

Structural and Electronic Properties of Hexagonal $Y_{1-x}Eu_xMnO_3$

ABSTRACT

Magnetolectric materials attract interest due to coupling between the magnetic and dipole moments, which provides additional degrees of freedom in magnetolectric device design and nanotechnological applications. Despite intensive theoretical and experimental studies already carried out in magnetolectric materials, some issues deserve more attention, specifically their structural and electronic properties. Here, density functional theory (DFT) was used to investigate the structural and electronic properties of hexagonal $Y_{1-x}Eu_xMnO_3$ ($x = 0.0, 0.1$ and 0.2) compounds. Our approach is based on the local spin density approximation (LSDA+U). The magnetic moment carried out by Mn atoms is very sensitive to the LSDA+U. We obtain the lattice parameters that compare well with experimental X-ray measurements, showing a difference between calculated values and experiment less than 2%. The calculated PDOS shows important contributions from the rare earth and the oxygen atoms in these systems, in which main contributions comes from the manganese atom. In addition, the electronic partial density of states (PDOS) shows a dominant contribution from the Mn and rare earth atoms near the Fermi level.

Keywords: Magnetolectric; Ab-initio; Hexagonal and Ceramic.

1. INTRODUCTION

A major current technological thrust is based on the development and optimization of new materials, in particular multiferroic compounds and heterostructures, since they exhibit a strong coupling in magnetic and polar degrees of freedom (the so called magnetolectric effect) [1]. "Magnetolectric materials have attracted a lot of interest, as the coupling between the magnetization and electric polarization provides an additional degree of freedom in magnetolectric device design" [2, 3].

In previous work, we studied a system of manganites, called $Eu_{1-x}Y_xMnO_3$, leading to great interest in these compounds [4], but we examined only its orthorhombic regime (Pbnm structure). Hexagonal manganites are few despite their interesting properties. Magnetic ordering occurs in both the orthorhombic and the hexagonal phase, but the hexagonal regime is more interesting due to ferroelectricity in the non-centrosymmetric $P6_3cm$ phase group, in which the rich yttrium content $Y_{1-x}Eu_xMnO_3$ ceramics crystallize. Unlike the orthorhombic case, there are practically no reported investigations on hexagonal $Y_{1-x}Eu_xMnO_3$ compounds.

"The small ionic radius of Y^{3+} results in a small value of the tolerance factor, leading to an instability of the perovskite structure" [5]. "Under standard preparation conditions, $YMnO_3$ crystallizes in a hexagonal structure and is a perovskite type oxide. However, the metastable $YMnO_3$ orthorhombic perovskite phase can be stabilized by high pressure synthesis or by

33 changing the average ionic radius of the Y site, i.e., by partial substitution of yttrium (Y) by
34 europium (Eu)” [6].

35 The hexagonal YMnO_3 ceramics system displays antiferromagnetic order below a Néel
36 temperature of 80 K, and a para-ferroelectric phase transition at 914 K. The couplings
37 observed in this material have a realistic potential for practical applications in electronic
38 devices, where the dielectric (capacitive) response can be changed by the onset of the
39 magnetic transition or by application of an external magnetic field [7].

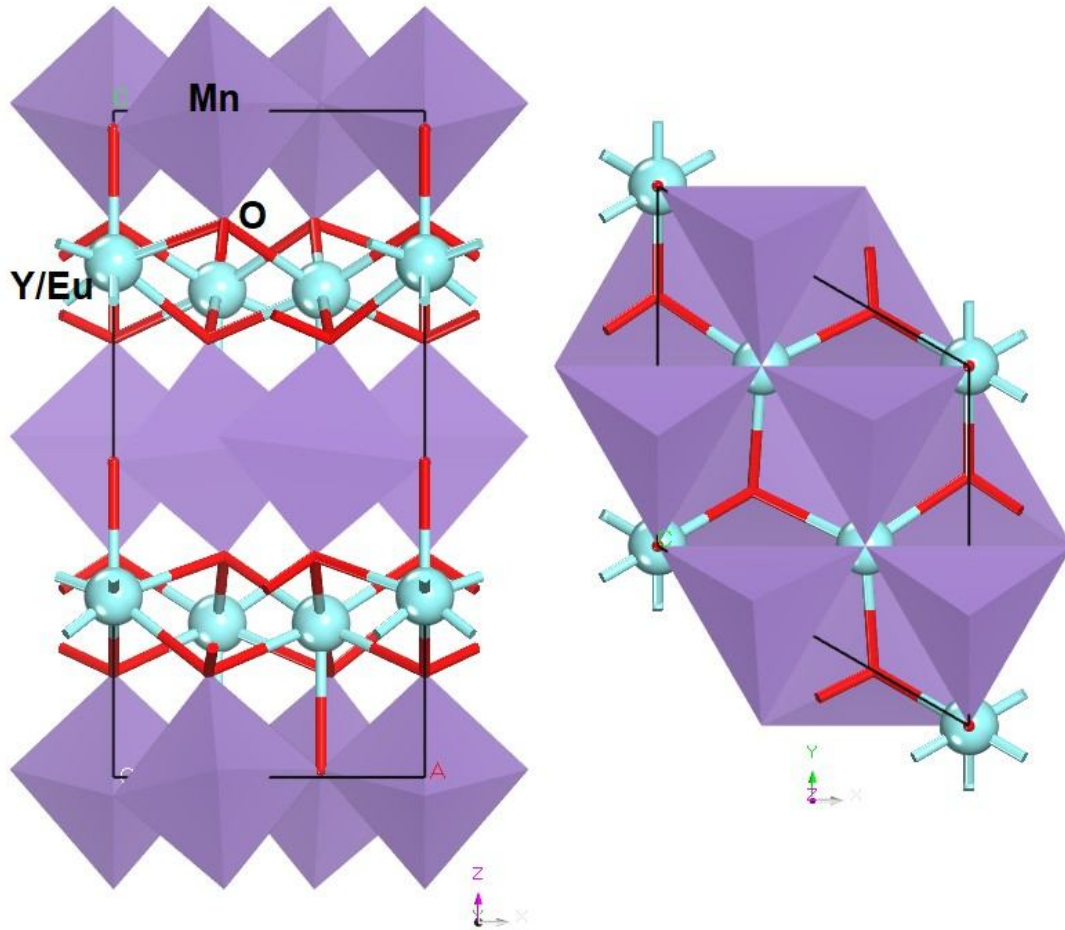
40 In this paper, we carry out a systematic study of YMnO_3 , $\text{Y}_{0.9}\text{Eu}_{0.1}\text{MnO}_3$, and $\text{Y}_{0.8}\text{Eu}_{0.2}\text{MnO}_3$
41 using density functional theory and X-ray diffraction.

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43 2. METHODOLOGY

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45 The electronic properties of $\text{Y}_{1-x}\text{Eu}_x\text{MnO}_3$ were obtained by optimizing the structures using
46 the density functional theory (DFT) approach [8, 9]. The systems crystallize in a hexagonal
47 structure with space group $\text{P6}_3\text{cm}$ (see Fig. 1). The periodic DFT calculations were
48 performed using the plane-wave pseudopotential method, as implemented in the CASTEP
49 code [10]. The calculations were carried out by spin-polarized DFT within the local spin
50 density approximation (LSDA+U), suitable for transition metal oxides, certain inorganic
51 surface studies, and metallic systems containing magnetic elements, as presented in Ref.
52 [11]. The exchange correlation was calculated using the Perdew-Zunger parametrization [12]
53 of the Ceperley-Alder potential [13]. For geometry optimization, ultrasoft Vanderbilt-type
54 pseudopotentials [14] were used, considering the following electronic configurations for each
55 atomic species: $\text{Eu-}4f^7\text{-}5s^2\text{-}5p^6$, $\text{Y-}4s^2\text{-}4p^6\text{-}4d^1\text{-}5s^2$, $\text{Mn-}3d^5\text{-}4s^2$, and $\text{O-}2s^2\text{-}2p^4$ within the
56 virtual crystal approximation (VCA) implemented in the CASTEP code [15], which is used to
57 model disorder in solids. VCA calculations use weights according to the site occupancies to
58 obtain the contribution of each pseudopotential. “A Monkhorst-Pack [16] $3 \times 3 \times 2$ sampling
59 was used to evaluate all integrals in reciprocal space, its grid being selected to ensure a well
60 converged electronic structure for each crystal”.



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Fig. 1. Hexagonal crystal structure of $Y_{1-x}Eu_xMnO_3$.

63 “Lattice parameters and atomic positions were optimized by seeking a total minimum energy
 64 for the $Y_{1-x}Eu_xMnO_3$ unit cell. The convergence tolerances for all geometry optimizations
 65 were: total energy change smaller than 0.5×10^{-5} eV/atom, maximum force per atom
 66 below 0.1×10^{-1} eV/Å, pressure smaller than 0.02 GPa, and maximum atomic
 67 displacement not exceeding 0.5×10^{-3} Å. The convergence tolerance window was for two
 68 successive steps, and the optimization method used Broyden-Fletcher-Goldfarb-Shanno
 69 (BFGS) minimization [17], which is used to perform cell optimization, including optimization
 70 at fixed external stress”. The BFGS scheme uses a starting Hessian which is recursively
 71 updated during optimization. Within each self-consistent field (SCF) step, the electronic
 72 minimization parameters for convergence were: total energy/atom smaller 5×10^{-7} eV/atom,
 73 electronic eigen-energy variation smaller than 0.1071×10^{-6} eV at most, and a convergence
 74 window of three SCF cycles. A plane-wave basis set was adopted to represent the Kohn-
 75 Sham orbitals, with cutoff energy chosen, after convergence studies, to be 880 eV. The
 76 quality of this basis set was kept fixed even taking into account the unit cell volume
 77 variations during the geometry optimization process. After obtaining the optimized unit cells
 78 and atomic positions, the Kohn-Sham electronic band structure and the partial density of
 79 states (PDOS) were evaluated for the optimized LSDA unit cell.

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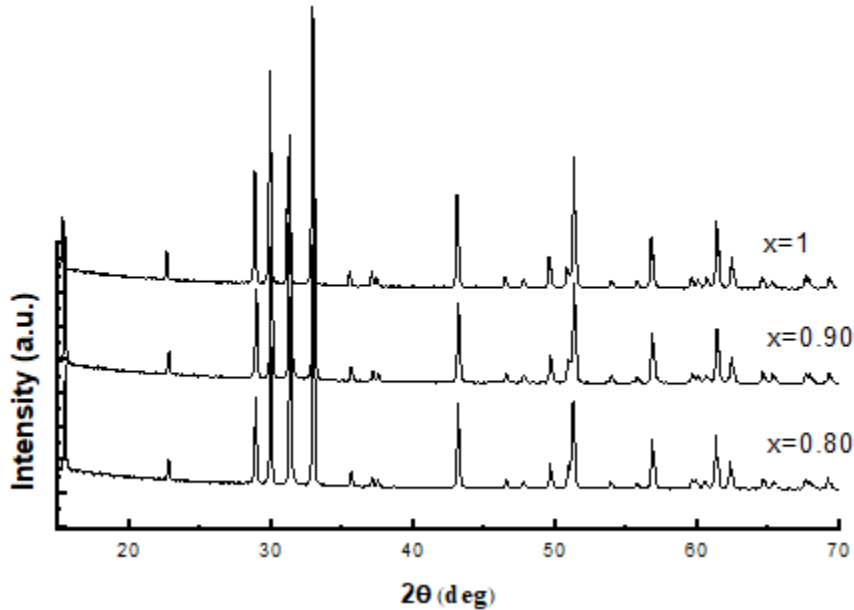
81 **3. RESULTS AND DISCUSSION**

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83 **3.1 Crystal Structure at Room Temperature**

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85 Room temperature X-ray powder diffraction (XRD) spectra obtained from the system, are
 86 displayed in Fig. 2. Here, $x = 1$, $x = 0.1$, and $x = 0.2$ correspond to YMnO_3 , $\text{Y}_{0.9}\text{Eu}_{0.1}\text{MnO}_3$,
 87 and $\text{Y}_{0.8}\text{Eu}_{0.2}\text{MnO}_3$, respectively. No secondary crystallographic phases were detected.



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89 **Fig. 2. X-ray diffraction spectra of $\text{Y}_{1-x}\text{Eu}_x\text{MnO}_3$ recorded at room temperature.**

90 The samples were prepared using the urea sol-gel combustion method. Stoichiometric
 91 amounts of Eu_2O_3 (Alfa Aesar, chemical purity), Y_2O_3 (Aldrich, 99.99%), and $\text{Mn}(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O}$
 92 (ABCR chemical purity) were dissolved in diluted aqueous solution of nitric acid.

93 Hexagonal $\text{Y}_{1-x}\text{Eu}_x\text{MnO}_3$ consists of MnO_5 trigonal bipyramids where each manganese ion is
 94 surrounded by three in-plane and two apical oxygen ions and presents corner linked to form
 95 a triangular-lattice layer in the ab -plane. The Mn-O1 and Mn-O2 bonds are parallel to the c -
 96 axis, and the triangular base of MnO_5 bipyramids is vertical to the c -axis.

97 Table 1 shows the values of the cell parameters and density obtained from the structural
 98 refinement of the XRD data.

99 **Table 1. Cell parameters and density obtained from the analysis of the XRD**
 100 **spectra.**

	$\text{Y}_{0.8}\text{Eu}_{0.2}\text{MnO}_3$	$\text{Y}_{0.9}\text{Eu}_{0.1}\text{MnO}_3$	YMnO_3
$a(\text{Å})$	6.1663	6.155	6.1404
$c(\text{Å})$	11.3985	11.3990	11.3967
$V(\text{Å}^3)$	375.289	373.999	372.14
$\rho(\text{g/cm}^3)$	4.968	4.990	4.470

101 The computed lattice parameters and unit cell volumes for $Y_{1-x}Eu_xMnO_3$ system have been
 102 performed from our experimental lattice parameters, as shown in Table 1. LDA lattice
 103 parameters are smaller, almost always, due to the well-known trend of this functional to
 104 overestimate the strength of interatomic interactions, but due to the calculations were carried
 105 out by spin-polarized DFT calculations, the c lattice parameters increased causing an
 106 increase in volume for hexagonal $Y_{1-x}Eu_xMnO_3$.

108 3.2 Geometry Optimization

109
 110 LDA lattice parameters, almost always, are smaller how experimental measured ones due to
 111 the well-known trend of this functional to overestimate the strength of interatomic
 112 interactions, while the calculations were carried out by spin-polarized DFT calculations.

113 Table 2 presents a comparison of the experimental lattice parameters and cell volumes and
 114 the corresponding values obtained from DFT-LSDA+U computations. The deviations
 115 between the experimental and calculated values are also presented.

116 **Table 2. Lattice parameters for $Y_{1-x}Eu_xMnO_3$ after DFT-LSDA computations.**
 117 **Experimental data (EXP.) for $YMnO_3$ ($x = 1$), $Y_{0.8}Eu_{0.2}MnO_3$ ($x=0.2$) and $Y_{0.9}Eu_{0.1}MnO_3$**
 118 **($x=0.1$), respectively.**

Alloy/Data Source	$a(\text{\AA})$	$b(\text{\AA})$	$c(\text{\AA})$	$V(\text{\AA}^3)$
LSDA ($x=1$)	6.0514 (-1.4%)	6.0514 (-1.4%)	11.4284 (+0.2%)	362.43 (-2.6%)
<i>Exp</i> ($x=1$)	6.1404	6.1404	11.3967	372.14
LSDA ($x=0.2$)	6.0657 (-1.4%)	6.0657 (-1.4%)	11.4635 (+0.5%)	365.271 (-2.3%)
<i>Exp</i> ($x=0.2$)	6.1551	6.1551	11.3990	373.999
LSDA ($x=0.1$)	6.0839 (-1.3%)	6.0839 (-1.3%)	11.9336 (+4.4%)	382.245 (+1.8%)
<i>Exp</i> ($x=0.1$)	6.1663	6.1663	11.3985	375.289

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120 An analysis of Table 2 allows us to conclude that the theoretical LSDA+U approach give
 121 results with a reasonable approximation to the experimental data, as it can be obtained for
 122 $GdMnO_3$ [11].

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124 3.3 Partial Density of States

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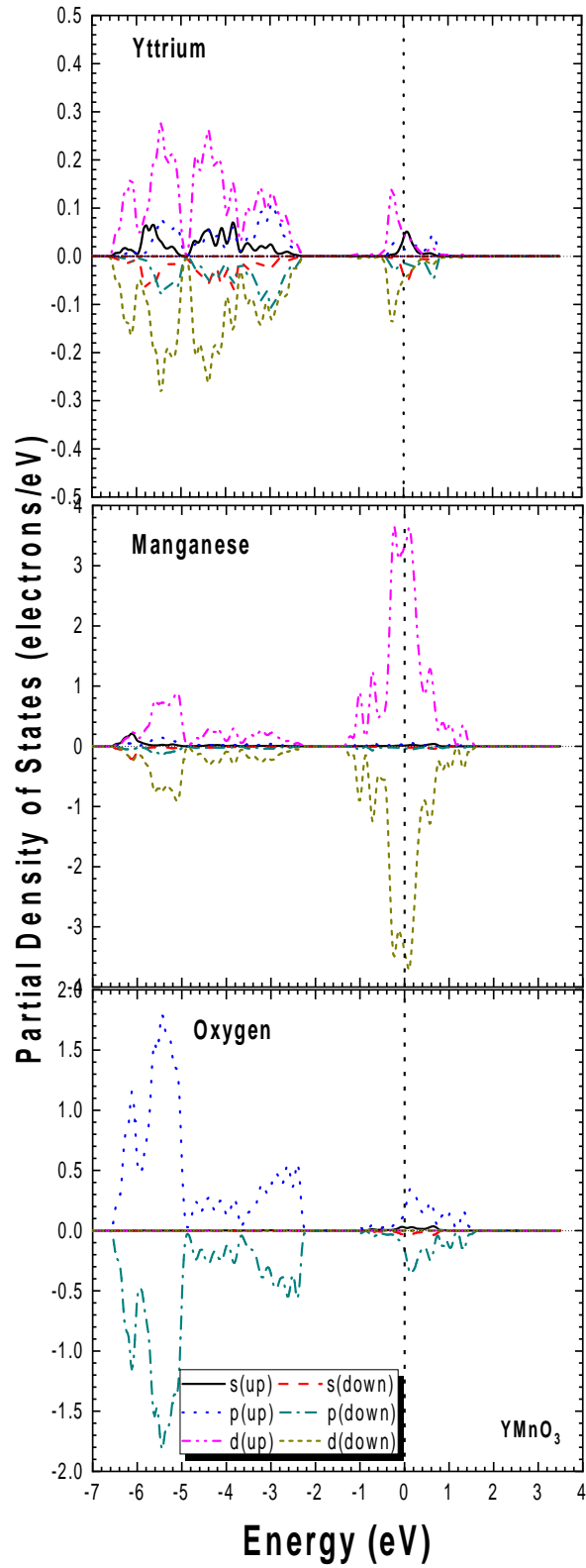
126 The Kohn-Sham electronic band structure gives a picture of the electronic eigenenergies E
 127 as a function of a wavevector k in the first Brillouin zone (BZ). The partial densities of states
 128 (PDOS) per orbital for the here studied $Y_{1-x}Eu_xMnO_3$ are shown individually in Fig. 3. The
 129 obtained PDOS are mainly formed from d atomic orbitals, particularly the bands between 0.0
 130 and -1.0 eV.

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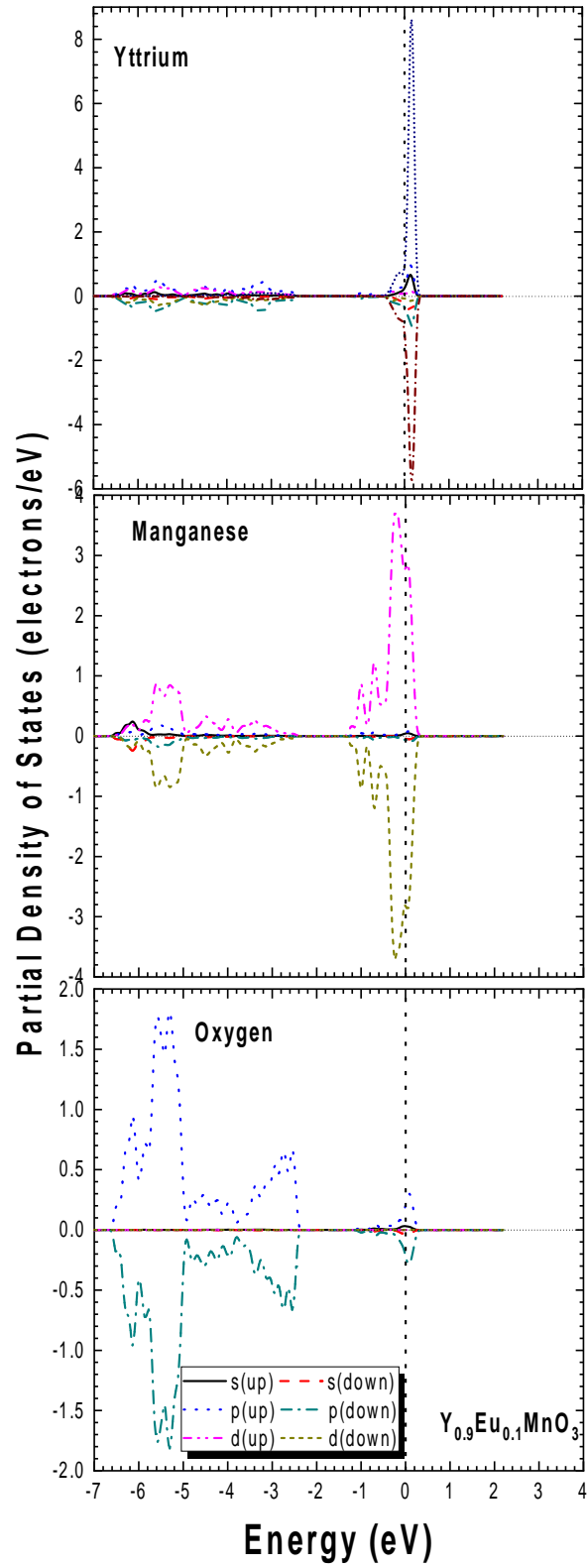
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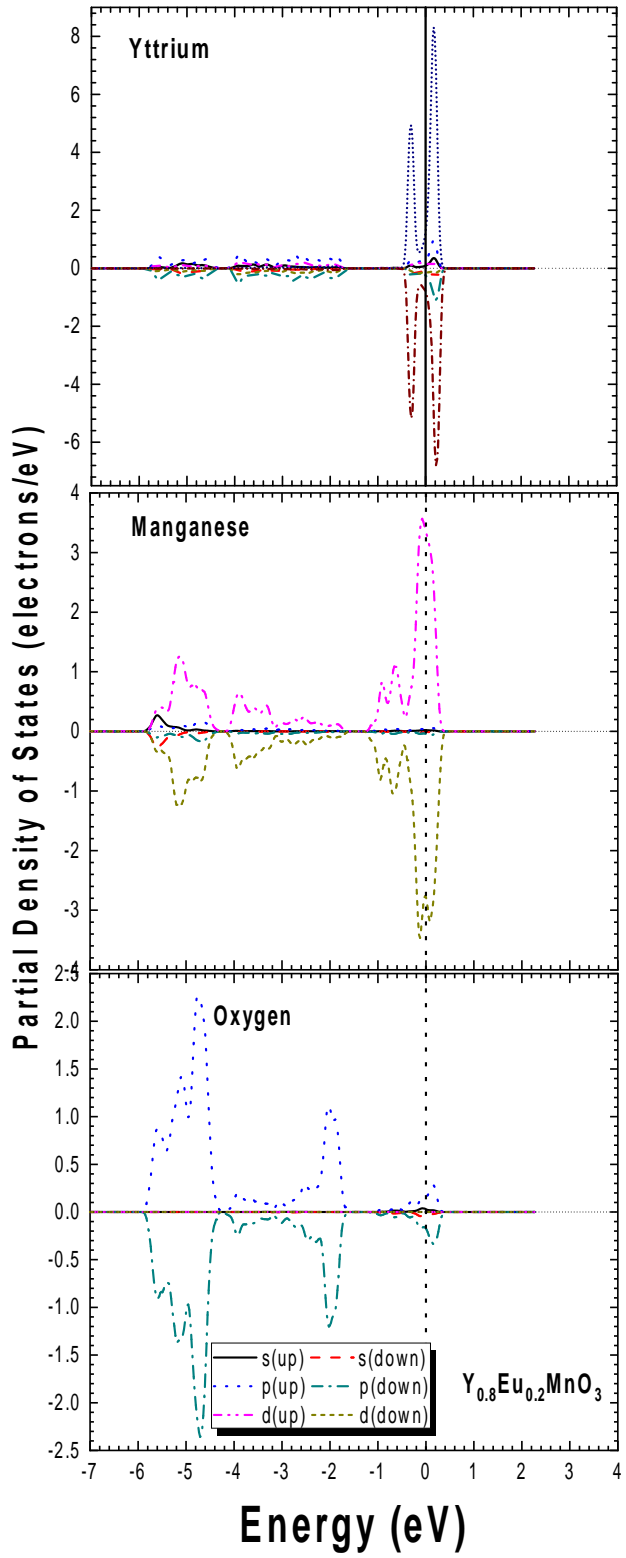
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285 **Fig. 3. Partial density of states of $Y_{1-x}Eu_xMnO_3$ recorded at room temperature.**

286 The Fermi level is taken arise be 0.0 eV. For energy bands below Fermi level, the smaller
287 contribution, from the O-2p level. The main contribution observed around the Fermi level, is
288 dominated the orbitals from the transition metal element specifically the Mn-3d orbitals. This
289 important because manganese presents the magnetic characteristics. **Moreover, until now,**
290 **the literature does not present a detailed study of these properties.**

291 PDOS analysis formalism is not for high energy states in the conduction band, in our case
292 PDOS representation will usually decay to zero at about 1 eV above the Fermi level. This is
293 associated with the fact that expansion of essentially free electron states in terms of a limited
294 number of atomic-like basis functions is impossible to carry out with any degree of accuracy.
295 Only the valence band and lower part of the conduction band are meaningful in the PDOS
296 plot.

297

298 **4. CONCLUSION**

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300 $Y_{1-x}Eu_xMnO_3$ perovskite were studied using a DFT formalism, based on the local density
301 approximation (LSDA+U) for the exchange-correlation functional. After geometry
302 optimization, we have obtained lattice parameters that compare well with experimental X-ray
303 with the difference between calculated values and experiment being less than 2% because
304 the LDA exchange- correlation energy tends to produce larger forces between atoms, an
305 effect also responsible for the small lattice parameters (angles and bond length) predicted by
306 using this level of theory in comparison with measurements.

307 The density of states at the Fermi level is dominated by Mn seems consistent with the fact
308 that the system is ferroelectric. Finally, the calculated PDOS shows important contributions
309 from the rare earth and the oxygen atoms in both systems, in which main contributions
310 comes from the manganese atom.

311

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318 **COMPETING INTERESTS**

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320 The authors declare that they have no known competing financial interests.

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322 **AUTHORS' CONTRIBUTIONS**

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324 The authors declare that they have no known competing financial interests.

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