

Design, Simulation and Optimization of PZT-5A Cantilever Piezoelectric Pressure Sensor

ABSTRACT

Aims: The main aim of this research work is

- To design a mathematical model of the sensor and validate with the 3D model simulation of the sensor in COMSOL Multiphysics simulator and
- To optimize the sensor for maximizing its sensitivity.

Study design: In the methodology, we design and utilize PZT-5A piezoelectric in shear mode as the piezoelectric is attached on a cantilever structure. The various factors affecting the sensitivity of the sensor are investigated after validating the mathematical model with the simulated values.

Place and Duration of Study: This study is done in the Department of Electronics and Communication Engineering, Rajiv Gandhi University, Arunachal Pradesh at COMSOL Simulation Laboratory during 2022 to 2023.

Methodology: In this study, a cantilever structure is considered for the mechanical structure. The stress distribution on the structure is calculated for the applied pressure range from 0 to 1000 Pa. Later, the output voltage of the sensor is calculated. This mathematical model is validated with the COMSOL multiphysics simulator. The optimization of the sensor is done in mathematical tool with maximizing function after providing the conditions.

Results: The maximum stress on the sensor structure occurred near the clamped part of the cantilever. The calculated and simulated output sensitivities of the PZT-5A piezoelectric based pressure sensor are 1.6021 mV/kPa and -1.046887 mV/kPa respectively.

Conclusion: We conclude that the PZT-5A piezoelectric based pressure sensor has a linear output with negative gradient as the stress induced on the structure is tensile stress. The various parameters that affect the sensitivity of the sensor are found to depend on the shape and size of the cantilever structure, Poisson's ratio and Young's modulus, piezoelectric voltage coefficient and piezoelectric material thickness.

Future Scope: In future, this study can be extended by taking different shape and size of the cantilever. The different modes of piezoelectric and different materials may be another future scope of this study.

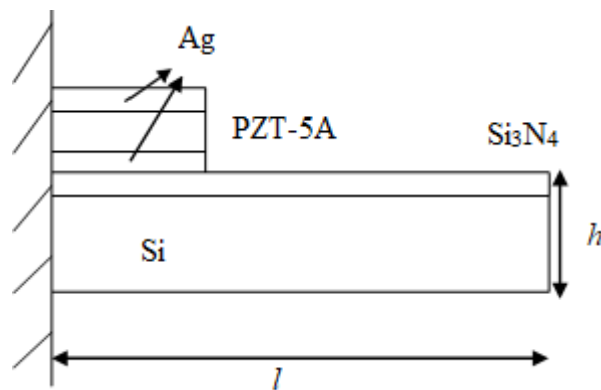
Keywords: Flexural Rigidity, Linear, Sensitivity, Stress, Voltage Coefficient.

1. INTRODUCTION

Pressure sensor becomes a very promising device because of its sensitivity and measurement for the pressure of gases or liquids of any system. The pressure sensors such as piezoelectric, piezoresistive, capacitive, inductive, and optical sensors have different sensing mechanisms. Among these sensors piezoelectric pressure sensor don't require any input voltage to the sensor. Nowadays, there are various applications of pressure sensor in, namely 1. Automotive systems: inertial brake lights, car security systems, and air bag systems, rollover detection, electronic door locks, 2. Aerospace: wind tunnel instrumentation, sensors for fuel efficiency and safety, micro-satellites, control systems, inertial guidance systems with micro-gyroscopes, accelerometers, 3. Medical services: disposable blood pressure monitors, respirators, lung capacity meters, controlling medical procedures,

25 apparatus for kidney dialysis, 4. Microbioanalytical systems: capillary electrophoresis and
26 biochip, manufacturing automation, instrumentation, 5. Communications: fibre optic
27 couplings and optical switching, RF relays and switches, tunable resonators, 6. Consumer
28 goods: computers and watches, sensors for exercise equipment, washers with adjustable
29 water levels, athletic footwear with automated cushion control, and 6. Environmental
30 monitoring and control: moisture or humidity, control in water volume[1-2][4][13]. They are
31 also used in energy harvesting and vibration sensing [6-7][9]. The various advantages of
32 piezoelectric pressure sensor are that the sensor can retain to have low power consumption,
33 more sensitive to input variation, cheap cost of production, enhanced performance &
34 reliability, able to replace bulky parts of traditional electronic appliances, improved
35 reproducibility. Piezoelectric pressure sensor can be used in Internet of things (IoT) devices
36 for improvising the life span of the battery used in IoT.

37 Piezoelectric materials usually exhibit different piezoelectric coefficient according to their
38 modes of operation. The most common structure used in the piezoelectric pressure sensors
39 are cantilever, bridge and diaphragm. The cantilever piezoelectric pressure sensor is shown
40 in fig. 1.



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Fig. 1: Cantilever Piezoelectric Pressure Sensor.

43 The piezoelectric output and stress are mutually correlated. The sensing layers are positioned
44 close to the cantilever's fixed edge as maximum stress occurred at the clamped area of the
45 cantilever. The PZT-5A and its composites are used in thin film deposition and utilized for
46 different applications [3][8-10][12]. The optimization of the sensor is also very important to
47 maximize the performance with higher sensitivity [5].

48 This work is organized as follows: in section 2, we consider material and design
49 methodology to describe the mechanical modeling and electrostatic modeling used in the
50 mathematical modeling of the sensor. In section 3, the COMSOL multiphysics simulator's 3D
51 studies of the designed sensor structure and its design structure are described and the
52 numerous factors impacting the sensitivity and optimization of the sensor are presented and
53 analytically compared for the mathematical analysis outputs and 3D analysis outputs. Finally
54 we conclude the work.

55 2. MATERIAL AND DESIGN METHODOLOGY

56

57 Applying the pressure from 0 to 1000 Pa with 100 Pa step size, the design model of a
58 cantilever structure with PZT-5A as the sensing layer is simulated in COMSOL multiphysics
59 simulator. The dimensions of the 3D model of the proposed PZT-5A piezoelectric pressure

60 sensor are tabulated in table 1. Whereas, the materials properties used in PZT-5A
61 piezoelectric pressure for this study are tabulated in table 2.

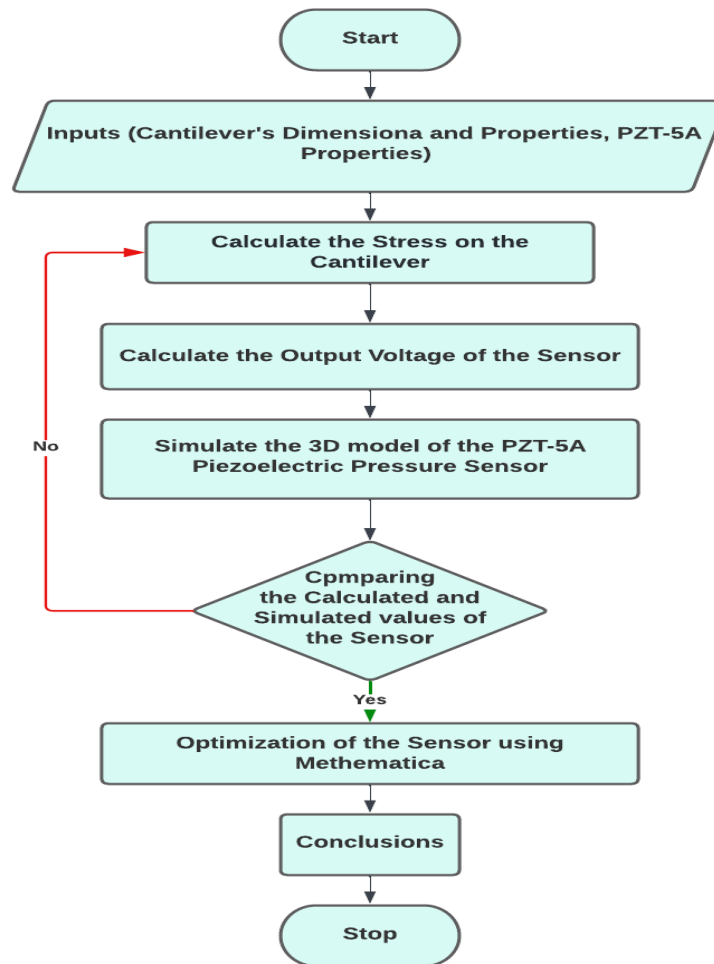
62 **Table 1: Dimension of the 3D structure of the sensor.**

Material	Si	Si ₃ N ₄	Ag	PZT-5A
Length	200 μm	200 μm	50 μm	50 μm
Breadth	50 μm	50 μm	50 μm	50 μm
Thickness	50 μm	3 μm	3 μm	10 μm

63 **Table 2: Material properties used in PZT-5A piezoelectric pressure sensor.**

Material	Si	Si ₃ N ₄	Ag	PZT-5A
Density	2320 kg/m ³	3100 kg/m ³	10500 kg/ m ³	7950 kg/ m ³
Young's modulus	160 GPa	250 GPa	83 GPa	79 GPa
Poisson's ratio	0.22	0.23	0.37	0.34

64
65 In this study, a model of the sensor is proposed and the mathematical model of the sensor is
66 developed in two steps, i.e. Stress on the cantiliver and Voltage on the surface of the PZT-
67 5A. Secondly, the 3D model of the senosr is simulated and the mathematical model is
68 validated by comparing the simulated and calculated values. Next, the model is optimized for
69 the sensitivity to be maximized. The work flow of this study is illustrated fig. 2.



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Fig. 2: The work flow of this study.

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2.1 Mathematical Model

75 As mentioned before, the mathematical model has two sections namely, mechanical model
76 and electrostatic model.

77 In mechanical model, the stress on the cantilever surface is calculated and find the position
78 where the maximum stress occurs. Let us consider a uniformly load or pressure (P) is
79 distributed on the surface of the cantilever as shown in fig.1. The mathematical expression for
80 conservation of moment on for the cantilever system is [14-16].

$$81 \quad -EI \frac{\partial^2 w(x)}{\partial x^2} = Fx - m_0 - \int_0^x \frac{F}{l}(x-s) \partial s, \quad (1)$$

82 where, E represents the Young's modulus, $w(x)$ is the deflection function of the cantilever in term
83 of x , I represents the moment of inertia, F represents the total force on the cantilever surface,
84 m_0 represents the moment at the clamped part, x represents the position the cantilever,

85 l represents the length of the cantilever and s represents the position with small displacement
86 from position x .

87

88 Now, integrating and applying the boundary condition, we get

$$89 \quad -EI \frac{\partial^2 w(x)}{\partial x^2} = Fx - m_0 - \frac{F}{l} x(x-0) + \frac{F}{l} (x^2 - 0), \quad (2)$$

$$90 \quad = Fx - m_0 - \frac{Fx^2}{2l}.$$

91 The boundary conditions of deflection are given by:

$$92 \quad \frac{\partial^2 w(0)}{\partial x^2} = 0, w(0) = 0, \frac{\partial^2 w(l)}{\partial x^2} = 0.$$

93 Applying the above boundary condition to Eq. 2, we get

$$94 \quad 0 = Fl - m_0 - \frac{Fl^2}{2l},$$

$$95 \quad \Rightarrow m_0 = \frac{Fl}{2}. \quad (3)$$

96 The putting the value of m_0 into Eq. 2, we get

97

$$98 \quad -EI \frac{\partial^2 w(x)}{\partial x^2} = Fx - \frac{Fl}{2} - \frac{Fx^2}{2l},$$

$$99 \quad \frac{\partial^2 w(x)}{\partial x^2} = \frac{1}{EI} \left(\frac{Fl}{2} + \frac{Fx^2}{2l} - Fx \right). \quad (4)$$

100 The stress $T(x)$ equation is given by

$$101 \quad T(x) = -Ez \frac{\partial^2 w(x)}{\partial x^2},$$

102 Where z represents the distance from the natural plane. Generally, it is half of the thickness
103 of the cantilever. Now, we get

$$104 \quad T(x) = -E \left(-\frac{h}{2} \right) \left(\frac{1}{EI} \left(\frac{Fl}{2} + \frac{Fx^2}{2l} - Fx \right) \right),$$

$$105 \quad = \frac{h}{2I} \left(\frac{Fl}{2} + \frac{Fx^2}{2l} - Fx \right). \quad (5)$$

106 The value of I is given by [15-16]

$$107 \quad I = \frac{bh^3}{12}.$$

108 Now, putting the value of I into Eq.5, we get

$$109 \quad T(x) = \frac{12h}{2bh^3} \left(\frac{Fl}{2} + \frac{Fx^2}{2l} - Fx \right),$$

$$110 \quad = \frac{3h}{lh^3} (Fl^2 + Fx^2 - 2lFx),$$

111
$$T(x) = \frac{3P}{h^2}(l^2 + x^2 - 2lx).$$
 (6)

112 To optimize the stress equation, the values of $(l^2 + x^2 - 2lx)$ in Eq. 6 is needto maximize.
 113 Now applying maxima and minima operation, we get the maximum value at $x=0$.As the value
 114 of $F=PA=Pbl$, we get

115
$$T(x)_{\max} = T(0) = \frac{3Fl}{bh^2} = \frac{3Pl^2}{h^2}.$$
 (7)

116 The optimized value of stress will be given by Eq. 7. In electrostatic model, the sensor's
 117 operational mode falls under the transverse mode (g_{31}) in the case of a cantilever beam
 118 structure. The output voltage on the piezoelectric surface of the sensor is given by

119
$$V(x) = g_{31}T(x)t.$$
 (8)

120 The sensitivity (S) of the sensor is calculated from the equation:

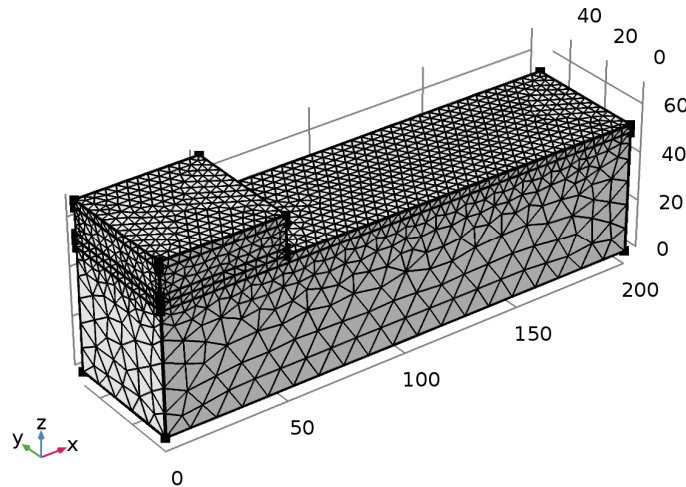
121
$$S = \frac{\Delta V}{\Delta P} = \frac{g_{31}t(T(x)_2 - T(x)_1)}{P_2 - P_1}.$$
 (9)

122 The sensitivity of the sensor can be improvised by taking the material with higher values of
 123 piezoelectric voltage coefficient, higher thickness of the piezoelectric material and higher
 124 induced stress values for the given input pressure.

125

126 3. SIMULATIONAND DISCUSSION

127 A 3D model of the sensor as shown in fig. 1 is designed in the COMSOL multiphysics
 128 simulator with the dimensions as tabulated in table 1 and simulated for the applied pressure
 129 range from 0 to 1000 Pa with step size 100 Pa. In COMSOL, the 3D model is assigned with
 130 the respective materials. The structure is configured with fixed constraints, boundary load,
 131 ground, terminal etc. After configuration the 3D model is meshing with tetrahedral shape and
 132 finer size as shown in fig. 3.

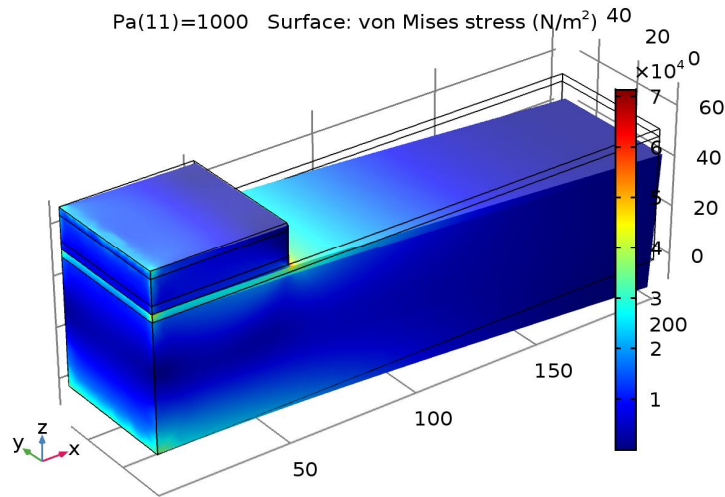


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Fig. 3: Meshing of the 3D model of the sensor.

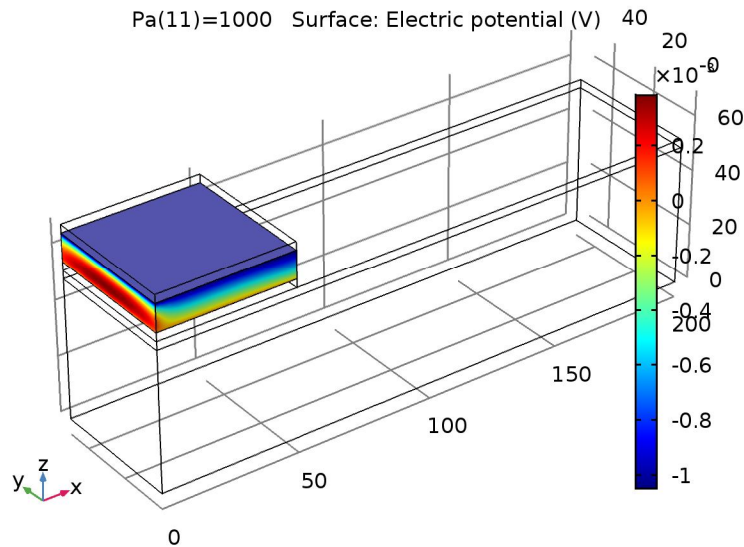
135 After meshing, the study of the 3D model sensor is done after simulation. The stress
136 distribution on the surface of the piezoelectric pressure sensor is shown in fig.4.



137

138 **Fig. 4: Stress distribution on the surface of the sensor.**

139 The maximum stress is occurred at the top of the sensor near the clamped part and
140 decreases as the position changes toward the free end of the cantilever. The voltage is
141 distributed on the surface of the piezoelectric pressure sensor as shown in fig.5.

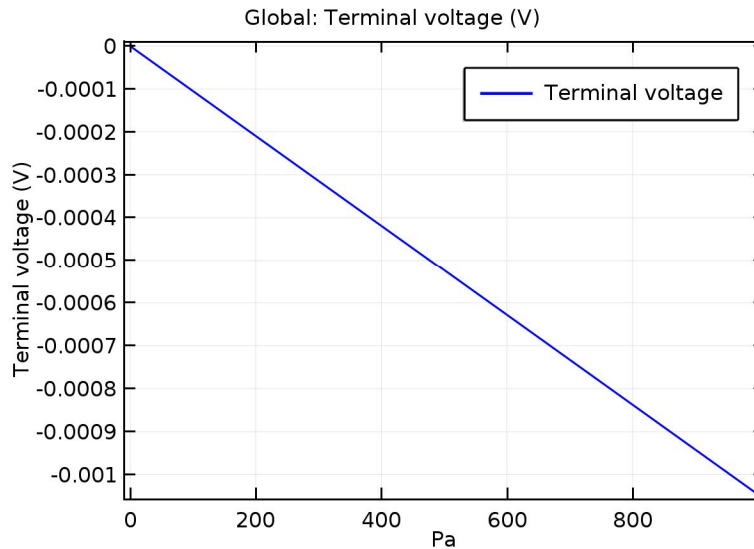


142

143 **Fig. 5: Voltage distribution on the surface of the piezoelectric material.**

144 The voltage distribution is higher in magnitude on the top surface of the piezoelectric material
145 with negative values. This negative value exists as the stress induced on the top surface is
146 tensile stress.

147 The average output voltage on the upper surface of the piezoelectric surface is shown in fig.
 148 6. It is obvious that the output voltage is highly linear with the input pressure with negative
 149 slope.



150

151 **Fig. 6: Simulated output voltage on the surface of the piezoelectric material.**

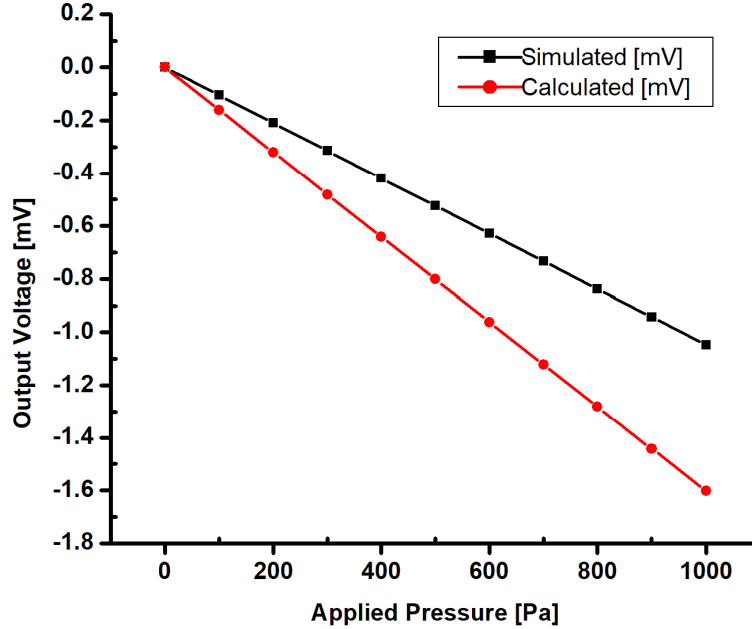
152 An analytical comparison is performed between the simulated and calculated values of the
 153 output voltage on the surface of piezoelectric pressure sensor. For calculation, Eq. 9 is used
 154 at $x=50 \mu\text{m}$ and the values of calculated and simulated values are tabulated in table 3.

155 **Table 3: Simulated and calculated values of output voltage of the sensor.**

Pressure	Simulated [mV]	Calculated [mV]
0	0.0	0.0
100	-0.104688	-0.16021
200	-0.209377	-0.32042
300	-0.314066	-0.48063
400	-0.418755	-0.64084
500	-0.523444	-0.80105
600	-0.628132	-0.96126
700	-0.732821	-1.12147
800	-0.837510	-1.28168
900	-0.942199	-1.44189
1000	-1.046887	-1.6021

156

157 The graphical representation of the table 3 is shown in fig.7. From the figure, it is seen that
 158 the calculated values are found slightly higher than the simulated values. The output voltage
 159 magnitudes shoot up with increase in applied pressure but the slope is negative.



160 **Fig. 7: Comparison of Simulated and Calculated output values.**

162 The simulated and calculated output values are found very close to each other. So, the
 163 proposed mathematical model can be used for future application as it is validated with
 164 simulated output values. The sensitivity of the simulated and calculated values are found as-
 165 1.046887mV/kPa and -1.6021 mV/kPa respectively.

166 Optimization of the output voltage is achieved by combining Eq. 6 and Eq. 8 and yields

167
$$V(x) = g_{31} \left(\frac{3P}{h^2} (l^2 + x^2 - 2lx) \right) t. \quad (10)$$

168 The above equation is utilized in Matlab software to maximize the output voltage at $x=0$ with
 169 various values of g_{31} , h , l and t .

170 **4. CONCLUSION**

172 The mathematical modelling, simulation, and optimisation of the PZT-5A Cantilever
 173 Piezoelectric Pressure Sensor for pressure ranges of 0-1000 Pa are the main topics of this
 174 research work. The mathematic model of the sensor is design and validated with the
 175 simulated values. According to the mathematical model, the stress on the structure depends
 176 on its length, width, thickness as well as its position and the pressure being applied. The
 177 stress, the piezoelectric voltage coefficient, and the thickness of the piezoelectric material all
 178 influence the sensor's output voltage. The output voltage has a negative slope and increases
 179 in magnitude as applied pressure increases. By maximising the stress, voltage coefficient,
 180 and thickness of the piezoelectric, the output voltage can be optimised. Therefore, it is

181 important to select a material that has a high piezoelectric coefficient and the highest
182 possible sensor dimension of the sensor structure. The sensitivity of the simulated and
183 calculated values are found as -1.046887 mV/kPa and -1.6021 mV/kPa respectively.

184

185 **COMPETING INTERESTS**

186

187 “Authors have declared that no competing interests exist”.

188

189 **AUTHORS’ CONTRIBUTIONS**

190

191 ‘Maibam Sanju Meetei’ designed the mathematical model and simulation of this work, and
192 wrote the first draft of the manuscript. ‘Heisnam Shanjit Singh’ analyzed and wrote the
193 second draft of the manuscript. Then both the authors read and approved the final
194 manuscript.”

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