

The Effects of Gravitational Wave Recoil on Black Holes

Abstract. In space, a black hole is a region where gravity is so strong that even light cannot escape. Because the substance is compressed into such a small area, the gravity is extremely intense. While a star is dying, this may take place. Furthermore, the asymmetric emission of gravitational waves that results from the merger of two black holes gives the merged system an impulse; this gravitational-wave recoil velocity can reach up to 4000 km/s, which is more than fast enough for the black hole to leave its host galaxy. After doing vast quantities of systematic literature research, one can see that much more research is required on the effects of gravitational wave recoil and its impact on the growth of the **supermassive black hole (SMBH)**. Most research makes the assumption that the black hole is stationary, which is problematic since recoil can be altered by the black hole moving in an opposite, identical, or parallel direction. The shape of the primordial globular cluster, the amount of mass in low metallicity systems, the impact of few body-black hole interactions on the emergence of the early globular structure, and other factors are all the subject of extensive research on the current methods for determining the characteristics of a black hole. In addition to considering the growth and evolution of the host galaxies of the host black hole, this review paper investigates the effects of gravitational recoil on three different types of black holes, namely **Massive Black Holes (MBH), Intermediate Black Holes (IBH), and SMBH**. **This paper suggests future research and identifies knowledge gaps, such as the knowledge gap regarding non-stationary black holes and the structure of the primordial globular cluster, where the current research methodologies and procedures regarding gravitational recoil in different black holes would require study.**

Keywords. Black Hole—Gravitation—Recoil—Universe—Intermediate Black Hole—Supermassive Black Hole

1. Introduction

Light cannot escape from a black because of its intense gravitational attraction. Due to matter being crammed into a small area; gravity is extremely strong. When a star is dying, this can occur. According to science, the tiniest black holes emerged during the creation of the universe. When the core of a massive star collapses in on itself, a stellar black hole is created. A supernova results from this situation. A star that explodes and sends a piece of itself into space is called a supernova. Supermassive black holes are thought to have formed at the same time as the galaxy they are in. Galactic bulges are known to include center black holes whose mass is closely associated with the star mass and bulge velocity dispersion.

In a hierarchical universe, galaxies are created by a series of mergers of sub galactic units. During this process, bulges combine and galactocentric black holes are expected to form. In these mergers, the beaming of gravitational radiation during the black hole collision's plunge phase might give the remnant a linear momentum kick or "gravitational recoil." If strong enough, this kick will completely evict the remnant from the galaxy and fill the interstellar void with roving black holes. This study examines the impact of gravitational recoil on black holes as well as the development and evolution of the host black hole's host galaxies. The combined system receives an impulse when two black holes merge because of the asymmetric emission of gravitational waves; the recoil velocity of these waves may reach up to 4000 km/s, which is more than enough time for the black hole to escape its host galaxy.

Due to episodes of black hole creation after a recoil event, the MBH occupancy fraction, however,

well adapted to pick up gravitational-wave signals from them. Many astronomical research, including the examination of nearby objects that are subjected to a black hole's gravitational attraction, provide enough indirect proof that black holes exist. The General Theory of Relativity provides a clear explanation for these situations (GR). The direct observation of a black hole's event horizon, which is its immediate surroundings, had never before been accomplished. The EHT has significantly addressed a substantial gap in our empirical knowledge with the publication of the first results in April 2019. The reason why it is important to do research on black holes is because Black holes serve as testing grounds for basic hypotheses that describe how the Universe functions on both the greatest and smallest scales (e.g., GR and Quantum Physics).

Although each of these theories is effective in its own domain, physicists are presently unable to develop a single, all-encompassing physical theory that would adequately describe the physics of black holes. Scientists can now directly resolve the spacetime conditions at the black hole border thanks to the EHT discoveries. Together with the fundamental scientific ideas, there are several aspects of plasma physics that remain unclear. Beyond the event horizon, the characteristics of the hot gas that surrounds and is drawn into the black hole are not completely understood. However, because this blazing plasma creates radiation-caught radio telescope arrays, it is essential to comprehend these characteristics in order to interpret black hole photographs. The features and behavior of these extreme settings will be better understood thanks to EHT observations of the incandescent hot plasma that effectively reveals the geometry of spacetime surrounding the black hole.

The three basic types of black holes are broken down and analyzed in this review study, along with the methodology used to determine each black hole's gravitational wave recoil. It makes suggestions for further study and points out gaps, such as the knowledge gap regarding non-stationary black holes and the structure of the primordial globular cluster, where the existing research methodologies and procedures pertaining to gravitational recoil in various black holes would require study.

1. Gravitational Recoil in Massive Black Holes (MBHs)

Gravitational Redshift is the process of the photons leaving the gravitational well which leads to loss of energy. This in turn leads to decrease in frequency and increase in wavelength also known more generally as Redshift in general relativity. Gravitational Redshift in galaxies leads to nearby galactic system mergers and thereby their corresponding black holes. The black holes will ultimately merge if stellar dynamical and gas processes push the binaries near enough, which is less than or equal to 0.01 picometer. At that point, energy and angular momentum losses will eventually be outweighed by gravitational radiation. Such events lead to the creation of a Laser Interferometer Space Antenna. Gravitational waves also decrease the binary's net linear momentum in pairings of unequal masses and give the system's center of mass a kick velocity.

Extreme mass ratio inspirals (EMRIs), galactic binaries, and huge black hole binaries are the principal generators of low frequency gravitational waves. The coalescence of black hole binaries following a merger is also one of the sources of a low frequency gravitational wave. For a linear system, the lowest order loss arises from the interference between quadrupole and octupole radiation which leads to the dominant gravitational recoil. The MBH may be ejected from its host galaxy in an asymmetric configuration where the recoil velocity is more than a few hundred kilometers per second. A powerful field effect that depends on the binary system's lack of symmetry is gravitational radiation recoil. In a quasi-circular in-spiraling orbit, the lighter hole travels more quickly and emits more gravitational radiation in the forward direction. As a result, the binary veers off course and expels momentum in the direction of the lighter mass's motion.

$$v_{cm} = 1480 \text{ km s}^{-1} \frac{(g)}{f_{max}} \left(\frac{2GM/c}{r_{isco}} \right)^2$$

A comparable-mass system's innermost stable circular orbit, or r , swings inward in r_{isco} relation to its test-mass limit. The fact that the recoil varies for equal-mass non-rotating holes is crucial to keep in mind. A Kerr black hole is a rotating black hole which possesses angular momentum. According to

more recent estimates using the perturbation theory, the recoil velocity can easily reach between 100 and 200 km/s, although it is highly improbable to go beyond 500 km. Because of their gravitational ties to the hole, stars within its gravitational field, do not

$$R_{BH} = \frac{GM_{BH}}{\sigma^2}$$

contribute to dynamical friction. The flattening of the inner stellar density profile is also brought about by the original MBH binary's demise, in which energy from the binary is transferred to the galaxy's core stars through dynamical friction and three-body interactions. The decay duration is dependent on the inner star density since the friction largely occurs at tiny radii. For instance, the decay durations rise by a factor of 3 if we double the isothermal sphere's core radius. This ambiguity in the decay period won't change our results given the uncertainties in the recoil velocity. Energy is conserved in the absence of dynamical friction, and an ejected MBH will arrive at its apocenter when the exponential dependency appears due to the potential's logarithmic nature. Yet, owing to dynamical friction, the hole loses a little portion of its orbital energy with each transit through the galactic nucleus. The MBH's continued orbit around the sun is assumed in the study above. Nonetheless, it is possible that the hole may gain angular momentum after leaving the nucleus (for instance, if the galactic potential is triaxial) and that this would change the orbital decay's time frame. The degradation duration in this scenario cannot be accurately estimated. Early periods are prone to large mergers; hence it is anticipated that many binary MBH systems will emerge at that time. It is yet unknown if halo massive mergers inevitably result in the coalescence of their MBHs or if the binaries "stall" before the gravitational wave back-reaction becomes significant. In the most recent research, a variety of plausible strategies that could help prevent such stalling have been proposed¹.

When accounting for the satellite's tidal stripping's effect on the orbital decay timescale, it is feasible to demonstrate that satellites will only merge with the core galaxy on timeframes shorter than the Hubble time in the event of massive mergers. In modest mergers, tidal strip ping may cause the satellite MBH to stray in the halo, too far from the remnant's core for a black hole binary to develop. For galaxies with average kick velocities of 50–75 km/s or a few hundred km/s are adequate to unbind the hole or move it far enough away from the nucleus such that the decay time resulting from dynamical friction is equivalent to the Hubble time.

According to this, MBHs with masses $10^6 M$ may be similarly uncommon in MBH-j late-type spiral galaxies or dwarf galaxies (applying the connection). "It is crucial to emphasize that even if galaxies don't have a central MBH right now, they could have in the past. Hence, the lack of MBHs in shallow potential wells might be caused by recoil during MBH coalescence rather than necessarily implying ineffective MBH generation. Furthermore, take note that the low-mass black holes predicted to dominate the LISA gravitational-wave signal from MBH-MBH coalescence are ones that are preferentially influenced by gravitational recoil. If such MBHs are often ejected, this may reduce the number of sources that LISA can identify. Galaxy mergers are a major source of fuel for MBHs; hence the prospect of off-nuclear quasar activity is a logical consequence of gravitational recoil. With radio observations of AGNs, the effects of gravitational recoil could be particularly noticeable. Others contend that by altering the spin axis of the MBH and hence the direction of the radio jet, MBH coalescence may leave its mark on the morphology of radio galaxies"².

By shifting the radio-loud AGNs from the galaxy's core, gravitational recoil may have an impact that is comparable to importance. This might seem as a flat spectrum radio core separated from the galaxy's optical core and a jet or lobe that is nonetheless symmetrical around the core. In contrast to optical quasars, contamination from the host galaxy is less of an issue with radio measurements, and extremely long baseline interferometry enables accurate localization of the radio emission. The genesis of off-nuclear ultra luminous X-ray sources in neighboring galaxies may be related to gravitational recoil. One explanation for these sources is that they are intermediate-mass black holes (IMBHs), which are thought to originate in globular clusters through recurrent black hole mergers and

¹ Mateo, M. 1998, ARA&A, 36, 435

² Merritt, D., & Fridman, T. 1996, ApJ, 460, 136

are accreting close to the Eddington limit. Nonetheless, it is likely that the gravitational rocket will prohibit significant growth through hole mergers in the shallow potential well of a globular cluster since even coalescences with mass ratios as little as 0.1 can result in kick velocities greater than the cluster's escape velocity.

It should be emphasized that during the core collapse of young star clusters, an IMBH might potentially emerge by stellar mergers as opposed to compact object mergers. The possibility of MBHs to expand by gas accretion from uncommon, less massive seeds, such as IMBHs created by the collapse of Population III stars, isn't necessarily constrained by the gravitational rocket. While the merger of two (mini) halos housing black holes is a rare event at these extremely early epochs, seed holes that are as uncommon as, for example, the 3.5 σ peaks of the primordial density field would emerge mostly in isolation. When there are more halos hosting MBHs, a considerable number of MBH binary systems may arise. At that time, the usual host will be larger and lower in the merger hierarchy, making radiation recoil less disruptive.³

2. Gravitational Recoil in Intermediate Black Holes (IBHs)

Supermassive black holes (SMBHs) with masses more than $10^6 M$ and stellar-mass black holes (BHs) with masses less than $10^2 M$ and greater than are both supported by a wealth of observational data. There are observational clues for intermediate-mass black holes (IMBHs) as well, with masses less than $10^2 M$ and more than $10^2 M$, while the existence of a third black hole class is still up for question. Ultra luminous X-ray sources (ULXs) in early star-forming areas may best be explained by these IMBHs, which may form inside dense star clusters. While stellar-mass BH collisions may be a more likely growth mechanism in systems with a lengthy relaxation period, runaway star collisions appear to be the dominant IMBH production pathway within crowded systems. Here, a naturally occurring, heavier-than-average black hole, presumably a stellar remnant with a mass of 250 M , serves as the first seed IMBH. The original seed then traps stellar-mass BHs, and the ensuing binary hardens as a result of interactions with additional stellar-mass objects. Four Body Collisions to direct more BHs to the expanding IMBH even if the interactions run the danger of ejecting the black hole before considerable growth occurs. Pop III stars that are significantly that are significantly more massive might directly produce IMBHs.

It has been predicted that a Pop III protostar with a mass of $10^5 M$ will be gravitationally unstable and collapse to an IMBH before it ever reaches the main sequence. The initial stellar mass function (IMF) and highly speculative aspects of zero metallicity stellar evolution are also factors that affect the likelihood of an IMBH emerging from such a large Pop III star. These hypotheses imply that BHs are more massive in a proto globular cluster setting than they are in a more recent formation. Nevertheless, Pop III star formation is believed to occur in dark matter over densities at z , and only the largest globular clusters are anticipated to be contained in a sufficient amount of dark matter over density to support Pop III creation. Regardless of how the IMBH develops, it is actively active during the first 0.5 Gyr following development. The early environment around an IMBH in a globular cluster is particularly rich in BHs as a result of mass segregation. There are still enough of these BHs after few-body interactions with the IMBH, even though many of them are immediately expelled, for the IMBH to undergo tens to hundreds of mergers with BHs in the original globular cluster system. Within the first 0.5 Gyr after development, the IMBH is functionally active regardless of how it evolves. Because of mass segregation, the early environment around an IMBH in a globular cluster is exceptionally rich in BHs. Even if many of them are instantly ejected, there are still enough of these BHs to allow the IMBH to undergo tens to hundreds of mergers with BHs in the original globular cluster system.

The fact that binary black hole systems substantially emit linear momentum in the form of gravitational waves during the plunge phase of the inspiral is one of the most intriguing findings of

³ Murgia, M., Parma, P., de Ruiter, H. R., Bondi, M., Ekers, R. D., Fanti, R., & Fomalont, E. B. 2001, *A&A*, 380, 102

general relativity for structure development. This radiation has a general "kick" velocity of up to 4000 km/s and is produced as a direct result of an imbalance in the orbital arrangement. Even though they are uncommon, kick speeds of this magnitude are dynamically fascinating for galaxies at the current epoch and high redshift. No matter how an IMBH forms, the biggest challenge may be to understand how a globular cluster maintains them in the face of a constant barrage of gravitational wave kicks from mergers with other black holes. Even typical kick velocities (200 km/s) are interestingly large when compared to the escape velocity of an average globular cluster (50 km/s). Naturally, the formation mechanism itself must be able to explain these huge kicks if IMBHs are produced by stellar-mass black hole mergers. Less than 33% of the time, given the distribution of black hole masses inside a canonical globular cluster, an IMBH of less than 1000 M_{\odot} is retained.

While the overall number of mergers is dominated by a large number of lower mass black holes, stellar-mass black hole ejections are dominated by a small number of rare mergers, and as the IMBH mass grows, ejections are more likely to be generated by the most massive stellar-mass black holes. Using the shallower and more realistic Belczynski black hole mass function, with just 30% expelled, it is simpler to keep an IMBH of less than 1000 M_{\odot} . The computations should predict that the IMBH is continually merging with m black holes, however this is not the case. They should also predict that $m_{comp} = 80 M_{\odot}$ the dynamical ejections may be lower than anticipated. Time affects both the quantity and density of black holes of various masses⁴. According to research, keeping IMBHs around throughout the onslaught of BH mergers anticipated in a fiducial early globular cluster is difficult. When the interacting BHs are chosen from a suitable distribution of spins, orientations, and mass ratios, we are unable to uncover any scenario that ensures 100% retention for IMBHs up to 3000 M_{\odot} . The retention likelihood is higher, nevertheless, the larger the original IMBH seed. This would suggest that any IMBH found in globular clusters today likely came from an early stellar runaway channel.

The findings from this study may be applied to examine various IMBH production pathways. For instance, a single cluster can contain numerous runaways, resulting in many IMBHs, when the binary fraction is above 10%. The two heaviest of these IMBHs will move towards the cluster's core and unite there in a matter of minutes (1 Myr). Such IMBHs will join into the cluster, but since their masses are almost equal and they most likely have high spins, they will break out. This prevents the cluster from producing a seed, barring the occurrence of a third runaway of sufficient mass. The issue is that, as we have seen, the third runaway is frequently far less big and challenging to hold onto. The lower the spin, the lower the mass, the better the retention for the IMBH. The same processes could take place in other galaxies, even though our attention has been on IMBHs in the population of Galactic globular clusters. Young star clusters are regularly discovered nearby, but extragalactic ULXs, which may be fueled by $10^2 M_{\odot}$ IMBHs, are not detected within them. "Nevertheless, keep in mind that the star clusters linked to ULXs are not always the dense stellar systems required by the IMBH formation models under consideration. As they would combine with the most massive black holes first, if such IMBHs did develop inside the surrounding clusters, they may be expelled through gravitational wave kicks emanating from stellar-mass black hole mergers"⁵.

It is unclear how an IMBH would pick up a partner on its journey out of the cluster, and it seems improbable that it would keep a stellar companion near enough to overflow its Roche lobe. But this would explain their departure from the cluster center, not why ULXs are accreting sources. Yet, a few-body Newtonian dynamical kicking may be used to expel an IMBH with a stellar partner from the host cluster, hardening the binary until it starts accreting. The effects of these high recoil velocities might potentially have an impact on SMBH assembly. At redshifts $z \geq 12-20$, $10^3 M_{\odot}$ Population III star remnants are the most plausible candidates for SMBH seeds. According to predictions, these relic seeds will develop in the middle of low-mass dark matter haloes ($4 \times 10^6 M_{\odot}$). The seed black holes

⁴ Bullock, J. S., Kolatt, T. S., Sigad, U., Somerville, R. S., Kravtsov, A. V., Klypin, A. A., Primack, J. R., & Dekel, A. 2001, MNRAS, 321, 559

⁵ Erwin, P., Graham, A. W., & Caon, N. 2004, in Carnegie Obs. Astrophys. Ser. 1, Coevolution of Black Holes and Galaxies, ed. L. C. Ho (Cambridge: Cambridge Univ. Press), 12

eventually combine as they descend to the center due to dynamical friction as dark matter halos merge hierarchically to build the galaxy. Moreover, it could be challenging to keep seed SMBHs in high-redshift low-mass dark matter halos with kick velocities in the range of 102 to 103 km.

3. Gravitational Recoil in Supermassive Black Holes (SMBHs)

Supermassive black holes (SMBHs, $\geq 10^6 M_{\odot}$) have long been thought to be the likely source of quasar central engines. They are currently known to be common in the centres of both active and dormant galaxies, according to observations. There is a lot of evidence connecting SMBHs with the dynamical characteristics of their host galaxies, suggesting that the two may have developed together. The mass of their host galactic bulges, which is determined by their brightness, is strongly associated with the measured masses of the SMBH. Moreover, $M_{\text{BH}} \propto \sigma^4$, a substantial link between star velocity dispersion in the bulge and SMBH mass, has been discovered. Recent investigations have discovered that if dwarf galaxies' compact nucleus is thought to be the equivalent of SMBHs in giant galaxies, a comparable link may exist between them and big galaxies. According to these results, SMBHs contain a lot of knowledge regarding the creation and development of structure in the universe. The specifics of SMBH accretion and how it pertains to galaxy development have been extensively studied theoretically in this context.

The black hole (BH) is assumed to stay stable at the galaxy's centre in almost all of these investigations, though. Although the known sample only includes local galaxies and so, lays minimal limits on the dynamics of SMBH across the lifetimes of galaxies, this is a fair assumption given the observed prevalence of central compact objects in galaxies. Yet, gravitational-wave (GW) recoil can give the resulting combined BH a significant kick if two SMBHs coalesce after a significant galaxy merger. Asymmetrical emission of gravitational waves causes a net linear momentum flow at merger when the merging black holes (BHs) have different masses or spins, which causes the combined BH to recoil in the opposite direction. Up until recently, the significance of this effect as an astrophysical phenomenon was largely unknown, despite the fact that it has long been recognized as an intriguing relativistic phenomenon. The best approximative estimations indicated that kick velocities were most likely to be low, a few hundred kilometers per hour or less. Findings from simulations employing complete numerical relativity have shown that kicks up to 4000 km/s are achievable with specific mass and spin combinations if large BH spins are taken into account.

The consequences of enormous recoil kicks would obviously be significant, given these velocities easily surpass the escape speed of any known galaxy. The active galactic nucleus (AGN) feedback created, the pace of fuelling, and the location of the BH in the galaxy will all vary. For instance, the Bondi accretion model, which is frequently used in simulations, states that the accretion rate is inversely related to the accretor's cubed velocity. The spin parameters, spin alignment, and mass ratio of the merging BHs all have a significant impact on the velocity of recoil kicks. These quantities' distributions throughout the population of merging galaxies are quite hazy. The recoil distribution may be biased towards in-plane kicks as a result of torques in a circumbinary gas disc that align the BH spins with the disc orbital plane (and consequently low kick velocities).

According to calculations, recoil kick velocities have probability distributions that assume BH mass ratios and spin orientations are distributed randomly. By taking a range of kick inclinations into account, we enable for both aligned and random spins. One strategy to limit these distributions would be to look for GW recoil signatures in the future. Several of the observational characteristics we may anticipate from these sources, such geographically and kinematically offset quasars, are said to be present, according to research. They may be wandering SMBHs on bound paths that could drastically alter galaxy structure, or SMBHs that are expelled from their home galaxies and carry an accretion disc along with them. We may presume that the percentage of offset quasars is quite modest because no known quasar has been definitively recognized as such. In a similar vein, research reveals that the $M_{\text{BH}}-\sigma^*$ relation's restrictions on ejected BHs. She came to the conclusion that SMBH ejection could not have been a very frequent occurrence for the majority of the history of the universe since

otherwise, we would see much more dispersion in BH-galaxy interactions⁶.

Volonteri draws attention to the fact that mergers were more frequent and recoil kicks, which are independent of absolute mass, might have more readily evicted BHs from the comparatively tiny host galaxies in big haloes at high redshift. A series of N-body simulations that simulate the motion of a kicked SMBH in a stellar potential have been used in studies on GW recoil. According to research, BHs in constrained orbits feature low-amplitude oscillations in the star core and extended oscillation timescales of up to 1 Gyr. These oscillations tear out a substantial star core, sometimes bigger than the cores that binary SMBHs are predicted to create. BHs on constrained orbits have extended oscillation time scales, according to study using GADGET-2, and recoil events can lead to considerable asymmetry in galaxy discs. We do see, however, that any galaxy with a recoiling SMBH would by definition have just experienced a merger, resulting in asymmetric shape. The tool of choice in most N-body simulations software's is GADGET-2 which revolves around the Λ CDM model. GADGET-2 is a cutting-edge TreePM programme that performs better than the traditional PP approach and incorporates a Smoothed-particle hydrodynamics (SPH) method for modelling gas. G2X, a hardware-accelerated version of GADGET-2 that runs 10 to 20 times faster than the original version thanks to the use of GPGPUs and CUDA technologies.

Since the 1970s, when the first N-Body simulations were conducted, there has been an ongoing endeavour to create effective cosmological modelling software. The GPU's memory severely restricts it to simulations on the order of 10 particles, which is a significant impediment for researching real-world systems. An N-Body solution like the one created for the ART code is used by the more recent code RAMSES. But it also has a hydrodynamical solver based on the second-order Godunov approach, a cutting-edge shock-capturing technique that is known to precisely calculate the fluid component's thermal history. Another contemporary programme is VINE, which was developed in Fortran95 and has a modular design with various integrators, individual time steps, SPH, free or periodic boundaries, and support for GRAPE hardware. A third particle species can be added in addition to the N-Body and SPH particles to simulate enormous point particles that might accrete neighbouring SPH or N-Body particles (e.g., stars in a molecular cloud).

Depending on the simulation type, it outperforms GADGET-2 by a ratio of 2 to 5. The size of the simulations and the number of processors employed are both constrained to a single computational node since it is parallelized with OpenMP. A key application of this approach is to think about the observational fingerprints that recoiling BHs may give so that their existence could be explicitly established. GW recoil has not been unequivocally recorded in any astronomical setting. Via offsets in either physical space or velocity space, a stationary core BH might be separated from a visible recoiling BH, i.e., one with considerable accretion luminosity. "As a significant portion of the orbital period is spent at turnaround, BHs⁷ with a resolvable spatial offset from their host galaxy is statistically more likely to have a relatively low velocity. Similarly, when there is a modest spatial offset from the galactic centre, the highest velocity offsets will occur either shortly after the recoil event or on successive crossings of the BH across the galactic disc".

The size of the accretion disc that the recoiling BH brings with it determines the duty cycle for the earlier kind of event; faster recoil speeds lead to smaller ejected discs and shorter duty cycles. The most likely mechanism for the wandering BH to become visible again after this disc is used up is by accreting matter during successive passes through the galactic disc, perhaps producing a quasi-periodic signal like knotted or twisted jets. As a result, we distinguish between two different categories of "recoiling quasars": the former is classified as "off-centre quasars," while the latter are classified as "Disc-crossing quasars," with the latter being largely velocity offset sources. But keep in mind that there is no exact correlation between quasar velocity offsets and disc crossings, or between spatial offsets and quasars that are "off-centre." Off-centre quasars frequently have a substantial velocity offset because ejected quasars are sometimes only observable for a brief period of time while

⁶ Favata, M., Hughes, S. A., & Holz, D. E. 2004, *ApJ*, 607, L5 (Paper I)

⁷ Lokas, E. L., & Mamon, G. A. 2001, *MNRAS*, 321, 155

they are still carrying an accretion disc. Similar to this, numerous "disc-crossing" occurrences take place when the BH slows down and returns to the galaxy's centre, therefore their velocity offsets will be minimal. Remember that in us runs all BHs radiate at their Eddington luminosities with the exception of those in Model D, and that the word "quasar" is used loosely here to refer to a source with visible accretion activity.

We have thought about SMBH accretion without requiring that the SMBH stay still at the galactic centre. Instead, it was supposed that the SMBH⁸ was "kicked" away from the centre at a speed of 100 to 1000 km/s, which can happen as a result of GW recoil after a BH merger. Remarkably, the kick velocity, v_k , has minimal impact on how much mass k the SMBH picks up as it travels around the galaxy. In every instance, the fractional SMBH increase, M/MBH , is around 10% from the recoil kick until the point where the BH settles back to the galactic centre. Moreover, the total mass of the BH is not greatly affected by bursts of accretion that occur during successive disc crossings. The constancy of M/MBH suggests that GW recoil is a useful tool for SMBH growth self-regulation. There may be significant expansion if the SMBH stayed still at the galactic center. Nevertheless, they depend on the specifics of the gas physics and may alter significantly in different galactic settings. Its growth might be controlled by more traditional mechanisms like energy or momentum feedback. In contrast, the characteristics of the merging SMBH progenitors are the only factors affecting GW recoil.

It's also noteworthy to notice that these two growths regulation strategies complement one another because other feedback mechanisms will come to an end after the recoiling SMBH has used up its supply of bound gas. Recoiling BHs might be compatible with the observed $MBH-\sigma^*$ connection even if big recoils $\lesssim v_{esc}$ are not uncommon events. This is because it is possible that both wandering and stationary SMBHs self-regulate their masses. The second result is predicated on the fact that recoiling SMBHs still have a low escape fraction; otherwise, we would more dispersion in the $MBH-\sigma^*$ relation or galaxies in the nearby universe without a core SMBH, which are not found. The frequency of substantial recoil kicks clearly determines the significance of GW recoil in the development of SMBHs. Because the recoil kick distribution depends on the poorly understood spin and mass ratio distributions of the progenitor BH binaries, estimating this is challenging.⁹

Analysis

The cosmos is affected by the possibility that a middle-massive black hole may be moved by a gravitational wave recoil. Due to their gravitational effect on the local environment, black holes produce space wind, also known as space weather or cosmic winds. This is problematic because if a black hole were to move, the stars developing around it would be ejected in large quantities of material in many directions. High levels of neutrinos, which are hazardous for life's ability to thrive because of their size, are released by the moving black hole. On a daily basis, humans encounter a lot of neutrinos from the sun, but those emanating from black holes are much more numerous and cause radioactive problems for items nearby. The unfavourable effects include the formation of a roaming black hole, which profoundly changes the development and growth of any potential life surrounding it as well as the evolution and growth of the stars it draws towards it while it is roaming.

Future Directions

Since most study assumes that the extremely large black hole is stationary, research topics include the relationship between a moving black hole and the influence produced to it by gravitational recoil. An interesting solution to the IMBH problem would be solving the three-body scattering simulations with a gravitational recoil as well as the correct tracking of the black hole population. The current methods for determining the characteristics of a black hole are generalized, such as the shape of the primordial

⁸ Volonteri, M., Haardt, F., & Madau, P. 2003, ApJ, 582, 559

⁹ van der Marel, R. P. 2004, in Carnegie Obs. Astrophys. Ser. 1, Coevolution of Black Holes and Galaxies, ed. L. C. Ho (Cambridge: Cambridge Univ. Press), 37

globular cluster IMF, the amount of mass low in low metallicity systems and its impact on the black hole IMF, and the part that few body-black hole interactions play in the emergence of the early globular structure. To more accurately forecast and comprehend the aforementioned events, further study in the techniques is needed. To better understand the retention rates of Intermediate Massive Black Holes, using high-resolution cosmological N-body simulations, one should investigate black hole retention and potential kick suppression mechanisms at the low-mass end of the halo mass function. The software used for solving N-body simulation in Supermassive Black holes is GADGET-2 that comes with its own disadvantages, a major research topic would be increasing the speed of the computation as the software such as Vine is 2 to 5 times faster than GADGET-2 depending on the simulation type.

Conclusion

The black hole is assumed to be stationary in most research. While in the case of Kerr Black holes, it may be rotating but it may not necessarily be moving. This is problematic because if the black is not stationary, it may move either in the direction of the gravitational wave's recoil or away from it. If it moves away from it, however, the displacement is much smaller than if it moves with it or if it were stationary. The shape of the primordial globular cluster IMF, the amount of mass low in low metallicity systems and its effect on the black hole IMF, and the role that few body-black hole interactions play in the emergence of the early globular structure are some examples of the current methods for determining the characteristics of a black hole that are generalized. The software that is used to solve N-body simulations is GADGET-2 which comes with a lot of disadvantages. The GPU's memory in GADGET-2 severely restricts it to simulations on the order of 10 particles, which is a significant impediment for researching 6 real-world systems.

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