.540

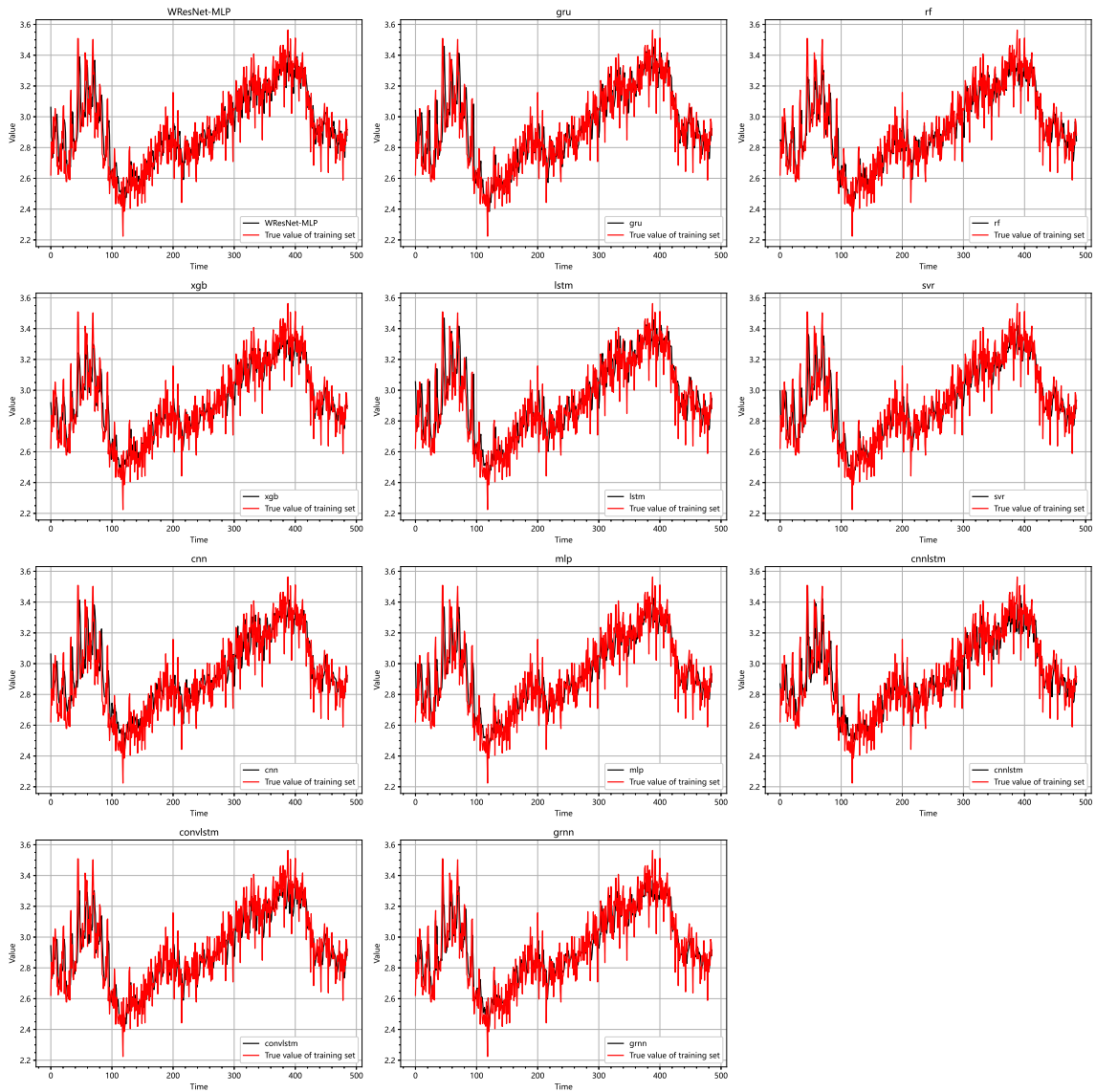


Fig. 5. Forecasted Petroleum Consumption Values: Training Set

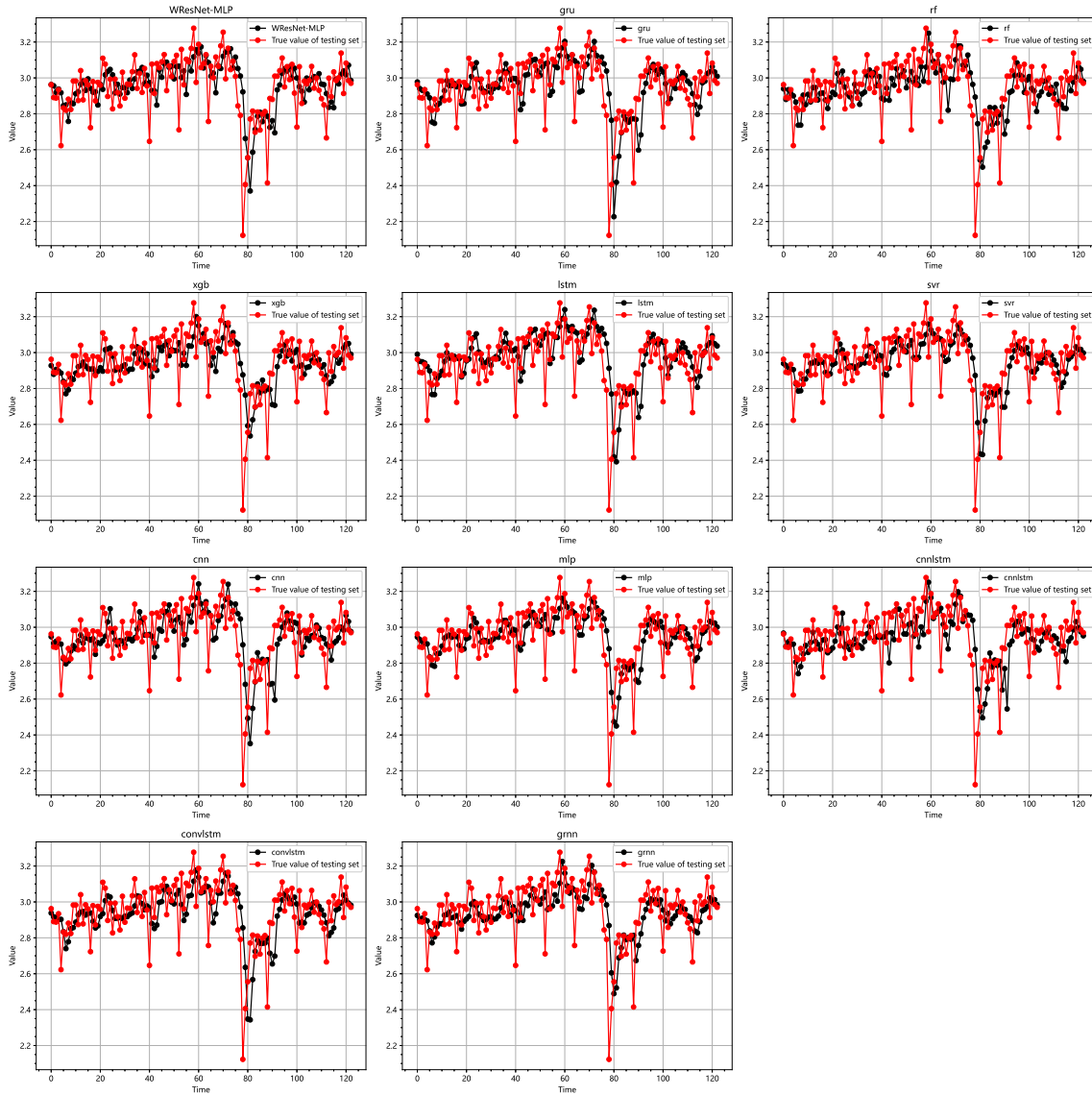


Fig. 6. Forecasted Natural Gas Consumption Values: Testing Set

4.3 Case 3: Total Fossil Fuels Consumption

Fossil fuels, as one of the primary energy sources, are extensively utilized in electricity generation, industrial production, transportation, and other sectors. Hence, accurately forecasting future trends in total fossil fuels consumption is crucial for national energy policy formulation, economic planning, and environmental conservation efforts.

The table below (see Table 4) presents the MAPE evaluation results for training and testing across all models in Case-1. Additionally, Figures 7 and 8 depict the prediction curves for both training and testing phases, respectively. In line with the preceding cases, WResNet-MLP continues to exhibit the optimal test MAPE value, while RF demonstrates the superior train MAPE value. Furthermore, the proposed model’s prediction curve aligns closely with the true curve in both the training and testing phases.

Table 4: MAPE Evaluation for Training and Testing Across All Models: Case-3

Model	WResNet-MLP	gru	rf	xgb	lstm	svr	cnn	mlp	cnnlstm	convlstm	grnn
Train	4.434	3.713	2.136	2.732	3.919	4.277	4.104	5.235	3.360	4.143	3.220
Test	4.464	4.816	4.900	4.848	4.822	4.621	4.466	5.730	4.801	4.959	4.742

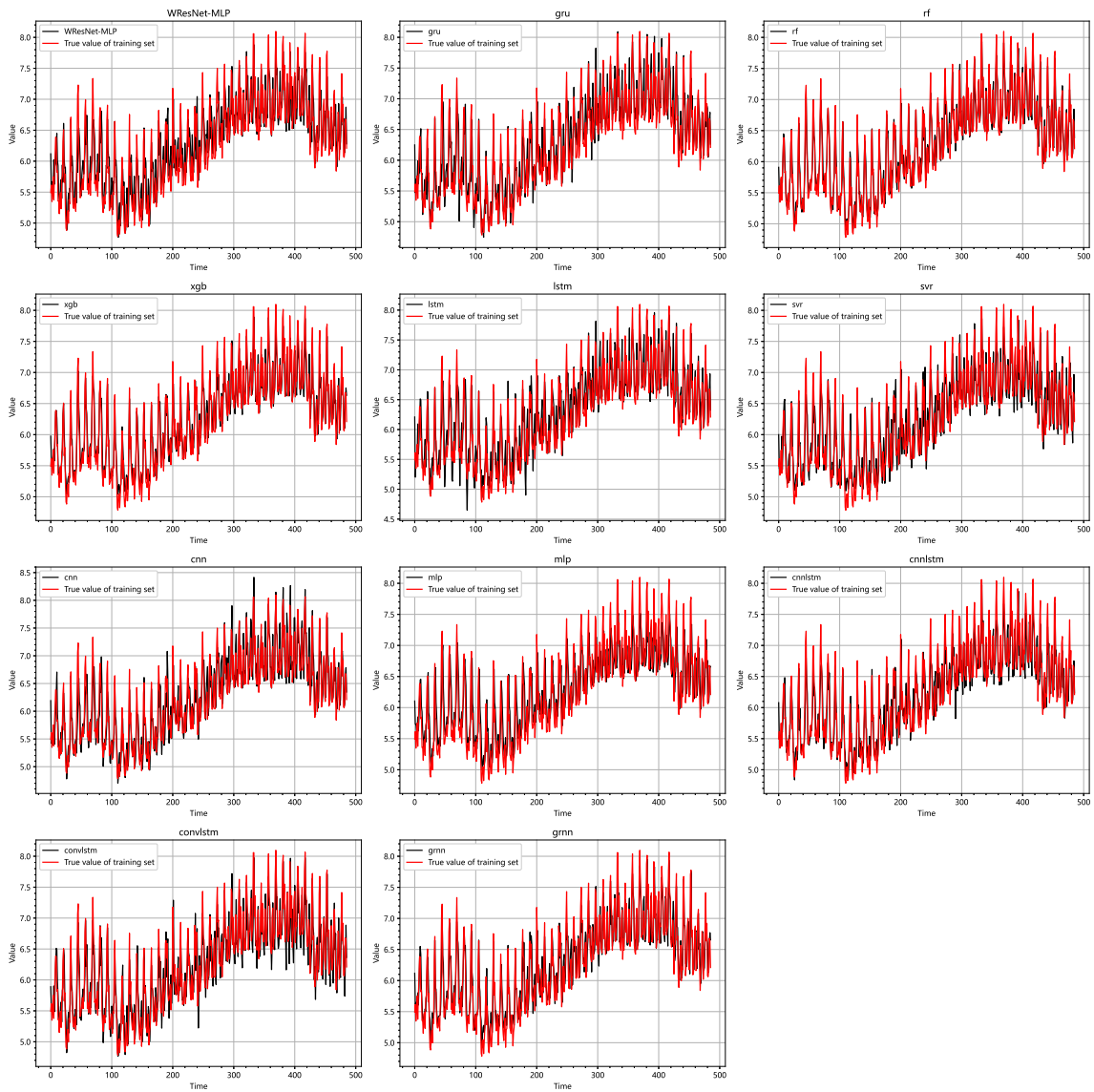


Fig. 7. Forecasted Total Fossil Fuels Consumption Values: Training Set

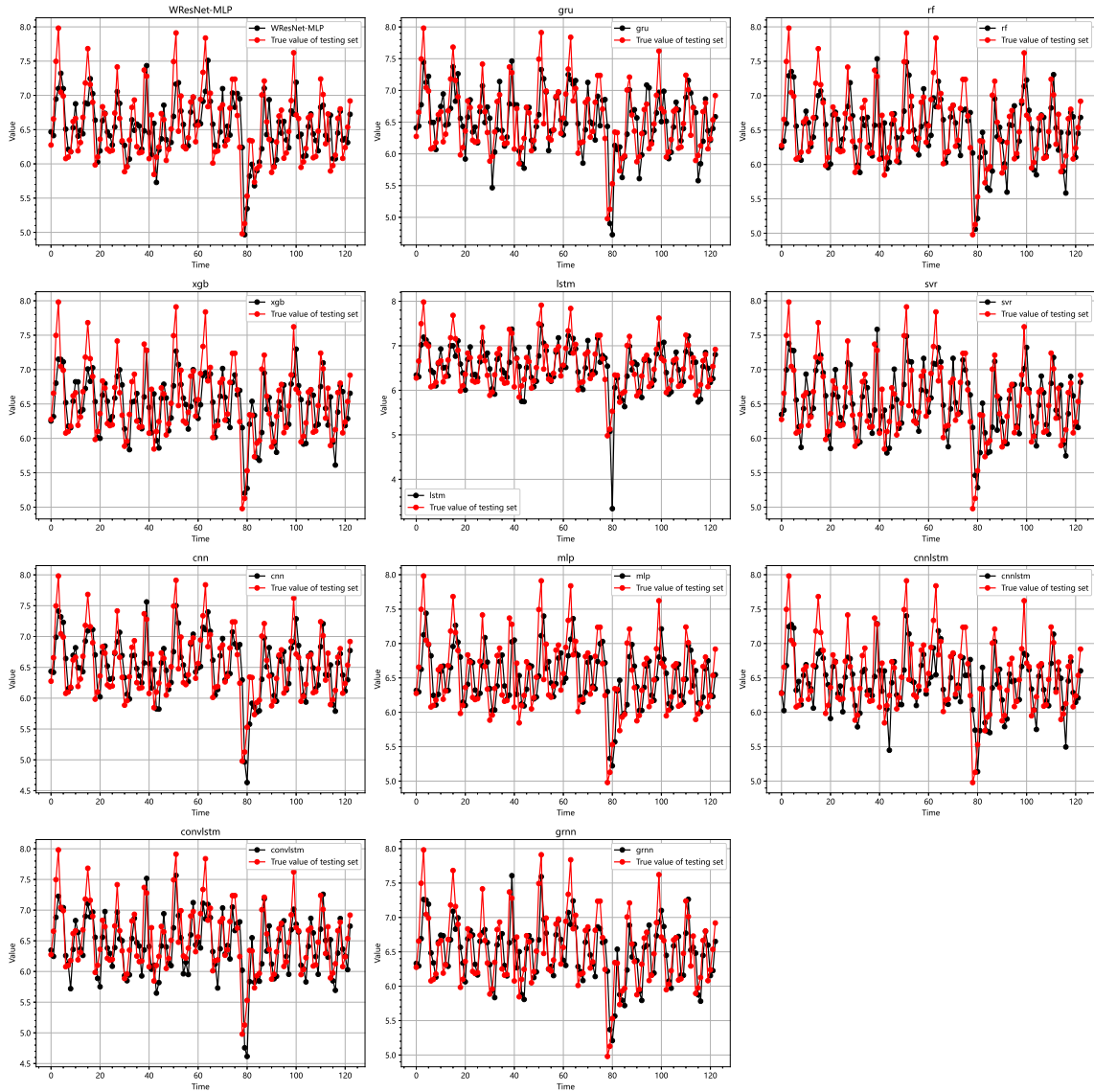


Fig. 8. Forecasted Total Fossil Fuels Consumption Values: Testing Set

4.4 Discussion

The performance of the proposed WResNet-MLP model on the training set is evidently not outstanding. However, across three cases, it emerges as the best performer in testing, closely mirroring the raw data with its prediction curve. This underscores its strong generalization ability and predictive accuracy, showcasing reliability and stability in real-world scenarios. Conversely, although the RF model achieves the highest training MAPE value, it frequently exhibits inferior performance during testing. This could be attributed to either the model’s insufficient complexity or susceptibility to overfitting.

5 Conclusions

In this paper, we introduce the WResNet-MLP model along with its comprehensive theoretical framework and model training methodology. Moreover, the model’s

consistent top performance in testing across cases of natural gas, petroleum, and total fossil fuel consumption highlights its robustness and versatility.

The integration of ResNet and MLP significantly improves prediction accuracy and applicability. We are confident that this approach holds considerable potential for further exploration in future research endeavors.

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