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# Computing Y-index of Different corona products of Graphs

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## ABSTRACT

The Y-index of a graph is defined by the sum of four of degrees of the vertices of a graph. Among the all topological indices the Zagreb indices have been used more considerably than any other topological indices in chemical literature. The concept of Corona Product is a recent inclusion to mathematical vocabulary. One of the most significant graph operations is the corona product of several generic and specific graphs, which is one of the most well-known graph products. In this study, we derive some explicit formulations of several corona product types, including subdivision-vertex corona, subdivision-edge corona, subdivision-vertex neighborhood corona, subdivision-edge neighborhood corona, and vertex-edge corona of two graphs.

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*Keywords:* Topological index, Zagreb index, Y-index, Corona product, Graph operations.

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## 1. INTRODUCTION

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The definition of a topological function is a real valued function that converts any molecular graph into a real number and is inescapably invariant under graph automorphism. In theoretical chemistry, molecule structure is given a numerical value that closely corresponds to the physical quantities and activities. For modeling the physicochemical, pharmacologic, toxicologic, biological, and other aspects of chemical substances, topological indices, also known as molecular structure descriptors, are used.

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In this paper, we consider only finite, connected and undirected graphs without any self-loops or multiple edges. Let  $A$  be a graph with vertex set  $V(A)$  and edge set  $E(A)$ . So that the vertex set will be considered  $n$  and the edge set will be considered  $m$ . The vertices  $u$  and  $v$  is connected by edge and is denoted by  $u v$ . Let  $d_G(v)$  denote the degree of the vertex  $v$  in  $A$ , which is the number of edges incident to  $v$ .

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Zagreb indices are among the best applications for recognizing physical properties and chemical reactions in practical applications. The First Zagreb index  $M_1(A)$  and Second Zagreb index  $M_2(A)$  were firstly considered by I. Gutman and N. Trinajstić in 1972[1] defined as

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$$M_1(A) = \sum_{v \in V(A)} d_A(v)^2 = \sum_{uv \in E(A)} [d_A(u) + d_A(v)]$$

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$$M_2(A) = \sum_{u, v \in V(A)} d_A(u) d_A(v)$$

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These indices have considerably studied with respect to both mathematical and chemical point of view. In 2005, Li and Zheng [1], introduce the First general Zagreb index as

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$$\begin{aligned} M_1^{\alpha+1}(A) &= \sum_{v \in V(A)} d_A^{\alpha+1}(v) \\ &= \sum_{uv \in E(A)} d_A^{\alpha}(u) + d_A^{\alpha}(v) \end{aligned}$$

36 In 2018, Nilanjan De uses modern index to calculate the F-index and co index of some  
 37 derived graphs [2]. Its special of First general Zagreb index where  $\alpha = 3$

38 
$$M_1^4(A) = \sum_{uv \in E(A)} d_A^3(u) + d_A^3(v)$$

39 So that the Y-index is defined as [3],

40 
$$Y(A) = \sum_{u \in V(A)} d_A^4(u) = \sum_{uv \in E(A)} d_A^3(u) + d_A^3(v)$$

41 Let  $A_1$  and  $A_2$  be two simple connected graphs with  $n_i$  number of vertices and  $m_i$   
 42 number of edges respectively, for  $i \in \{1,2\}$ . The Corona product  $A_1 \circ A_2$  of these two  
 43 graphs is obtained by taking one copy of  $A_1$  and  $n_1$  copies of  $A_2$ : and by joining each vertex  
 44 of the  $i$ -th copy of  $A_2$  to the  $i$ -th vertex of  $A_1$  where  $1 \leq i \leq n$ . The corona product of  $A_1$  and  
 45  $A_2$  has total number of  $(n_1 n_2 + n_1)$  vertices and  $(m_1 + n_1 m_2 + n_1 n_2)$  edges

46  
 47 The Subdivision graph  $S=S(A)$  is a graph obtained from  $A$  by replacing each of its  
 48 edges by a path of length two, or equivalently by inserting an additional vertex into each  
 49 edge of  $A$

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## 52 2. MAIN RESULTS

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### 54 2.1 Subdivision-vertex corona

55 **Definition.** [4] Let  $A_1$  and  $A_2$  be two vertex disjoint graphs. The Subdivision-vertex corona  
 56 of  $A_1$  and  $A_2$  is denoted by  $A_1 \square A_2$  and obtained from  $S(A_1)$  and  $n_1$  copies of  $A_2$ , all  
 57 vertex-disjoint, by joining the  $i$ -th vertex of  $V(A_1)$  to every vertex in the  $i$ -th copy of  
 58  $A_2$

59 By definition it is clear that the Subdivision-vertex corona  $A_1 \square A_2$  has  
 60  $n_1(1 + n_2) + m_1$  vertices and  $2m_1 + n_1(n_2 + m_2)$  edges. Also the degree of the vertices of  
 61  $A_1 \square A_2$  are given by

62

63 
$$d_{A_1 \square A_2}(v_i) = d_{A_1}(v_i) + n_2 \text{ for } i = 1, 2, \dots, n_1$$

64 
$$d_{A_1 \square A_2}(e_i) = 2 \text{ for } i = 1, 2, \dots, m_1$$

65 
$$d_{A_1 \square A_2}(v_j^i) = d_{A_2}(v_j) + 1 \text{ for } i = 1, 2, \dots, n_1 \text{ and } j = 1, 2, \dots, n_2$$

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67 We calculate the Y-index for the Subdivision-vertex corona  $A_1 \square A_2$

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### 73 Theorem.2.1

74 The Y-index of the Subdivision-vertex corona  $A_1 \square A_2$  is given by

75 
$$Y(A_1 \square A_2) = Y(A_1) + 4n_2 F(A_1) + 6n_2^2 M_1(A_1) + 8m_1 n_2^3 + n_1 n_2^4$$

76

77 
$$+ 16m_1 + n_1 Y(A_2) + 4n_1 F(A_2) + 6n_1 M_1(A_2) + 8n_1 m_2 + n_1 n_2$$

78

79 Proof : From the definition of Subdivision-vertex corona  $A_1 \square A_2$  , we get

80 
$$Y(A_1 \square A_2) = \sum_{i=1}^{n_1} (d_{A_1}(v_i) + n_2)^4 + \sum_{i=1}^{m_1} 2^4 + \sum_{i=1}^{n_1} \sum_{j=1}^{n_2} (d_{A_2}(u_j) + 1)^4$$

81 
$$= \sum_{i=1}^{n_1} d_{A_1}(v_i)^4 + 4n_2 d_{A_1}(v_i)^3 + 6d_{A_1}(v_i)^2 n_2^2 + 4d_{A_1}(v_i) n_2^3 + n_2^4 +$$

82 
$$16m_1 + n_1 \left( \sum_{j=1}^{n_2} d_{A_2}(u_j)^4 + 4d_{A_2}(u_j)^3 + 6d_{A_2}(u_j)^2 + 4d_{A_2}(u_j) + 1 \right)$$

83 
$$= Y(A_1) + 4n_2 F(A_1) + 6n_2^2 M_1(A_1) + 8m_1 n_2^3 + n_1 n_2^4$$

84 
$$+ 16m_1 + n_1 Y(A_2) + 4n_1 F(A_2) + 6n_1 M_1(A_2) + 8n_1 m_2 + n_1 n_2$$

85 Hence, we get the desired result.

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88 **Corollary. 2.2**

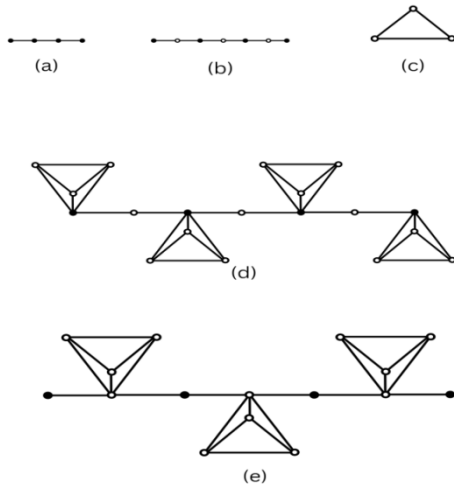
89 
$$Y(P_n \square P_m) = nm^4 + 8m^3(n - 1) + 12m^2(2n - 3) + 113nm - 56m - 98n - 46$$

90 
$$Y(C_n \square C_m) = nm^4 + 8nm^3 + 24nm^2 + 113nm + 32n$$

91 
$$Y(C_n \square P_m) = nm^4 + 8nm^3 + 24nm^2 + 113nm - 98n$$

92

93 The Subdivision-vertex corona of  $P_4, P_2$  and  $C_3$  is given by



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96 **Figure 1:** (a)-path p4, (b)-Subdivision S (p4), (c)-Cycle c3, (d)-Subdivision –vertex corona

97 p4 c3, (e)- Subdivision-edge corona p4 c3

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100 **2.2 Subdivision-edge corona**

101 **Definition.**[4] Again from the definition of subdivision graphs, The Subdivision-edge corona  
102 product  $A_1 \oplus A_2$  of  $A_1$  and  $A_2$  is obtained from the  $S(A_1)$  and  $m_1$  copies of  $A_2$  such that for all  
103 disjoint vertices joining the  $i$ -th vertex of  $S(A_1)$  to every vertex in the  $i$ -th copy of  $A_2$ . Clearly  
104 the product  $A_1 \oplus A_2$  has  $m_1(1 + n_2) + n_1$  vertices and  $m_1(n_2 + m_2 + 2)$  edges. Also the  
degree of vertices of  $A_1 \oplus A_2$  are given by

105

106  $d_{A_1 \oplus A_2}(v_i) = d_{A_1}(v_i)$  for  $i = 1, 2, \dots, n_1$

107  $d_{A_1 \oplus A_2}(v_i) = 2 + n_2$  for  $i = 1, 2, \dots, m_1$

108  $d_{A_1 \oplus A_2}(v_j^i) = d_{A_2}(u_j) + 1$  for  $i = 1, 2, \dots, n_1$  and  $j = 1, 2, \dots, n_2$

109

110 **Theorem 2.3.**

111 The Y-index of Subdivision-edge corona  $A_1 \oplus A_2$  is given by

112  $Y(A_1 \oplus A_2) = Y(A_1) + [m_1(n_2 + 2)]^4 + m_1 Y(A_2) + 4m_1 F(A_2)$

113

114  $+6m_1 M_1(A_2) + 8m_1 m_2 + m_1 n_2$

115

116 Proof: From the definition of Subdivision-edge corona  $A_1 \oplus A_2$ , we have

117  $Y(A_1 \oplus A_2) = \sum_{i=1}^{n_1} (d_{A_1}(v_i))^4 + \sum_{i=1}^{m_1} (2 + n_2)^4 + \sum_{i=1}^{m_1} \sum_{j=1}^{n_2} (d_{A_2}(u_j) + 1)^4$

118  $= Y(A_1) + [m_1(n_2 + 2)]^4 + m_1 Y(A_2) + 4m_1 F(A_2)$

119

120  $+6m_1 M_1(A_2) + 8m_1 m_2 + m_1 n_2$

121

122 Hence we get the result

123

124 **Corollary.2.4**

125  $Y(P_n \oplus P_m) = m^4(n - 1) + 8m^3(n - 1) + 2m^2(n - 1) + 113nm - 113m - 98n + 84$

126  $Y(C_n \oplus C_m) = nm^4 + 8nm^3 + 2nm^2 + 113nm + 32n$

127  $Y(C_n \oplus P_m) = nm^4 + 8nm^3 + 2nm^2 + 113nm - 98n$

128

129 **2.3 Subdivision- vertex neighborhood corona**

130 **Definition.**[5] Subdivision –vertex neighborhood corona product  $A_1 \odot A_2$  of  $A_1$  and  $A_2$  is  
131 obtained from the  $S(A_1)$  and  $n_1$  copies of  $A_2$  such that for all disjoint vertices joining the  
132 neighbors of the  $i$ -th vertex of  $S(A_1)$  to every vertex in the  $i$ -th copy of  $A_2$ . Thus  $A_1 \odot A_2$  has  
133  $m_1(1 + n_2) + n_1$  vertices  $2m_1$  edges .

134 Let  $V(A_1) = \{v_1, v_2, \dots, v_{n_1}\}$ ,  $I(A_1) = \{e_1, e_2, \dots, e_{m_1}\}$  and  $V(A_2) = \{v_1, v_2, \dots, v_{n_2}\}$ . Also , let the  
135 vertex set of the  $i$ -th copy of  $A_2$  is denoted by  $V(A_2^i) = \{u_1^i, u_2^i, \dots, u_{n_2}^i\}$ , for  $i=1, 2, \dots, n_2$ . Then  
136  $(A_1 \odot A_2) = V(A_1) \cup I(A_1) \cup [V^1(A_2) \cup V^2(A_2) \cup \dots \cup V^{n_1}(A_2)]$  . The degree of the vertices  
137 of  $A_1 \odot A_2$  are given by

138  $d_{A_1 \odot A_2}(v_i) = d_{A_1}(v_i)$  for  $i = 1, 2, \dots, n_1$

139  $d_{A_1 \odot A_2}(e_i) = 2n_2 + 2$  for  $i = 1, 2, \dots, m_1$

140  $d_{A_1 \odot A_2}(v_j^i) = d_{A_2}(u_j) + d_{A_1}(v_j)$  for  $i = 1, 2, \dots, n_1$  and  $j = 1, 2, \dots, n_2$

141

142 The Y-index of Subdivision-vertex neighborhood corona of two graphs is defined in the  
143 following theorem

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145

146 **Theorem 2.5.**

147 The Y-index of  $A_1 \odot A_2$  is given by

148  $Y(A_1 \odot A_2) = Y(A_1) + 16m_1(n_2 + 1)^4 + n_1 Y(A_2) + 8m_1 F(A_2)$

149

150  $+6M_1(A_2) M_1(A_1) + 8m_2 F(A_1) + n_2 Y(A_1)$

151

152 Proof: From the definition of  $A_1 \odot A_2$ , we have

$$153 \quad Y(A_1 \odot A_2) = \sum_{i=1}^{n_1} (d_{A_1}(v_i))^4 + \sum_{i=1}^{m_1} (2n_2 + 2)^4 + \sum_{i=1}^{n_1} \sum_{j=1}^{n_2} (d_{A_2}(u_j) + d_{A_2}(v_j))^4$$

$$154 \quad = Y(A_1) + 16m_1(n_2 + 1)^4 + n_1Y(A_2) + 8m_1 F(A_2)$$

155

$$156 \quad + 6M_1(A_2) M_1(A_1) + 8m_2F(A_1) + n_2Y(A_1)$$

157

158 Hence we get the desired result

159

160 **Corollary. 2.6**

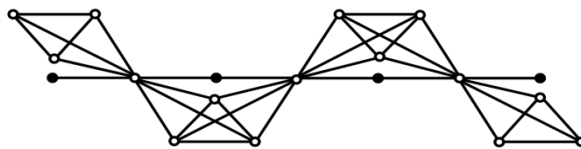
$$161 \quad Y(P_n \odot P_m) = 16m^4(n - 1) + 64m^3(n - 1) + 96m^2(n - 1) + 320nm - 414m - 318n + 394$$

$$162 \quad Y(C_n \odot C_m) = 16nm^4 + 6nm^3 + 96nm^2 + 320nm + 32n$$

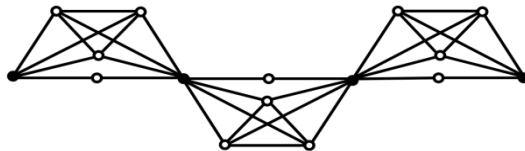
$$163 \quad Y(C_n \odot P_m) = 16nm^4 + 64nm^3 + 96nm^2 + 320nm - 318n$$

164

165 The Subdivision-vertex neighborhood corona of  $P_4, P_2$  and  $C_3$  is given in the figure.



(f)



(g)

166

167 **Figure.2:** (f)- Subdivision-vertex neighborhood corona p4 c3, (g)- Subdivision-edge  
168 neighborhood corona p4 c3

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## 172 **2.4 Subdivision-edge neighborhood corona**

173 **Definition.[5]:** For two vertex disjoint graphs  $A_1$  and  $A_2$ , the Subdivision –edge  
174 neighborhood corona  $A_1$  and  $A_2$  is denoted by  $A_1 \boxtimes A_2$  and obtained from  $S(A_1)$  and  $n_1$   
175 copies of  $A_2$  all vertex disjoint, by joining the neighbors of the  $i$ -th vertex of  $V(A_1)$  to every  
176 vertex in the  $i$ -th copy of  $A_2$ .

177 Let  $V(A_1) = \{v_1, v_2, \dots, v_{n_1}\}, I(A_1) = \{e_1, e_2, \dots, e_{m_1}\}$  and  $V(A_2) = \{v_1, v_2, \dots, v_{n_2}\}$ . Also, let the  
 178 vertex set of the  $i$ -th copy of  $A_2$  is denoted by  $V(A_2^i) = \{u_1^i, u_2^i, \dots, u_{n_2}^i\}$ , for  $i=1, 2, \dots, n_1$ . Then  
 179  $A_1 \boxminus A_2 = V(A_1) \cup I(A_1) \cup [V^1(A_2) \cup V^2(A_2) \cup \dots \cup V^{n_1}(A_2)]$

180 .The degree of the vertices of  $A_1 \boxminus A_2$  are given by

181  $d_{A_1 \boxminus A_2}(v_i) = (n_2 + 1)d_{A_1}(v_i)$  for  $i = 1, 2, \dots, n_1$

182  $d_{A_1 \boxminus A_2}(e_i) = 2$  for  $i = 1, 2, \dots, m_1$

183  $d_{A_1 \boxminus A_2}(v_j^i) = d_{A_2}(u_j) + 2$  for  $i = 1, 2, \dots, n_1$  and  $j = 1, 2, \dots, n_2$

184 The Subdivision-edge neighborhood corona of  $P_4, P_2$  and  $C_3$  is given in the figure.2

185 So the result of this section is the following

186

187 **Theorem.2.7**

188 The Y-index of  $A_1 \boxminus A_2$  is given by

189  $Y(A_1 \boxminus A_2) = Y(A_1)(n_2 + 1)^4 + 16m_1 + n_1Y(A_2) + 8n_1 F(A_2)$

190

191  $+24n_1M_1(A_2) + 64n_1m_2 + 16n_1n_2$

192

193 Proof: From the definition of Subdivision –edge neighborhood corona product of two graphs.

194 We have

195 
$$Y(A_1 \boxminus A_2) = \sum_{i=1}^{n_1} (n_2 + 1)^4 (d_{A_1}(v_i))^4 + \sum_{i=1}^{m_1} 2^4 + \sum_{i=1}^{n_1} \sum_{j=1}^{n_2} (d_{A_2}(u_j) + 2)^4$$

196 
$$= (n_2 + 1)^4 Y(A_1) + 16m_1 + n_1 \left( \sum_{i=1}^{n_2} d_{A_2}(u_j)^4 + 8d_{A_2}(u_j)^3 \right.$$

$$\left. + 24d_{A_2}(u_j)^2 + 4d_{A_2}(u_j).2^3 + 2^4 \right)$$

197 
$$= Y(A_1)(n_2 + 1)^4 + 16m_1 + n_1Y(A_2) + 8n_1 F(A_2)$$

198

199 
$$+24n_1M_1(A_2) + 64n_1m_2 + 16n_1n_2$$

200

201 Hence we get the result

202

203 **Corollary. 2.8**

204  $Y(P_n \boxminus P_m) = 16nm^4 - 30m^4 + 64nm^3 - 120m^3 + 96nm^2 - 180m^2 + 320nm - 318n -$   
 205  $120m - 46$

206  $Y(C_n \boxminus C_m) = 16nm^4 + 64nm^3 + 96nm^2 + 320nm + 32n$

207  $Y(C_n \boxminus P_m) = 16nm^4 + 64nm^3 + 96nm^2 + 320nm - 318n$

208

209 **2.5 The Vertex –edge corona.**

210 **Definition:**[6] The vertex –edge corona of two graphs  $A_1$  and  $A_2$  is denoted by  $A_1 \boxtimes A_2$  is

211 the graph obtained by taking one copy of  $A_1$ ,  $n_1$  copies of  $A_2$  and also  $m_1$  copies of  $A_2$ , then

212 joining the  $i$ -th vertex of  $A_1$  to every vertex in the  $i$ -th vertex copy of  $A_2$  and also joining the

213 end vertices of  $j$ -th edge of  $A_1$  to every vertex in the  $j$ -th edge copy of  $A_2$ .

214 Let the vertex set of the  $j$ -th edge copy of  $A_2$  is denoted by

215  $V_{je}(A_2) = \{u_{j1}, u_{j2}, \dots, u_{jn_2}\}$  and the vertex set of the  $i$ -th vertex copy of  $A_2$  is denoted by

216  $V_{iv}(A_2) = \{w_{i1}, w_{i2}, \dots, w_{in}\}$ . Also let us denote the edge set of the  $j$ -th edge and  $i$ -th vertex

217 copy of  $A_2$  by  $E_{je}(A_2)$  and  $E_{iv}(A_2)$  respectively. According to this definition we have the

218 vertex –edge corona  $A_1 \boxtimes A_2$  has  $m_1 + m_1(m_2 + 2m_2) + n_1n_2 + n_1m_2$  edges and  $n_1 + n_1n_2 +$

219  $mn_2$  vertices .Also the degree of the vertices of  $A_1 \boxtimes A_2$  are given by

$$\begin{aligned}
d_{A_1 \boxtimes A_2}(v_i) &= (n_2 + 1)d_{A_1}(v_i) + n_2 \forall v_i \in V(A_1) \\
d_{A_1 \boxtimes A_2}(e_i) &= d_{A_2}(u_j) + 2 \forall u_{ij} \in V_{ie}(A_2) \\
d_{A_1 \boxtimes A_2}(v_j^i) &= d_{A_2}(w_j) + 1 \forall w_{ij} \in V_{ie}(A_2)
\end{aligned}$$

220

221

222 **Theorem.2.9**

223 The Y-index of  $A_1 \boxtimes A_2$  is given by

$$224 Y(A_1 \boxtimes A_2) = Y(A_1)(n_2 + 1)^4 + 4(n_2 + 1)^3 Y(A_1)n_2 + 6n_2^2(n_2 + 1)^2 M_1(A_1) + 8m_1(n_2 + 1)$$

225

$$n_2^3 + n_1 n_2^4 + m_1 Y(A_2) + 8m_1 F(A_2) + 24M_1(A_2)m_1 + 8n_1 m_2 + n_1 n_2$$

226

227 Proof: From the definition of vertex-edge corona of graphs, we have

$$228 Y(A_1 \boxtimes A_2) = \sum_{v_i \in V(A_1)} d_A(v_i)^4 + \sum_{e_i \in E(A_1)} \sum_{u_{ij} \in V(A_2)} d_A(u_{ij})^4 + \sum_{v_i \in V(A_1)} \sum_{w_{ij} \in V(A_2)} d_A(w_{ij})^4$$

$$229 = S_1 + S_2 + S_3 \text{ (say)}$$

230 We have now determined by calculating  $S_1$ 's contribution

$$231 S_1 = \sum_{v_i \in V(A_1)} d_A(v_i)^4$$

$$232 = \sum_{v_i \in V(A_1)} [(n_2 + 1)d_{A_1}(v_i) + n_2]^4$$

$$233 = (n_2 + 1)^4 Y(A_1) + 4(n_2 + 1)^3 F(A_1)n_2 + 6(n_2 + 1)^2 M_1(A_1)n_2^2$$

$$234 + 8(n_2 + 1)m_1 n_2^3 + n_1 n_2^4 \text{ -----} \rightarrow (1)$$

235

236

237 Also, we have the contribution of  $S_2$  as

$$238 S_2 = \sum_{e_i \in E(A_1)} \sum_{u_{ij} \in V(A_2)} d_A(u_{ij})^4$$

$$239 = \sum_{e_i \in E(A_1)} \sum_{u_{ij} \in V(A_2)} [d_{A_2}(u_j) + 2]^4$$

$$240 = m_1 Y(A_2) + m_1 8F(A_2) + 24m_1 M_1(A_2) + 64m_1 m_2 + 16m_1 n_2 \text{ -----} \rightarrow (2)$$

241

242 Similarly, we get the  $S_3$ 's contribution

$$243 S_3 = \sum_{v_i \in V(A_1)} \sum_{w_{ij} \in V(A_2)} d_A(w_{ij})^4$$

$$244 = \sum_{v_i \in V(A_1)} \sum_{w_{ij} \in V(A_2)} [d_{A_2}(w_j) + 1]^4$$

$$245 = n_1 Y(A_2) + n_1 4F(A_2) + 6n_1 M_1(A_2) + 8n_1 m_2 + n_1 n_2 \text{ -----} \rightarrow (3)$$

246

247 After adding (1), (2) and (3) we obtain the equality in the statement of the theorem as

248 required

249

250 **Corollary. 2.10**

$$251 Y(P_n \boxtimes P_m) = 81nm^4 - 130m^4 + 216nm^3 - 368m^3 + 216nm^2 - 384m^2 + 433nm - 432m -$$

252  $480n + 336$

$$253 Y(C_n \boxtimes C_m) = 81nm^4 + 216nm^3 + 216nm^2 + 465nm + 16n$$

254

$$255 Y(C_n \boxtimes P_m) = 81nm^4 + 216nm^3 + 216nm^2 + 465nm - 464n$$

256 **3. CONCLUSION**

257

258 The corona product can be used to improve the latest scientific advancements, like the  
259 Internet of Things, Virtual Reality, and Augmented Reality, among others. Corona Product is  
260 so crucial to our inquiry. The Y-index of various corona products, including subdivision-  
261 vertex corona, subdivision-edge corona, subdivision-vertex neighborhood corona,  
262 subdivision-edge neighborhood corona, and vertex-edge corona, are computed in this  
263 article. As a practical example, we develop some explicit corona product formulas for  
264 specific graphs.

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