

1
2 **A COMPARATIVE STUDY FOR ESTIMATING**
3 **REFERENCE EVAPOTRANSPIRATION MODELS**
4 **OVER KANO, NIGERIA**
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10 **ABSTRACT**
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The major factor faced by Agricultural activities is water scarcity. Water is very essential in Agricultural activities (plantation), crop acquires water naturally by precipitation and subsurface moisture, when the supply of water is inadequate for crop use, mostly results to irrigation. This present study estimates and compares six various universally accepted models for estimating reference evapotranspiration (ET_0) for Kano situated in the Sahelian climatic zone of Nigeria using measured meteorological parameters of monthly average daily global solar radiation, sunshine hour, wind speed, minimum and maximum temperatures and relative humidity covering a period of thirty one years (1988 – 2018). Four different statistical validation indices of Root Mean Square Error (RMSE), Mean Bias Error (MBE), Mean Absolute Error (MAE) and coefficient of correlation (R) were carried out to test the accuracy of the evaluated models. The result indicated that high value of ET_0 was found in the month of April with 10.0256 mm/day for Kano and a low value was found to be in August with 5.0804 mm/day for Kano. The Blaney – Morin Nigeria model was found more accurate for Kano with RMSE, MBE, MAE and R values as 1.5078 mm/day, -1.4634 mm/day, 1.4634 mm/day and 0.9790 respectively.

12
13 *Keywords: Evapotranspiration, Kano, lysimeter, models, NIMET, statistical indicator*
14

15 **1. INTRODUCTION**
16

17 Evapotranspiration is a combination of evaporation and transpiration; these two processes
18 leads to the loss of water content in plant. It covers both water evaporation (movement of
19 water to the air directly from soil, canopies and water bodies) and transpiration (movement of
20 water from the soil, through roots and bodies of vegetation, on leaves and then into the air).
21 Evapotranspiration is measured in order to ascertain the amount of water required for
22 irrigation. The rate of evapotranspiration is measured in millimeters per a set unit of time
23 (usually per day) [1]
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25 The total crop water needed is directly proportional to ET, since ET is usually known as crop
26 water needed. These two processes i.e., Evaporation and Transpiration lead to water loss
27 from the crops. The significance of this study is to improve the control of water for irrigation
28 purpose between residential, industrial and agricultural use. This study also helps irrigation
29 managers to know the amount/quantity of water to be applied for irrigation purpose through
30 the help of the most suitable ET model recommended for Kano. Conforming to Allen et al.
31 [2], ET_0 is a major agro – meteorological parameter for climatological and hydrological
32 studies, as well as for irrigation scheme and management.

33 ET is measured with the aid of lysimeter, this lysimeter is not readily available for an
34 individual to obtain because of high cost acquisition and handling of the device leads to the

35 development of several ET models used in the estimation of the ET_0 . The major drivers that
36 speed up the rate of ET are solar radiation, wind speed, relative humidity and air
37 temperature [3].

38 Numerous researches have been carried out on this present study that involves the
39 estimation of evapotranspiration with different ET models across different climatic zones of
40 Nigeria. These includes the study by Yusuf et al. [4] conducted a research on the estimation
41 of evapotranspiration rate in the sahelian region of Nigeria using generalized regression
42 neural network and feed forward neural network. The climatological data used in their study
43 was collected from the International Institute of Tropical Agriculture (IITA) station of 25-year
44 monthly-time step. Based on performance ranking of input combinations used in different
45 neural networks, the solar radiation (GRNNSr) with a Root Mean Square Error (RMSE) of
46 1.982 ranked lowest while the temperature and wind speed combination input (GRNNTW)
47 ranked highest with a Root Mean Square Error (RMSE) of 0.7777. The input combination of
48 temperature, wind speed and solar radiation had the best performance under the Feed
49 Forward Back Propagation Neural Network (FFBP NN) with RMSE as low as 0.6333. This is
50 contrast to the input combination of solar radiation and humidity, which had the lowest
51 performance under the FFBP NN with RMSE of 1.3512. The input combination of
52 temperature and wind speed is the most preferred input combination, having less data input
53 and higher performance. Onwuegbunam et al. [5] carried out a research on estimation and
54 comparison of reference evapotranspiration within Kaduna central district Nigeria using four
55 different methods. The reference evapotranspiration (ET) within Kaduna central district,
56 Nigeria was estimated from 30-year climatological data using four different methods
57 panman-monteith (PM), Blaney - Criddle (BC), Hargreaves (HGRV) and piche evaporimeter
58 (PiEr) (atmometer) methods. In their study, they found out that the highest ET values
59 obtained from PM, BC and PiEr were 6.43 mm/day, 7.58 mm/day and 8.63 mm/day,
60 respectively and these occurred in February except for HGRV which estimated its highest
61 ET(3.78 mm/day) in March the lowest ET. Values were obtained in August for all the
62 methods, the results showed that BC, HGRV and PiEr gave c-values of 0.88, 0.48 and 0.67
63 respectively. Zarie et al. [6] compared several methods to estimate Reference ET_0 , their
64 study explores the output range and sensitivity of models of different models in the
65 Garebayegan research station at far province. The results show that pan evaporation
66 method, Hargreaves-Samani modified 2 and Blaney-criddle have no significant difference by
67 PM FAO-56 and Pan-Evaporation method has most similarity to PM FAO-56. Jensen-Haise
68 and Thoruthwaite has most difference by PM FAO- 56. In another studies, Akpootu and
69 Iliyasu [7] compared various universal accepted ET models for estimating ET_0 , they consider
70 in their study, six models for estimating ET_0 for Sokoto, using meteorological parameter of
71 monthly average daily global solar radiation, sunshine hour, wind speed, maximum and
72 minimum temperature and relative humidity covering a period of thirty -one years (1980-
73 2010). Their result shows that blaney-morin Nigeria model can also be used in place of FAO-
74 56 PM model for estimating ET_0 in Sokoto. Adekunle et al. [8] evaluated the performance of
75 some evapotranspiration models at tropical location in Ile-Ife, Nigeria. From their result, they
76 observed that Priestley Taylor model has the highest value ranging from between 1.323 -
77 6.936 mm/day of reference evapotranspiration. They concluded that Jessen - Haise model
78 has strong agreement with FAO-56 PM and can be adjusted suitable for ET estimation at
79 tropical location such as Ile-Ife.

80
81 This present study, evaluates and compares six evapotranspiration models for estimating
82 reference evapotranspiration in Kano, Nigeria, using FAO – 56 PM method as standard. The
83 reason for this comparison is to find out which of the six evaluated models is most
84 appropriate to be considered as an alternative to FAO – 56 PM model for estimating ET_0 in
85 Kano based on the four adopted statistical indicators.

86

87 2. METHODOLOGY

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89 Over forty (40) weather observatories are located in Nigeria at different stations which are
90 controlled by the Nigerian Meteorological Agency. None of these stations measure
91 evapotranspiration. The climatic data of measured monthly average daily global solar
92 radiation, sunshine hour, wind speed, maximum and minimum temperatures and relative
93 humidity covering a period of thirty-one years (1988-2018) for Kano situated in Sahelian
94 region of Nigeria was obtained from the Nigerian Meteorological Agency (NIMET), Oshodi,
95 Lagos, Nigeria.

96 2.1 FAO-56 Penman- Monteith Method (FAO56 PM)

97 This approach has been implemented and recommended as the general overall method for
98 the determinant of ET_0 by the United Nation Food and Agricultural Organizations (FAO) and
99 was used worldwide because it put both the physical and aerodynamic parameters into
100 consideration. PM equation is considered the best methods so far for the estimation of ET_0
101 in all climatic conditions. The FAO- 56 PM method is often recommended as a standard
102 procedure for accurate estimation of ET_0 where there is no measured lysimeter data on
103 reference evapotranspiration. The evapotranspiration ET values obtained from the derived
104 equations are usually compared against this method. The ET_0 was calculated using the PM
105 model for the ET_0 estimation recommended by the FAO-56 paper Allen et al. [2], and
106 standardized by the American society of the civil Engineer-ASCE [9] and is expressed as

$$107 \quad ET_0 = \frac{0.408\Delta(R_n - G) + \frac{900}{T+273} U_2 (e_s - e_a)}{\Delta + \gamma(1 + 0.34U_2)} \quad (1)$$

108 where ET_0 is the reference evapotranspiration (mmday^{-1}), R_n is the net radiation at the crop
109 surface ($\text{MJm}^{-2}\text{day}^{-1}$), G is the solar heat flux ($\text{MJm}^{-2}\text{day}^{-1}$), T is the mean daily air
110 temperature ($^{\circ}\text{C}$), U_2 is the wind speed at 2m height (ms^{-1}), e_s is the saturated vapour
111 pressure (KPa), e_a is the actual vapour pressure (KPa), $e_s - e_a$ is the saturated vapour
112 pressure difference (KPa) and γ is the psychrometric constant ($\text{KPa}^{\circ}\text{C}^{-1}$). According to
113 Łabędzki et al. [10], the soil heat flux can be ignored and assumed to be zero, since it is
114 small compared to the value R_n .

115 In this study, R_n , Δ , U_2 , e_s , e_a and γ was be calculated as proposed by FAO as reported by
116 Allen et al. [2]. The mean saturated vapour pressure derived from air temperature is given by
117 [2].

$$118 \quad e_s = \frac{e(T_{max}) + e(T_{min})}{2} \quad (2)$$

$$119 \quad e(T_{max}) = 0.6108 \exp\left(\frac{17.27T_{max}}{T_{max} + 273}\right) \quad (3)$$

$$120 \quad e(T_{min}) = 0.6108 \exp\left(\frac{17.27T_{min}}{T_{min} + 273}\right) \quad (4)$$

121 T_{max} is the maximum daily air temperature in $^{\circ}\text{C}$, T_{min} is the minimum daily temperature in
122 $^{\circ}\text{C}$.

123 The actual vapour pressure derived from relative humidity was computed using the
124 expression:

$$125 \quad e_a = \frac{RH_{max}}{100} \left[\frac{e(T_{max}) + e(T_{min})}{2} \right] \quad (5)$$

126 The slope of the saturated vapour pressure curve was obtained using the following
127 expression:

$$128 \quad \Delta = 4098 \left[\frac{0.6108 \exp\left(\frac{17.27T}{T+273.3}\right)}{(T+273.3)^2} \right] \quad (6)$$

129 The atmospheric pressure P is related to z as shown in the expression below

$$130 \quad P = 101.3 \left(\frac{293 - 0.0056Z}{293} \right)^{5.26} \quad (7)$$

131 where, Z is the station elevation above sea level in meters.

132 The psychrometric constant, is related to P by the expression given below:

$$133 \quad \gamma = 6.65 \times 10^{-4} P \quad (8)$$

134 The net radiation R_n was estimated using the expression

$$135 \quad R_n = R_{ns} - R_{nl} \quad (9)$$

136 where R_{ns} and R_{nl} is a shortwave and long wave radiation in ($\text{MJm}^{-2}\text{day}^{-1}$) was calculated
137 according to the FAO irrigation and drainage paper No. 56 as

$$138 \quad R_{ns} = (1 - a)R_s \quad (10)$$

139 where a is the albedo or canopy reflection coefficient which is 0.23 for the hypothetical grass
140 references crop (dimensionless) R_s is the incoming solar radiation ($\text{MJm}^{-2}\text{day}^{-1}$)

$$141 \quad R_{nl} = \sigma \left[\frac{T_{\max, k}^4 + T_{\min, k}^4}{2} \right] (0.34 - 0.14\sqrt{e_a}) \left\{ 1.35 \frac{R_s}{R_{s0}} - 0.35 \right\} \quad (11)$$

142 where σ is the Stefan Boltzmann constant ($4.903 \times 10^{-9} \text{MJm}^{-4} \text{m}^{-2}\text{day}^{-1}$)

143 $T_{\max, k}$ is the maximum absolute temperature during the 24hour period ($k=^{\circ}\text{C}+273.16$) $T_{\min, k}$

144 is the minimum absolute temperature during the 24-hour period ($k=^{\circ}\text{C}+273.16$)

145 R_s/R_{s0} is the relative shortwave radiation (limited to ≤ 1.0) and R_{s0} is the calculated clear sky
146 radiation ($\text{MJm}^{-2}\text{day}^{-1}$). R_{s0} was obtained using the following expression

$$147 \quad R_{s0} = (a_s + b_s)R_a \quad (12)$$

148 $a_s + b_s$ is the fraction of extraterrestrial radiation reaching the earth no clear sky day and R_a

149 is the extraterrestrial radiation ($\text{MJm}^{-2}\text{day}^{-1}$). The fraction of extraterrestrial radiation reaching

150 the earth on clear sky day was obtained using regression analysis with Minitab 16.0 software

151 based on the following expression

$$152 \quad R_s = \left[a_s + b_s \left(\frac{s}{s_0} \right) \right] R_a \quad (13)$$

153 where s/s_0 is the relative sunshine duration R_a was calculated according to the FAO irrigation
154 and drainage paper No. 56 Allen et al. [2].

155 The wind speed data obtained from the meteorological station was converted to 2m as
156 required for agrometeorological according to the following expression:

$$157 \quad U_2 = U_z \frac{4.87}{\ln(678z - 5.42)} \quad (14)$$

158 where U_z is the measured wind speed at Z_m above the ground surface (m/s). Six ET models
159 are utilized in this study.

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161 **2.2 Blaney- Morin- Nigeria Model**

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163 The Blaney- Morin- Nigeria (BMN) model was developed for the estimation of reference
164 evapotranspiration in Nigeria by [11]. This method was applied following the procedures laid
165 down by Duru [11]. The model equation is equation is given by

$$166 \quad ET_o = \frac{rf(0.45T_{mean} + 8)(520 - R^{1.31})}{100} \quad (15)$$

167 where, rf is the ratio of monthly radiation to annual radiation, T_{mean} is the mean monthly
168 temperature in $^{\circ}\text{C}$ and R is the mean monthly relative humidity, 520 and 1.31 are the model
169 constants given by Duru [11]. ET_o is as previously defined.

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171 **2.3 Priestley and Taylor model**

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173 Priestley and Taylor [12] method is a simplified method requiring only solar radiation and
174 temperature weather parameters for the computation of evapotranspiration. This is based on
175 the fact that radiation is the major source of energy and thus a potential factor as compared
176 to other weather parameters for evapotranspiration computation. According to them about
177 two-third radiation components contributes to the evaluation of evapotranspiration. The
178 model estimation is done using the equation:

$$179 \quad ET_o = \alpha \frac{\Delta}{\Delta + \gamma} (R_n - G) \frac{1}{\lambda} \quad (16)$$

180 where, α is an empirically determined dimensionless correction given as $\alpha=1.26$ and λ is the
 181 latent heat of vaporization (2.45 MJg^{-1} @ 20°C), $\Delta, \gamma, R_n, ET_o$ and G are as previously defined.

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183 **2.4 Mankkink (Makik) Model**

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185 The Mankkink model was proposed in 1957 in the Netherlands as a modification of Penman
 186 after comparing the Penman model to lysimetric data [9,13]. Recently, Mankkink is popular
 187 in West Europe and has been used successfully in the US Amatya et al. [14]. [9] gives the
 188 operational form of the Mankkink model as

$$189 \quad ET_0 = 0.61 \left(\frac{\Delta}{\Delta + \gamma} \right) \left(\frac{R_s}{2.45} - 0.12 \right) \quad (17)$$

190 where ET_0 is the reference Evapotranspiration (mmday^{-1}), R_s is the solar radiation ($\text{MJm}^{-2}\text{day}^{-1}$)
 191 and Δ and γ are as already defined.

192

193 **2.5 Hangreaves and Samani Model (H&M)**

194 This model was developed by Hargreaves and Samani, [15] using 8 years of daily lysimeter
 195 data from Daris California and the model was tested in different locations such as Australia,
 196 Haiti, and Bangladesh. Since the development of the model, it has been successfully
 197 implemented and recommended worldwide [16]. The Hangreaves equation requires only
 198 daily mean, maximum and minimum air temperature and extraterrestrial radiation. This
 199 simply means that any condition where solar radiation, wind speed and relative humidity
 200 data are not measured, ET_0 can be determined using temperature data according to the
 201 model equation stated by Hangreaves and Samani [15].

$$202 \quad ET_0 = 0.0023(T_{mean} + 17.8)(T_{max} - T_{min})^{0.5} R_a \quad (18)$$

203 where T_{mean} and R_a is extraterrestrial radiation, and the mean air temperature given as
 204 [17,18]

$$205 \quad T_{mean} = \frac{T_{max} + T_{min}}{2} \quad (19)$$

206

207 **2.6 Absteu Model (1996)**

208

209 Absteu [19] make used of simple empirical model which shows reference evapotranspiration
 210 ET_0 as a function of solar radiation only. The model is given by:

$$211 \quad ET_0 = \frac{0.53 R_s}{\lambda} \quad (20)$$

212 where λ is the latent heat flux and R_s is the shortwave solar radiation ($\text{MJm}^{-2}\text{day}^{-1}$)

213 Absteu approach was cross validated by comparing the estimates to four years of Bowen
 214 ratio ET_0 measurement at nine site (area) Everglade of South Florida [19] and the results
 215 revealed a very good correlation of ET_0 estimated by Absteu method and that obtained by
 216 Bowen-Ratio over a wet land.

217 **2.7 Jensen Haise Model (JHM)**

218

219 This model was estimated over 3000 observation of evapotranspiration (ET) as calculated by
 220 soil sampling steps over the period of 35 years in western USA [20]. From their study,
 221 Jensen-Haise Model developed the following relationship of evapotranspiration model used
 222 in computing reference evapotranspiration (ET_0) as reported by James [21]. The equation of
 223 the model is given by

$$224 \quad ET_0 = C_T (T_{mean} - T_x) R_s \quad (21)$$

225 C_T and T_x are constants expressed as;

$$226 \quad C_T = \frac{1}{\left[\left(45 - \frac{L}{137} \right) + \left(\frac{365}{e^{(T_{max})} - e^{(T_{min})}} \right) \right]} \quad (22)$$

$$227 \quad T_x = -2.5 - 0.14 \left[e^{(T_{max})} - e^{(T_{min})} \right] - \frac{h}{500} \quad (23)$$

228 where h is the attitude of the location $e^{(T_{max})}$, $e^{(T_{min})}$, T_{mean} and R_s are define previously.

229

230 2.8 Statistical Analysis

231

232 The models that are used in this study in computing the reference evapotranspiration (ET_o)
233 for the location under study were statistically tested using the Mean Bias Error (MBE), Root
234 Mean Square Error (RMSE), Mean Absolute Error (MAE) and correlation coefficient (R).

235

236 2.8.1 Root Mean Square Error (RMSE)

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238 This measures the average difference. RMSE involves the square of difference and
239 therefore becomes sensitive to extreme values [22]. The smaller the value of the RMSE the
240 better is the model Performance. The magnitudes of RMSE values are useful to identify
241 model performance but not of under or overestimation by individual model [23]. The peak
242 value for RMSE is zero or $0.0 \leq RMSE$ [24] is given by the equation [25 – 33]:

$$243 \quad RMSE = \left[\frac{1}{n} \sum_{i=1}^n (ET_{oest} - ET_{OFAO})^2 \right]^{\frac{1}{2}} \quad (24)$$

244 2.8.2 Mean Bias Error (MBE)

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246 The mean bias error is a very good measure of model bias and simplifies the average of all
247 differences in the set. It provides general business but not of the average error that could be
248 expected [22]. The positive MBE value indicates overestimation and the negative value
249 indicates underestimation. The absolute value is indicator of model performance. The peak
250 value for MBE is zero like RMSE and the biasness lies between the range of $-\infty$ to $+\infty$ ($-\infty <$
251 $bias \leq +\infty$). The MBE is given by the modified equation of [34 – 42]:

$$252 \quad MBE = \frac{1}{n} \sum_{i=1}^n (ET_{oest} - ET_{OFAO}) \quad (25)$$

253 2.8.3 Mean Absolute Error (MAE)

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255 The MAE is an absolute value of the MBE. Thus, in this case, all the value of MBE becomes
256 positive. The MAE is given by the equation:

$$257 \quad MAE = \frac{1}{n} \sum_{i=1}^n |ET_{oest} - ET_{OFAO}| \quad (26)$$

258 2.8.4 Correlation Coefficient (R)

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260 The quantity (R) called the coefficient of correlation and is given by the equation:

$$261 \quad R = \frac{\sum ET_{oest} ET_{OFAO} - \frac{1}{n} \sum ET_{oest} \sum ET_{OFAO}}{\sqrt{\left(\sum ET_{oest}^2 - \frac{(\sum ET_{oest})^2}{n} \right) \left(\sum ET_{OFAO}^2 - \frac{(\sum ET_{OFAO})^2}{n} \right)}} \quad (27)$$

262 The value of R varies between -1 and +1 [7].

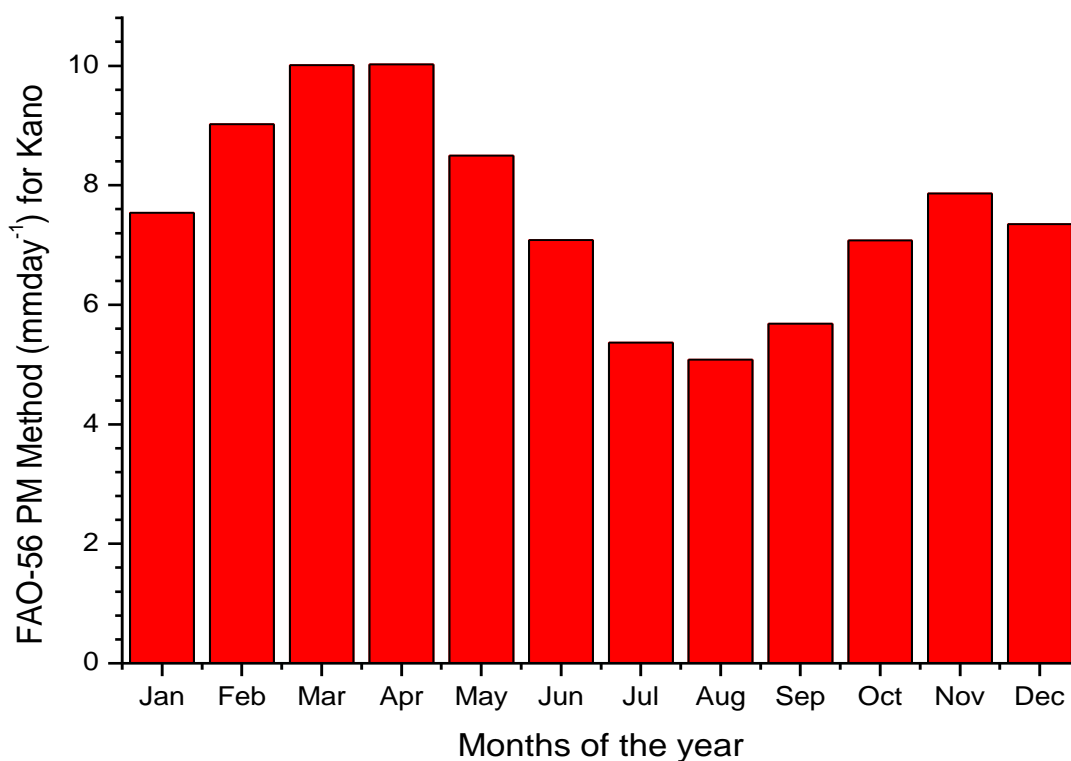
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264 From the equations above the variable ET_{OFAO} represents the observed or measured
265 reference evapotranspiration (ET_o) values (the FAO-56 PM model); ET_{oest} is the estimated/
266 predicted values of the reference evapotranspiration (ET_o) obtained from the other models, n
267 is the number of observations, \sum is the summation sign. In this study, coefficient of
268 correlation (R) was verified using scatter diagram as well.

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270 3. RESULTS AND DISCUSSION

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Fig. 1. Monthly values of ET_0 for FAO – 56 PM method in Kano during the period (1988 - 2018)

Fig. 1 shows the variation of evapotranspiration with month for the study area during the study period. It showed that the highest value of the evapotranspiration was obtained during the hot dry season in the month of April and the lowest value is in the month of August which is rainy (wet) season. This shows that during the hot dry season the amount rate of evapotranspiration is usually maximum and minimum during the rainy season. During the hot dry season, the amount of water required for irrigation is more than during the rainy (wet) season. For this study area, the highest value of ET was found in the month of April with 10.0256 mm/day and the lowest value of 5.0804 mm/day in the month of August. This result is closely related to that of Isikwue et al. [43], they found out that the lowest value was in the month of August with 60.406 mm/day, and the highest value in the month of February with 125.08 mm/day, however, the both results indicate that during the dry season the value of ET_0 is high and is low during the rainy season. The high value is due to the fact that ET is high during the hot dry weather or clear sky condition as a result of dryness of air and the amount of heat energy available for evaporation. Solar radiation is one of the weather parameters which contributes to the rate of evapotranspiration. Wind speed also serves as a catalyst during this period, which speedup evaporation that enhances fast transport of water vapour from moist vegetation of the dry atmosphere. The constant replacement of the moist air located within and just above the plant canopy with dry air from above is done by the wind. Solar radiation and wind speed play an important role in the rate of ET.

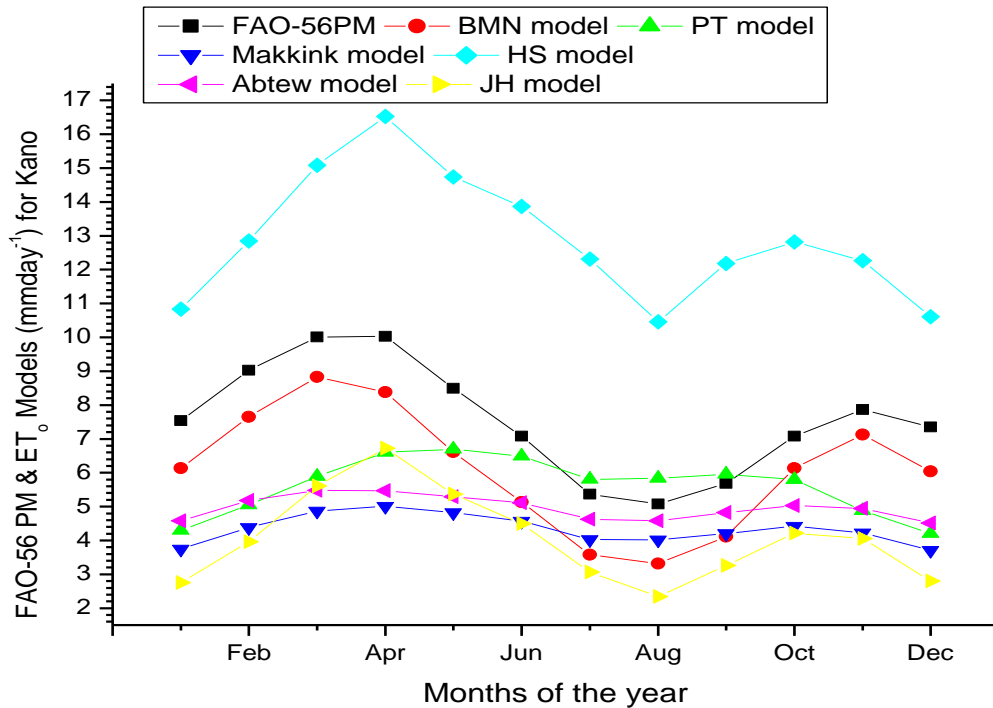


Fig. 2. Comparison between estimated ET₀ by FAO – 56 PM and evaluated models in Kano during the period (1988 - 2018)

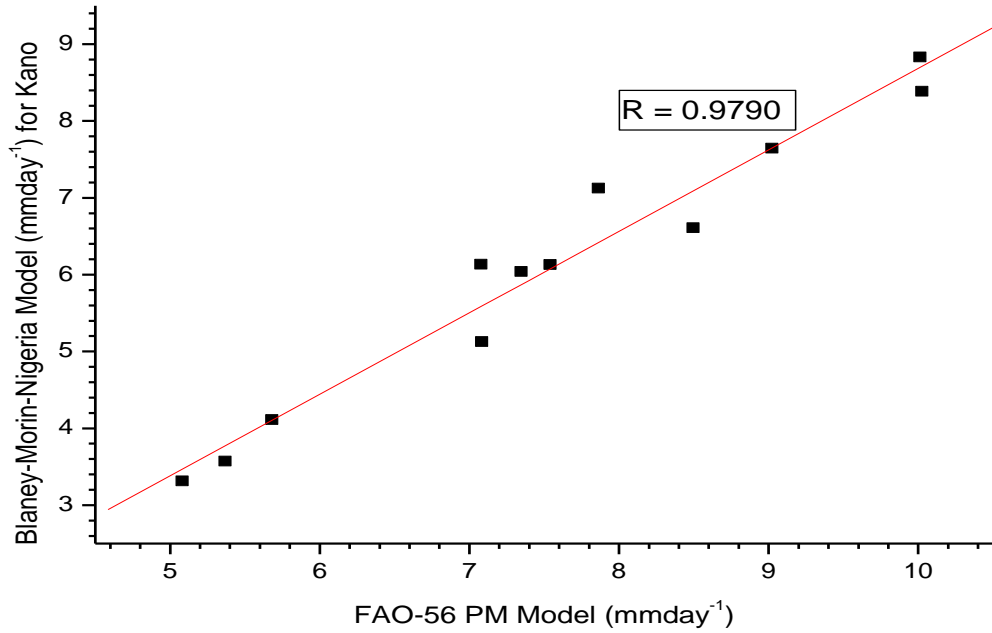
Fig. 2 shows the monthly averages values of ET₀ estimates, using as the baseline the period from 1988 – 2018. Obviously from figure 2, it shows FAO – 56 PM model overestimates the Blaney – Morin Nigeria model including other estimated ET₀ models from January to June and from October to December, except for Hangreaves and Samani model that overestimated other estimated ET models including the reference FAO – 56 PM model throughout the year. The Jessen – Haise model underestimates other estimated ET models from July to December. The Blaney – Morin Nigeria model curve pattern estimates closely follows the pattern of the FAO – 56 PM model during the entire year but there is some form of dispersion between them.

In view of the six evaluated ET models, the value of the ET was recorded to be high in the month of March with 8.8326 mm/day and the lowest value in the month of August with 3.3137 mm/day for Blaney – Morin Nigeria model. The highest value of ET was recorded in the month of May with 6.7003 mm/day and the lowest in the month of December with 4.2099 for Priestley and Taylor model. The highest value of ET was recorded in the month of April with 5.0087 mm/day and the lowest in the month of December with 3.7081 mm/day for Makkink model. The highest value of the ET was recorded in the month of April with 16.5282 mm/day and the lowest in the month of August with 10.4552 mm/day for Hangreaves and Samani model. The highest value of ET was recorded in the month March with 5.4805 mm/day and the lowest in the month of December with 4.5113 mm/day for Abstew model. The highest value of the ET was recorded in the month of April with 6.7256 mm/day and the lowest value in the month August with 2.3394 mm/day for Jessen – Haise model.

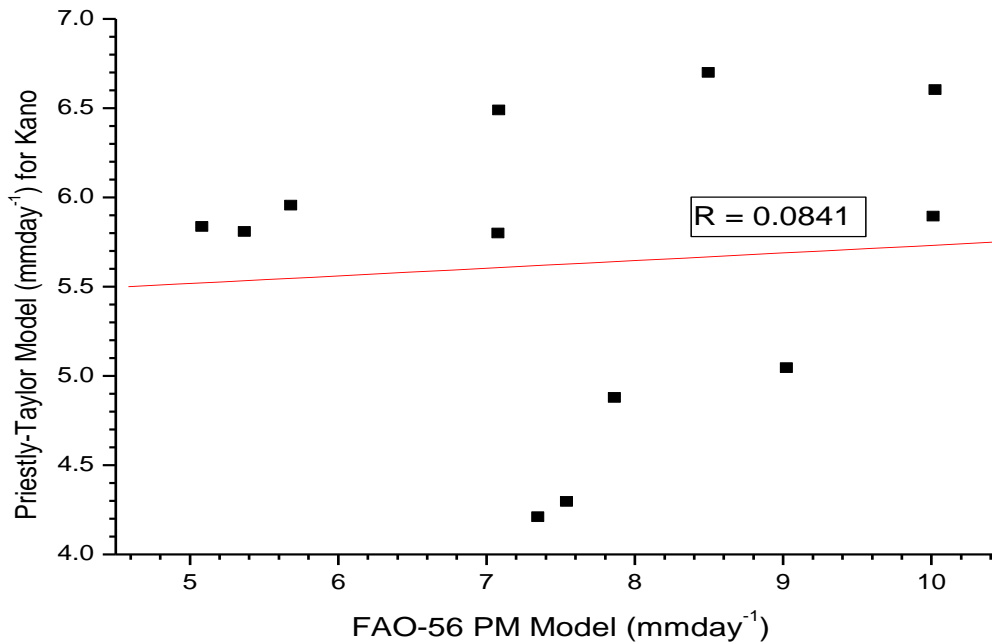
The ET₀ value computed was observed that Blaney – Morin Nigeria model is in line with FAO – 56 PM model value, as the highest and lowest values was in the same months of March and August respectively. Subsequently, the Blaney – Morin Nigeria model for

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321 estimating ET_0 compares favorably well with the FAO – 56 PM model and therefore can be
322 used as an alternative method of estimating ET in Kano.



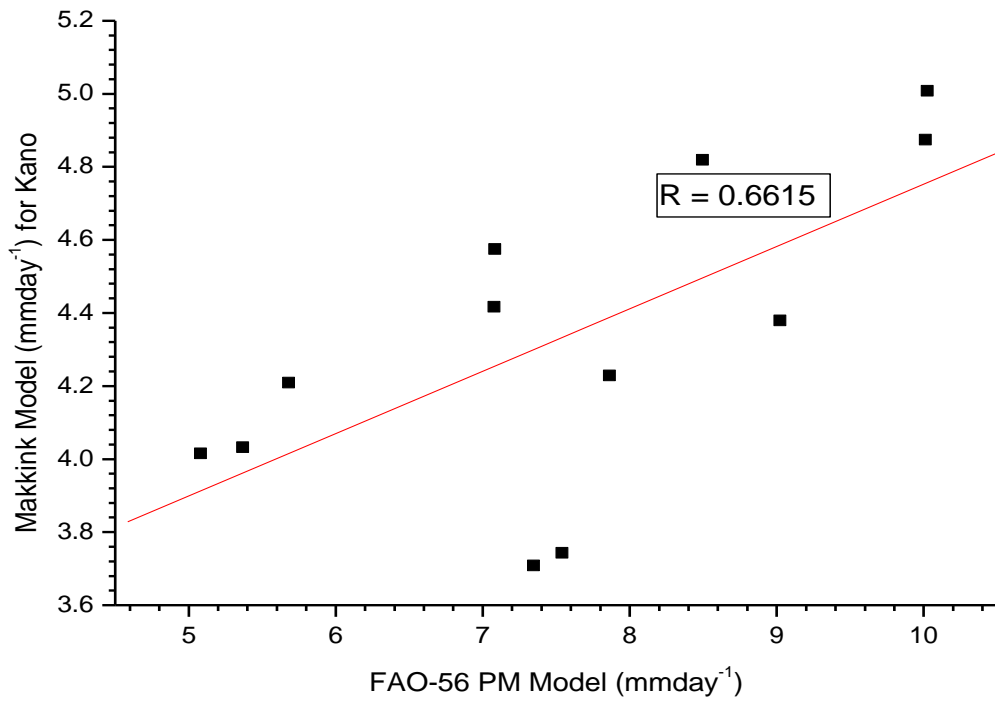
323 **Fig. 3. Fitted regression line of Blaney – Morin Nigeria model with reference FAO – 56**
324 **PM model**
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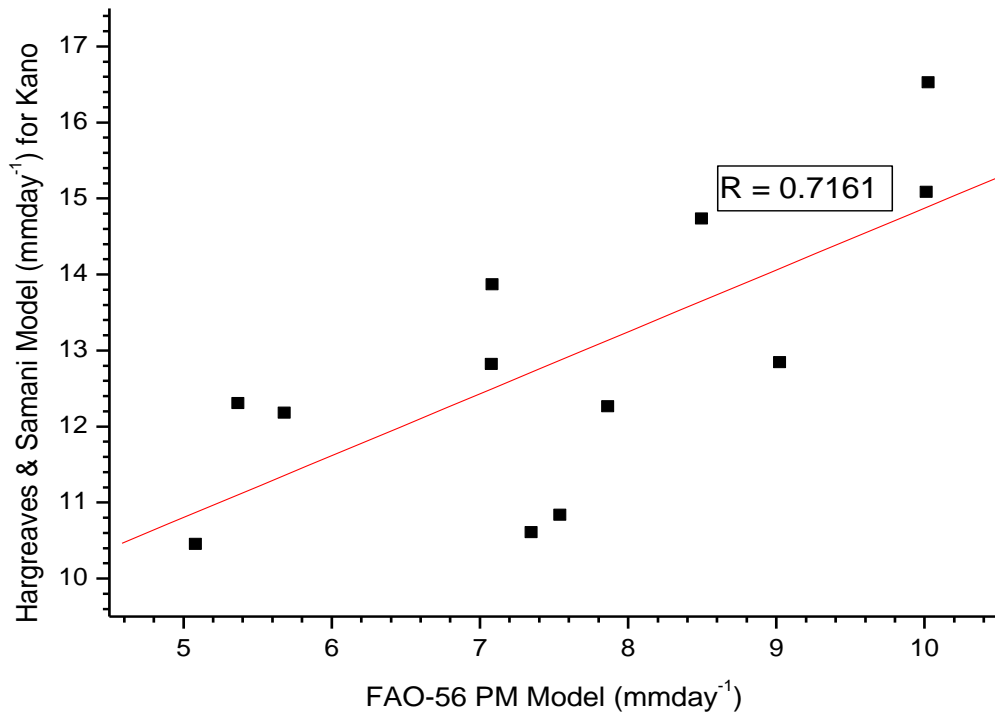
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Fig. 4. Fitted regression line of Priestley and Taylor model with reference FAO – 56 PM model

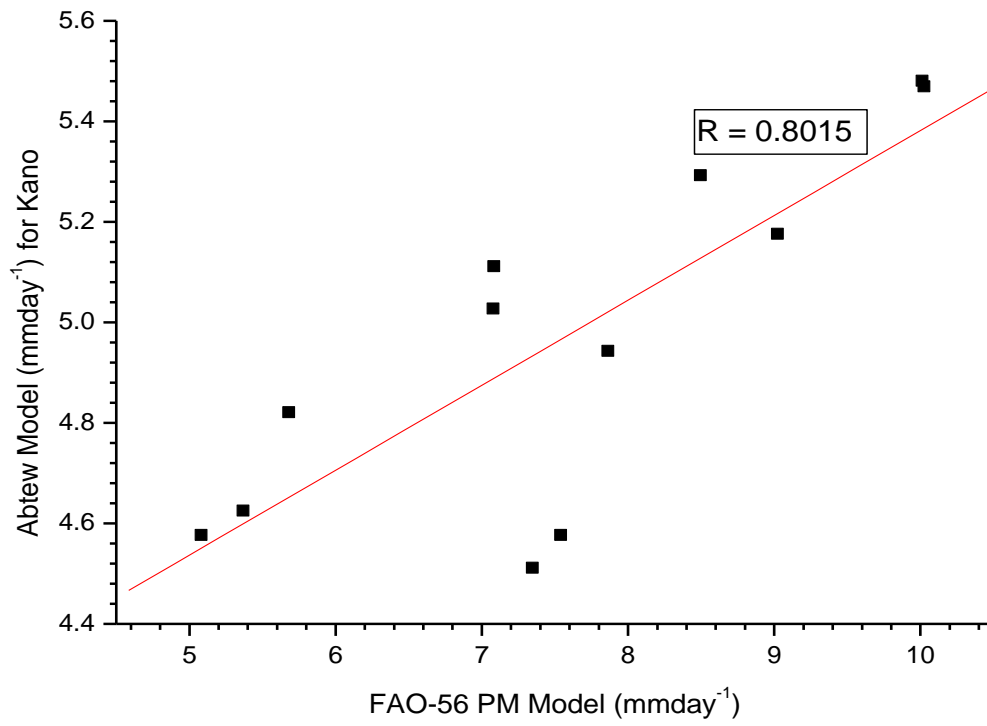


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Fig. 5. Fitted regression line of Makkink model with reference FAO – 56 PM model

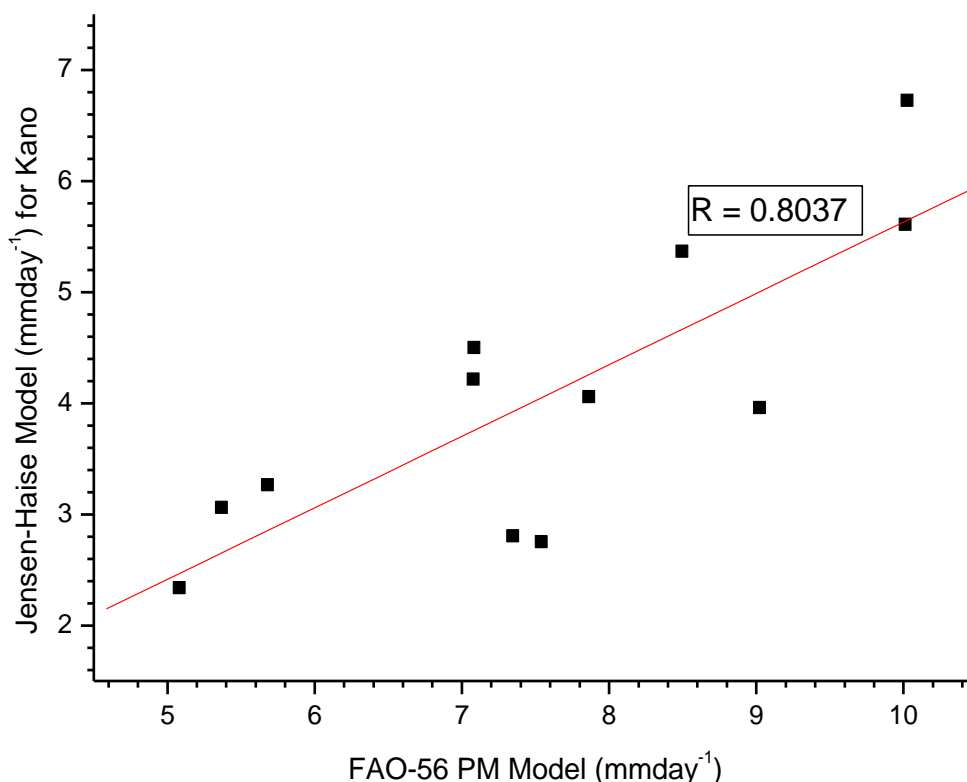


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332 **Fig. 6. Fitted regression line of Hangreaves and Samani model with reference FAO –**
333 **56 PM model**



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Fig. 7. Fitted regression line of Abtew model with reference FAO – 56 PM model



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Fig. 8. Fitted regression line of Jessen – Haise model with reference FAO – 56 PM model

The fitted regression lines obtained in the regression analysis using the reference FAO – 56 PM model and the computed models are shown on figure (3 – 8). The Blaney – Morin Nigeria model achieved the best fit resulting in correlation coefficient with 0.9790 showing a peak positive correlation between the Blaney – Morin Nigeria model and FAO – 56 PM models, followed by Jessen – Haise model with correlation coefficient with 0.8037. The lowest correlation coefficient is observed for priestley and Taylor model with 0.0841.

Table 1a. Statistical comparison between ET by FAO – 56 PM and other empirical models for Kano

| Models | MBE | RMSE | MAE | R |
|--------|---------|--------|--------|--------|
| BMNM | -1.4634 | 1.5078 | 1.4634 | 0.9790 |
| PTM | -1.9228 | 2.5784 | 1.9228 | 0.0841 |
| Mak | -3.2154 | 3.4875 | 3.2154 | 0.6615 |
| HSM | 5.3287 | 5.4833 | 5.3287 | 0.7161 |
| Abstew | -2.5819 | 2.9057 | 2.5819 | 0.8015 |
| JHM | -3.4948 | 3.6199 | 3.4948 | 0.8037 |

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The table 1a shows the different statistical indicators of RMSE, MBE, MAE and R which were carried out to verified the performance of the six models used in this study with the

reference FAO – 56 model and the results evaluated were used for ranking to ascertain the best model for the study area. The MBE values ranged from -1.4634 mm/day of the Blaney – Morin Nigeria model to 5.3287 mm/day of the Hangreaves and Samani model. The biasness which was indicated by Mean Bias Error (MBE) represents overestimation when it is positive and the negative sign indicates the underestimation. Based on the MBE, the Blaney – Morin Nigeria model has the least value with underestimation of 1.4634 mm/day in its estimated value and was reported the best. The RMSE values ranged from 1.5078 mm/day of the Blaney – Morin Nigeria model to 5.4833 mm/day of the Hangreaves and Samani model. Due to the least RMSE value of the Blaney – Morin Nigeria model (1.5078 mm/day) makes the Blaney – Morin Nigeria model performed best followed by the Priestley and Taylor model (2.5784 mm/day). The MAE values ranged from 1.4634 mm/day of the Blaney – Morin Nigeria model to 5.3287 mm/day of the Hangreaves and Samani model. Due to the least value of the MAE, it shows that the Blaney – Morin Nigeria model (1.4634 mm/day) performed best followed by the Priestley and Taylor model (1.9228 mm/day). Based on the high value of the correlation coefficient of the Blaney – Morin Nigeria model performed better with coefficient of 0.9790 (97.90 %) followed by the Hangreaves and Samani model with coefficient of 0.8037 (80.37 %). The overall results show that the Blaney – Morin Nigeria model performed better in term of MBE, RMSE, MAE and R.

Table 1b. Ranking of evaluated models as per statistical indication for estimating ET₀ for Kano

| Model | MBE | RMSE | MAE | R | Total | Rank |
|-------|-----|------|-----|---|-------|------|
| BMNM | 1 | 1 | 1 | 1 | 4 | 1 |
| PTM | 2 | 2 | 2 | 6 | 10 | 3 |
| MakM | 4 | 4 | 4 | 5 | 17 | 4 |
| HSM | 6 | 6 | 6 | 4 | 22 | 6 |
| Abs M | 3 | 3 | 3 | 3 | 12 | 2 |
| JH | 5 | 5 | 5 | 2 | 17 | 4 |

Table 1b shows the ranking of the models used in computing ET₀ tells which of the models serves as an alternative with the FAO – 56 PM model, this ranking of the selected models was done based on the statistical validation test of MBE, RMSE, MAE and r. The total ranks acquired by the different models were in the ranged of 4.00 to 22.00. The Blaney – Morin Nigeria model was found to performed better based on the total ranked acquired. So, it was found suitable for estimating ET₀ followed by Abstew model which came 2nd. Priestley and Taylor model was ranked 3rd, Makkink model and Jessen – Haise model were ranked 4th and Hangreaves and Samani model was ranked 6th. Thus, the Blaney – Morin Nigeria model was ranked 1st serves as a benchmark model for estimating ET₀ for this study area.

4. CONCLUSION

This study makes use of thirty one years monthly data of global solar radiation, sunshine hour, wind speed, maximum and minimum temperature and relative humidity obtained from the Nigerian Meteorological Agency (NIMET) to compute and compare six ET models with a view to ascertain the most suitable model that is capable of estimating ET in Kano situated in the Sahelian climatic zone of Nigeria, the FAO – 56 PM was used as the standard ET model. The result for this study shows that the highest value of ET was found in the month of April with 10.0256 mm/day and the lowest value of 5.0804 mm/day in the month of August. The Blaney – Morin Nigeria model was found most appropriate for computing ET as compared to other evaluated models in Kano based on the adopted statistical test carried out. This study provides information on evapotranspiration, if properly utilized, can provide correct estimates

395 of daily and monthly usage of water and therefore helps the irrigation managers in Kano and
396 those with similar climatic information with the important decisions of when water is to be
397 applied and the quantity of water to apply for the design, operation and management of
398 irrigation systems.

399

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407 **COMPETING INTERESTS**

408

409 Authors have declared that no competing interests exist.

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411 **AUTHORS' CONTRIBUTIONS**

412

413 This work was carried out in collaboration among all the authors. The data for the work was
414 sourced and analyzed by author DOA. Author SA and DOA supervised the work. The work
415 was drafted and edited by Author MKA. All the authors read and approved the final
416 manuscript.

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